

Getting life started:

Self-organized carbon fixation

Day II outline

- Properties of carbon fixation in modern life
- Concepts of self-organization
- Analyzing carbon fixation as a self-organizing process

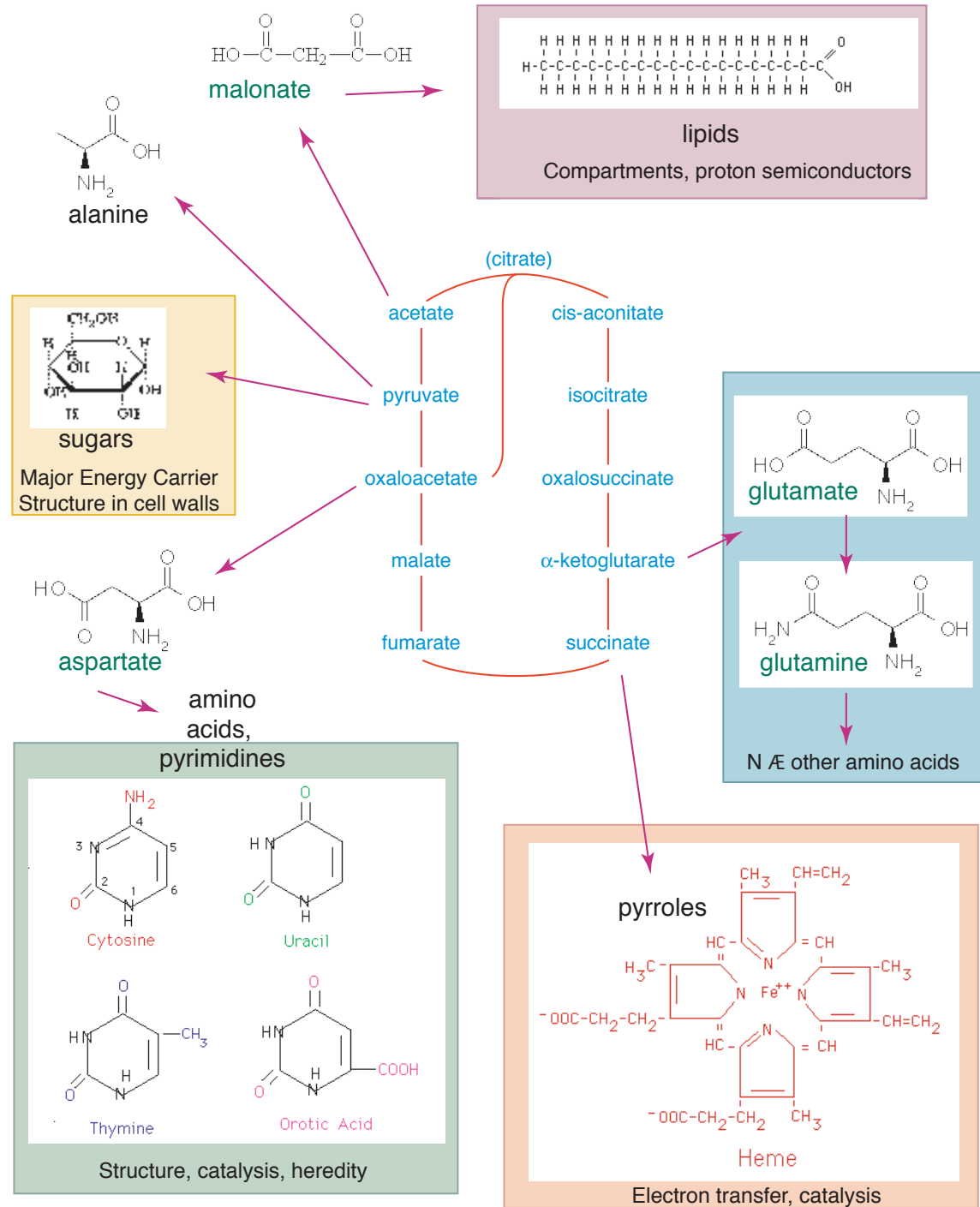
Carbon fixation and its properties in modern life

- Simple universal core
- Creating biomass is a way to release energy
- Core (TCA) cycle has 3 key properties
 - Simple and small
 - Biomass arises naturally
 - Favorable chemistry with carbon and energy sources
 - Possibly does not require containment in cells
 - Topology suggests exponential growth from random initial conditions

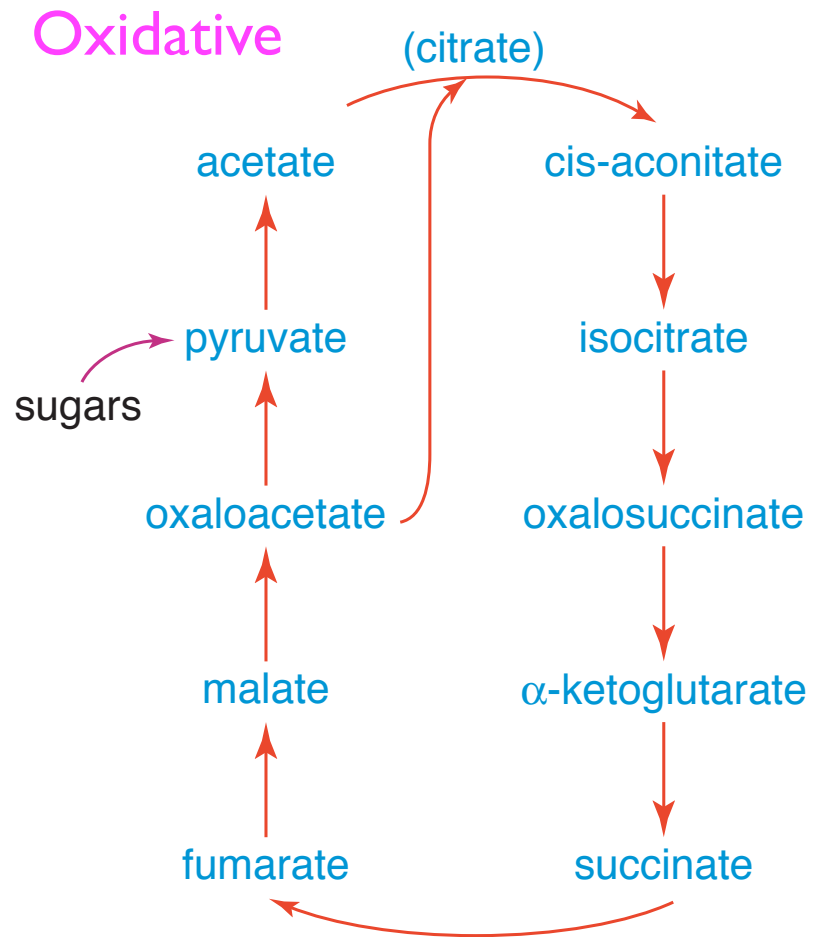
Carbon **anabolism** today begins within the “Krebs” (or TCA) cycle

(Tri-Carboxylic Acid cycle)

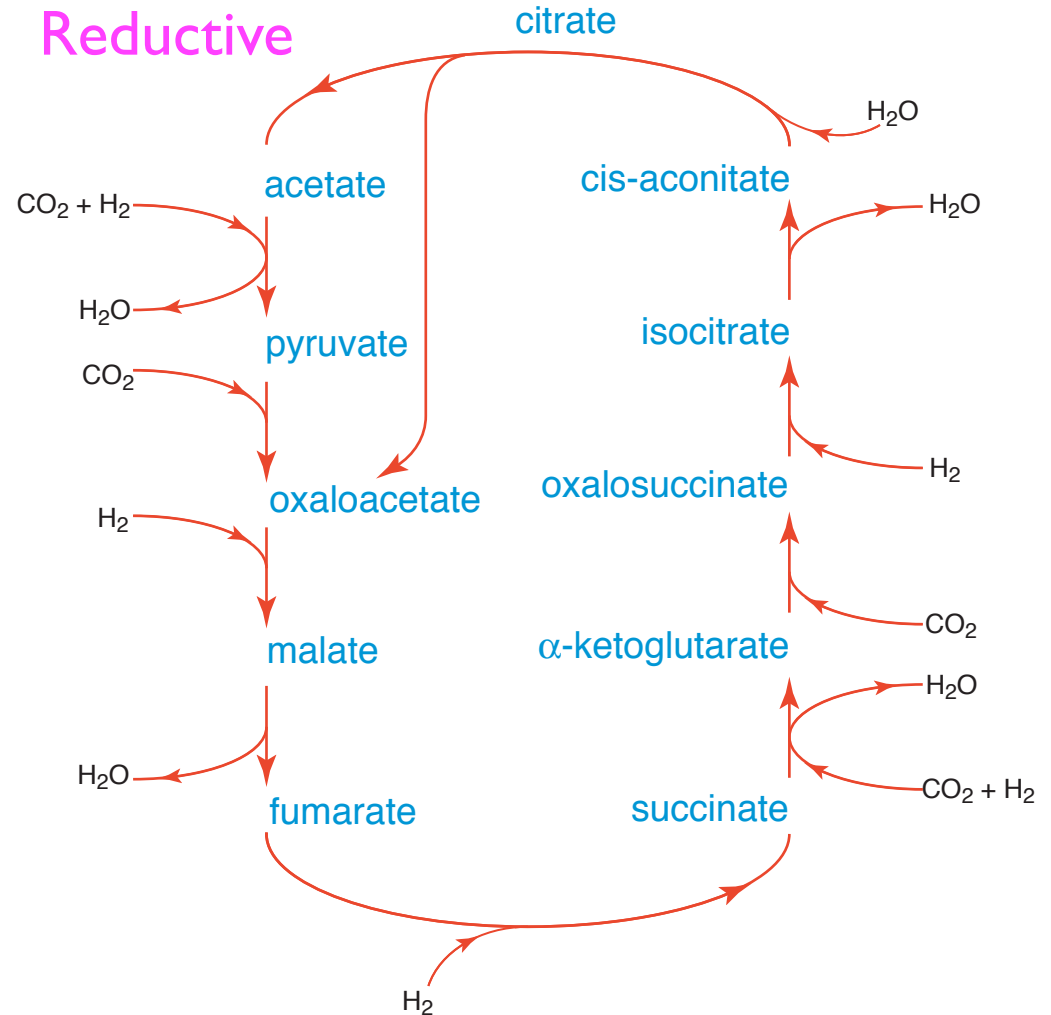
- TCA intermediates are synthetic precursors of:
 - lipids (Acetate)
 - sugars (Pyruvate)
 - amino acids (several)
 - nucleotides (OAA, AKG)
 - porphyrins (Succinate)



The universal reactions can run in either direction



(Takes in sugars or fats & water, to make energetic electrons, CO_2 , and precursors)



(Takes in CO_2 and electrons, to make water and precursors)

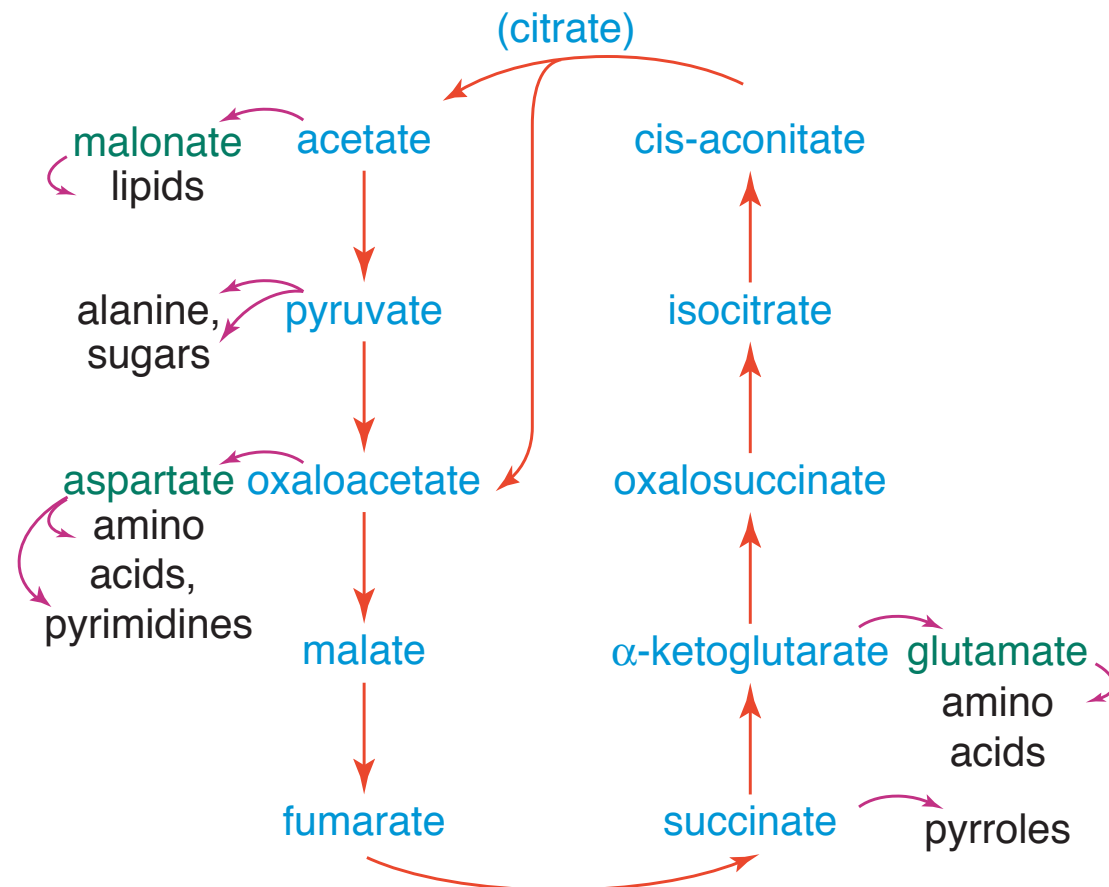
Anabolism is an electron-consuming (reducing) process; therefore possibly older than catabolism

- **Reductive** TCA (rTCA) cycle is a *carbon fixation* pathway that serves as the start for anabolism

- All the arrows in the reductive cycle go the same way:

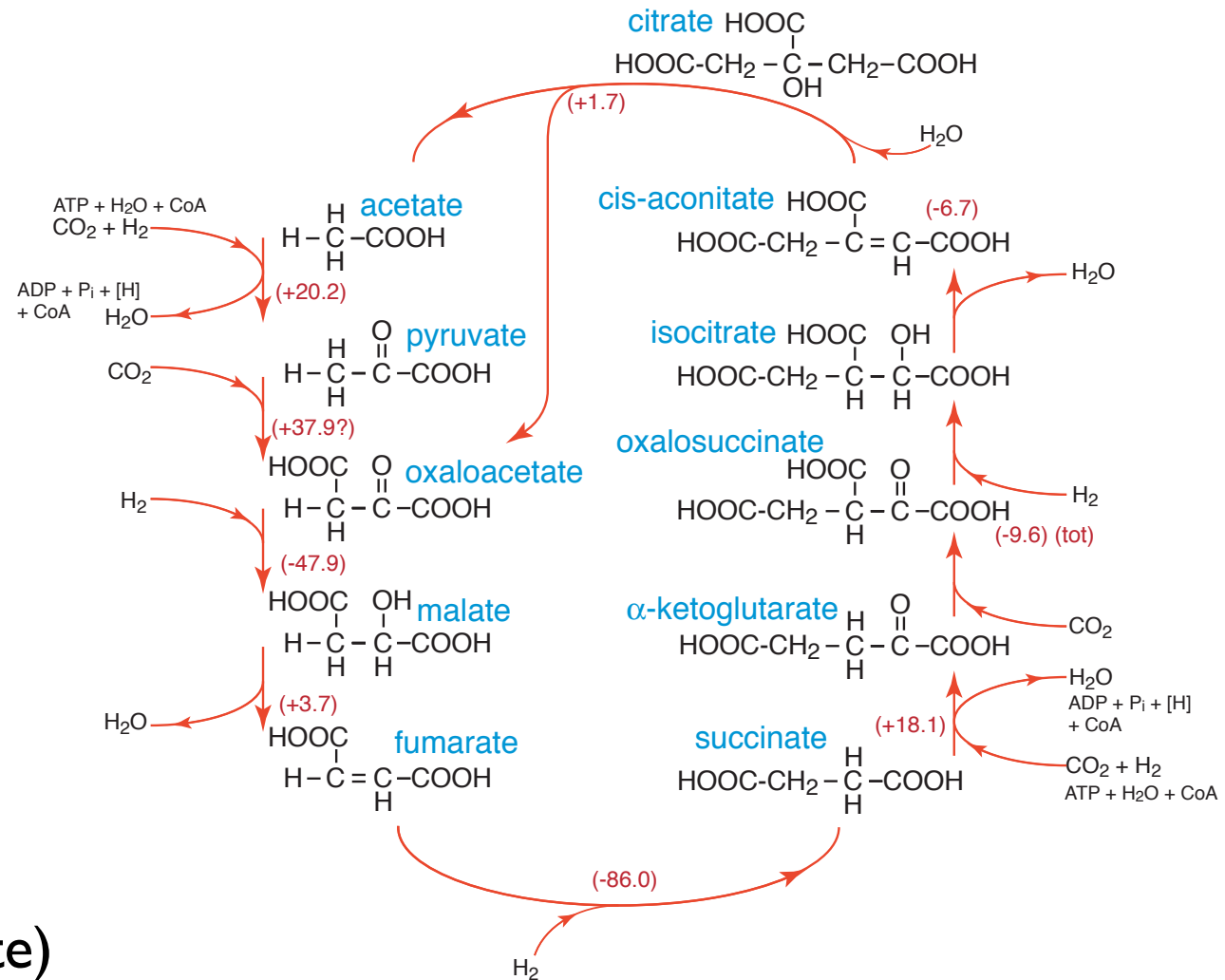
- Reducing CO_2 to acetate

- Producing complex biomolecules from simple inputs



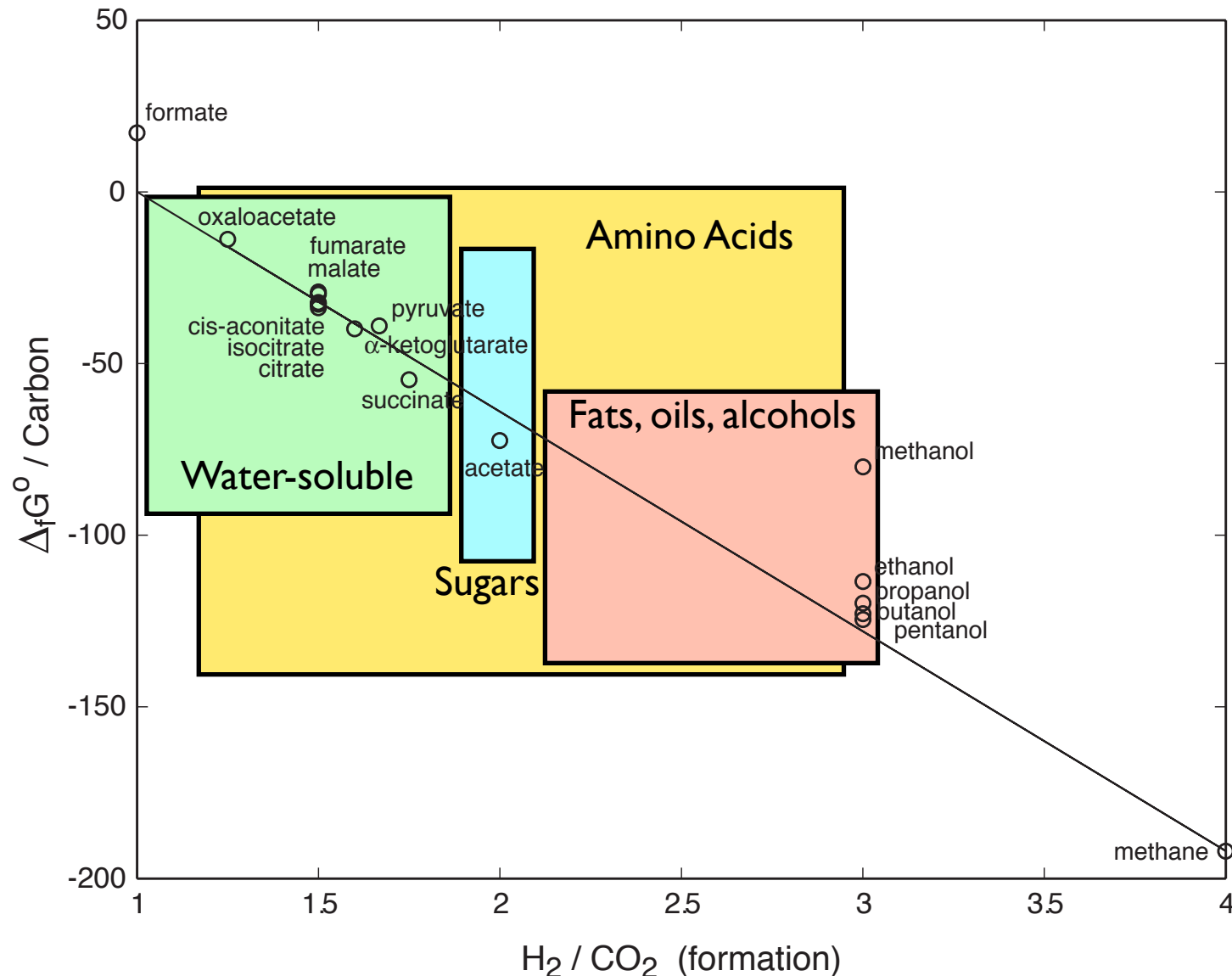
The chemical structures and reactions of the reductive TCA cycle

- In each reaction $C=O$ or $O-C=O$ from CO_2 is incorporated into a growing C chain, or else C or O is reduced
- C_4 (oxaloacetate) forms a starting state
- C_6 (citrate) fragments to give C_2 (acetate) and recover C_4 (oxaloacetate)



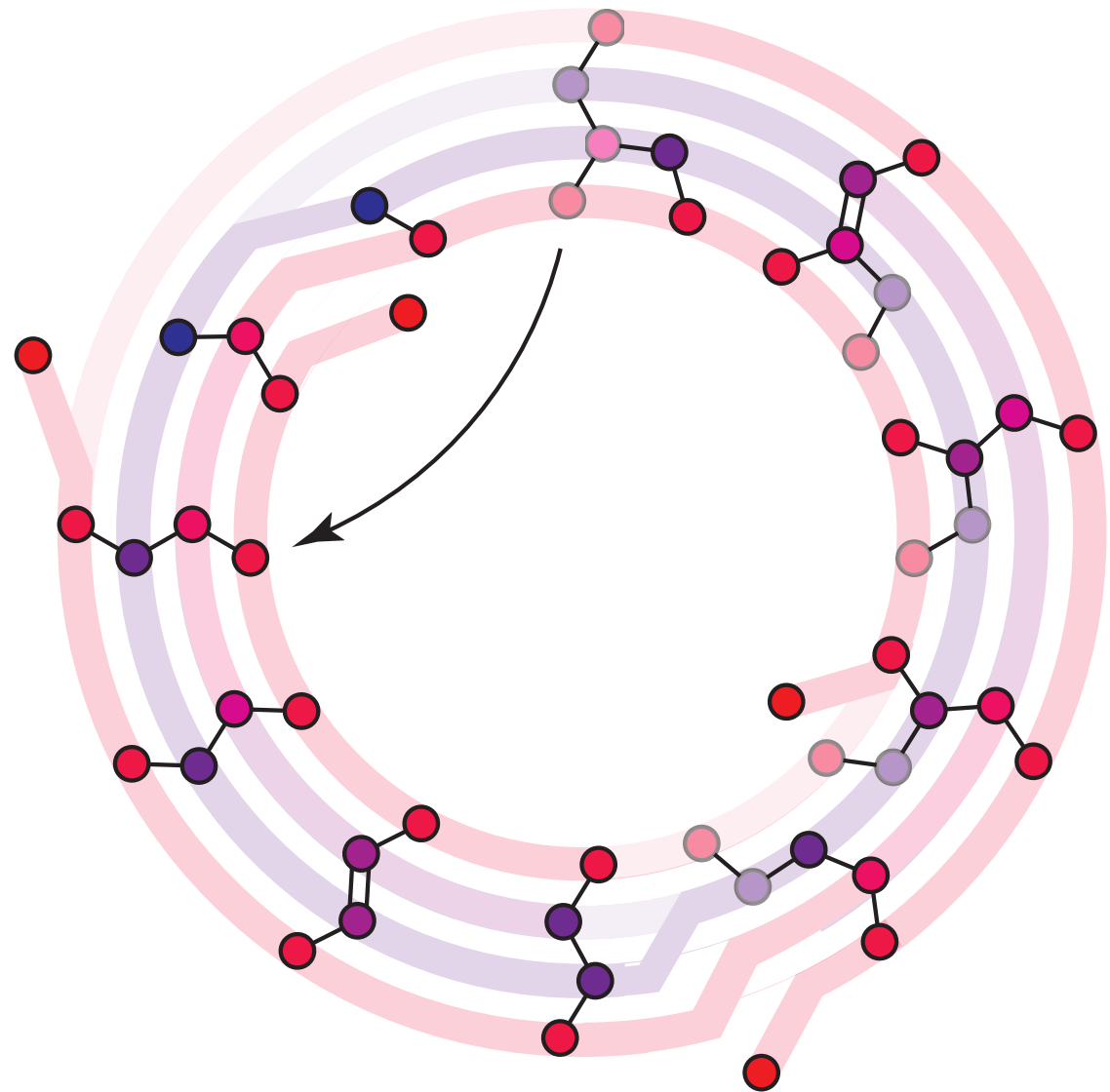
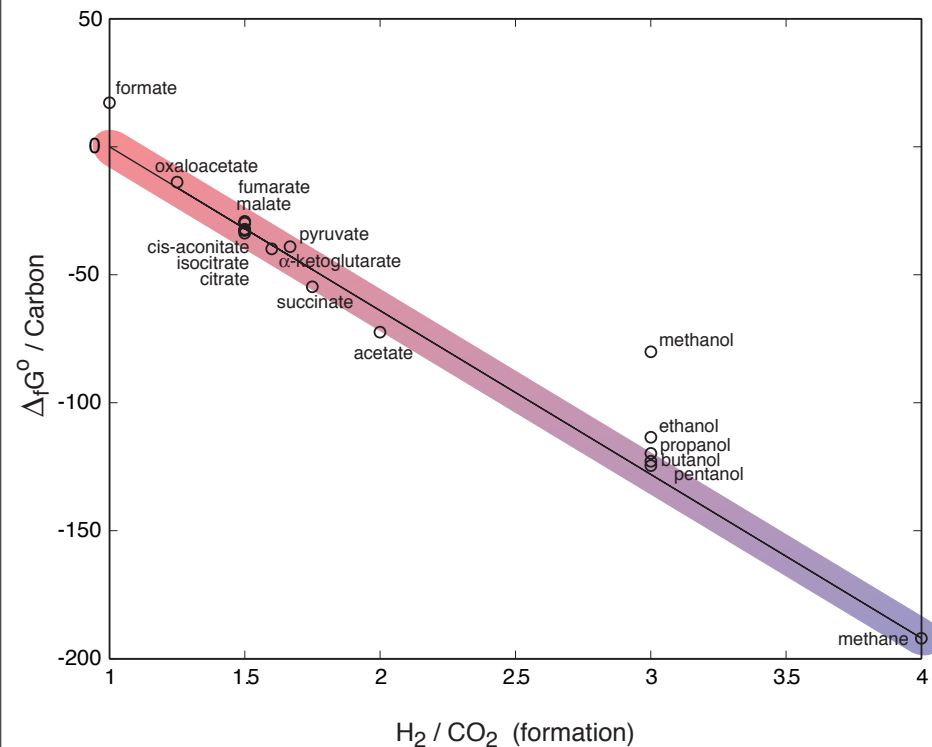
Biosynthesis is energy-yielding in a reducing world

- Extract energy and build biomass *at the same time*
- Biosynthesis only needs to “capture” carbon on the way from CO_2 to CH_4



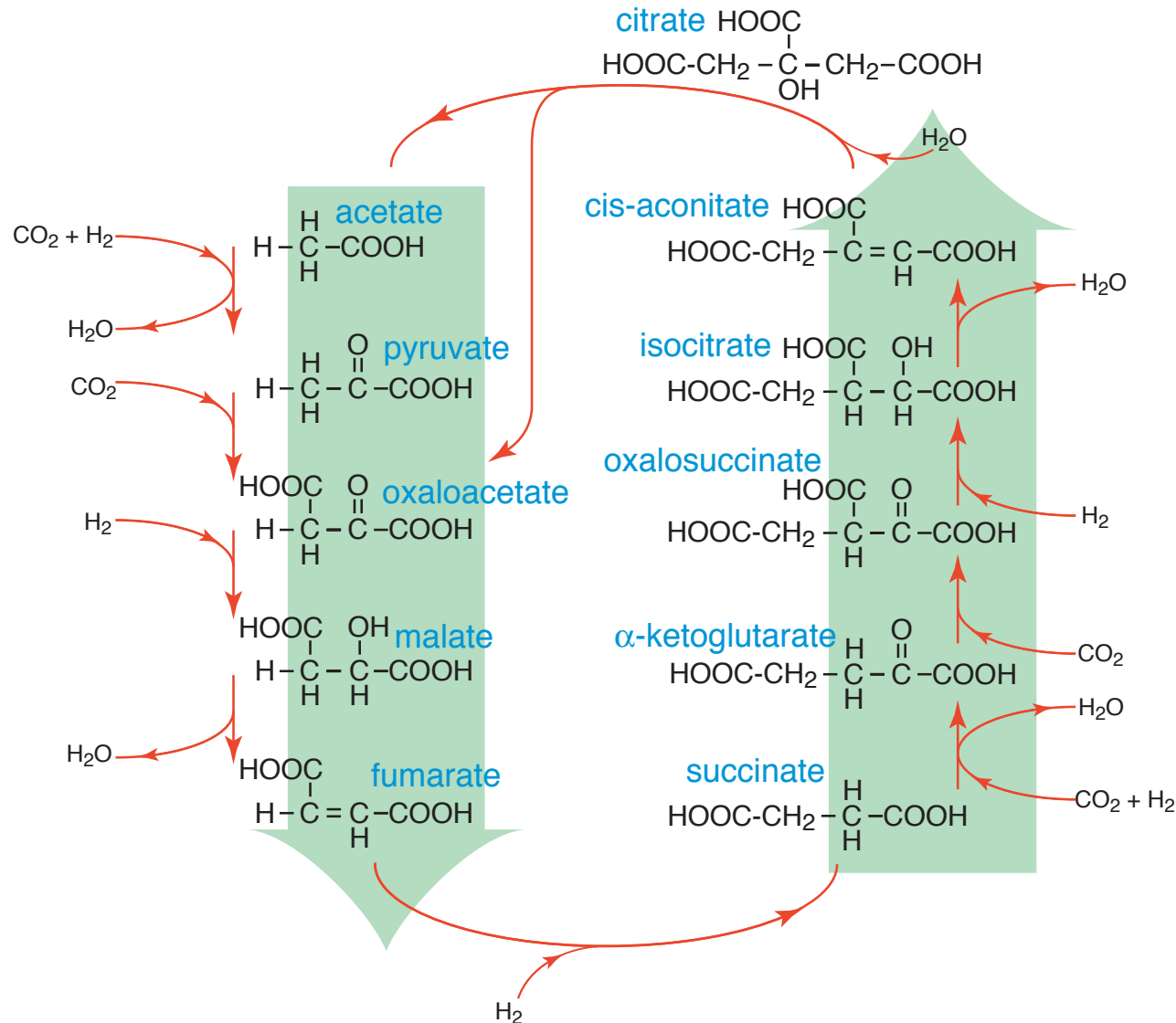
Downhill flow of carbon in reductive TCA

-4 -3 -2 -1 0 +1 +2 +3



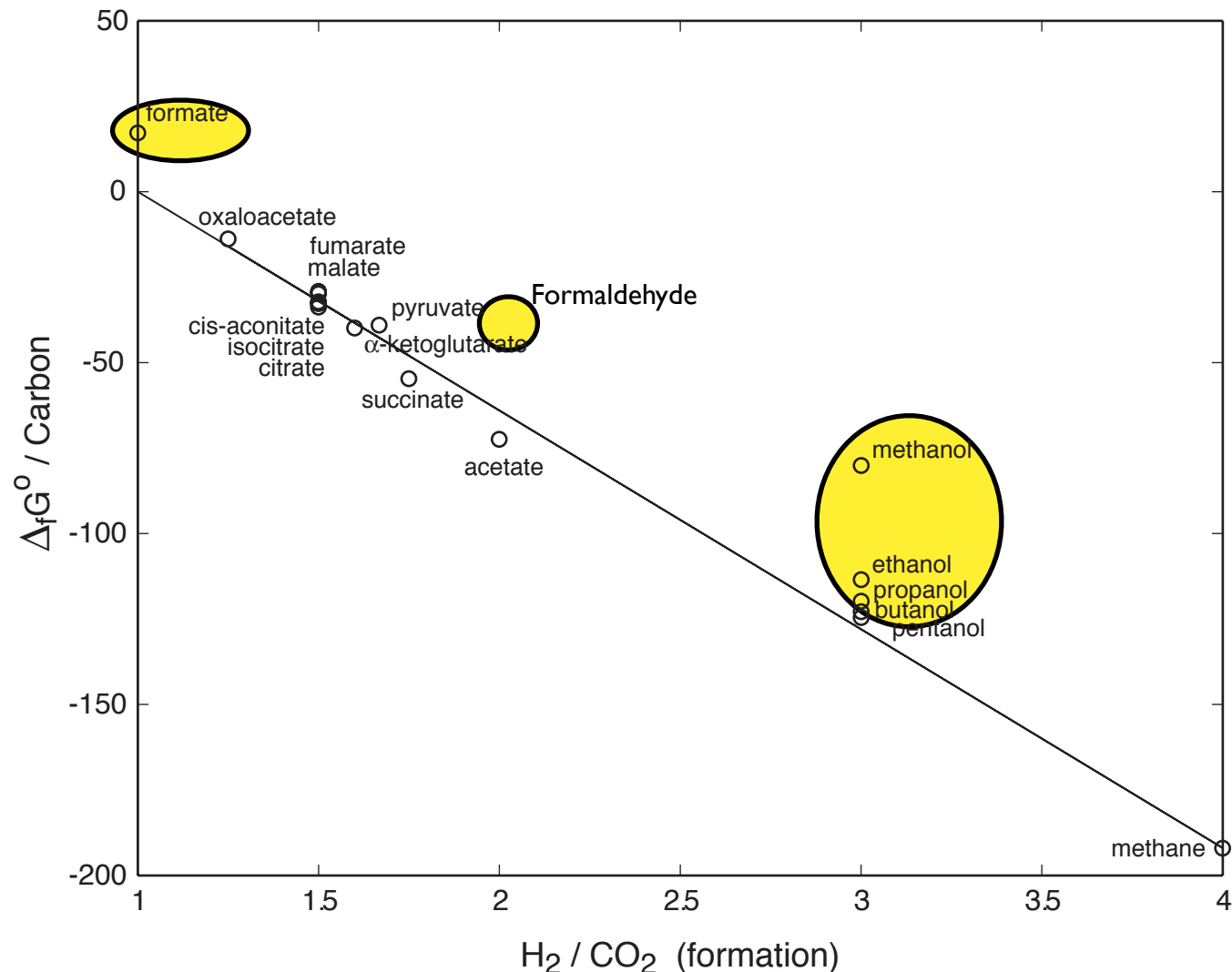
The reductive TCA reactions are few and simple; plausible as primordial “discoveries”

- Only **5** molecular groups and **7** reactions required
- Simplicity may have made the reactions easy to find in a random world



rTCA gets from *simple* CO₂ to *simple* CH₄ through *more complex* intermediate compounds

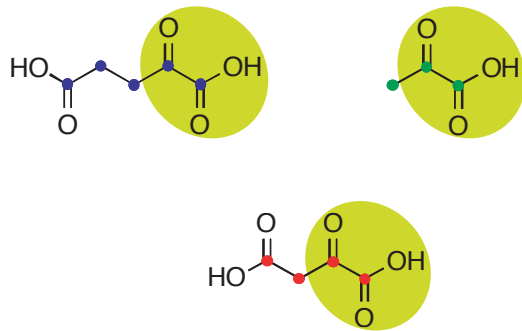
- Inputs and outputs are simple: but *there are no simple, low-energy intermediate compounds*
- Flow into cycle intermediates is thermodynamically favored over flow to smaller molecules at same oxidation states



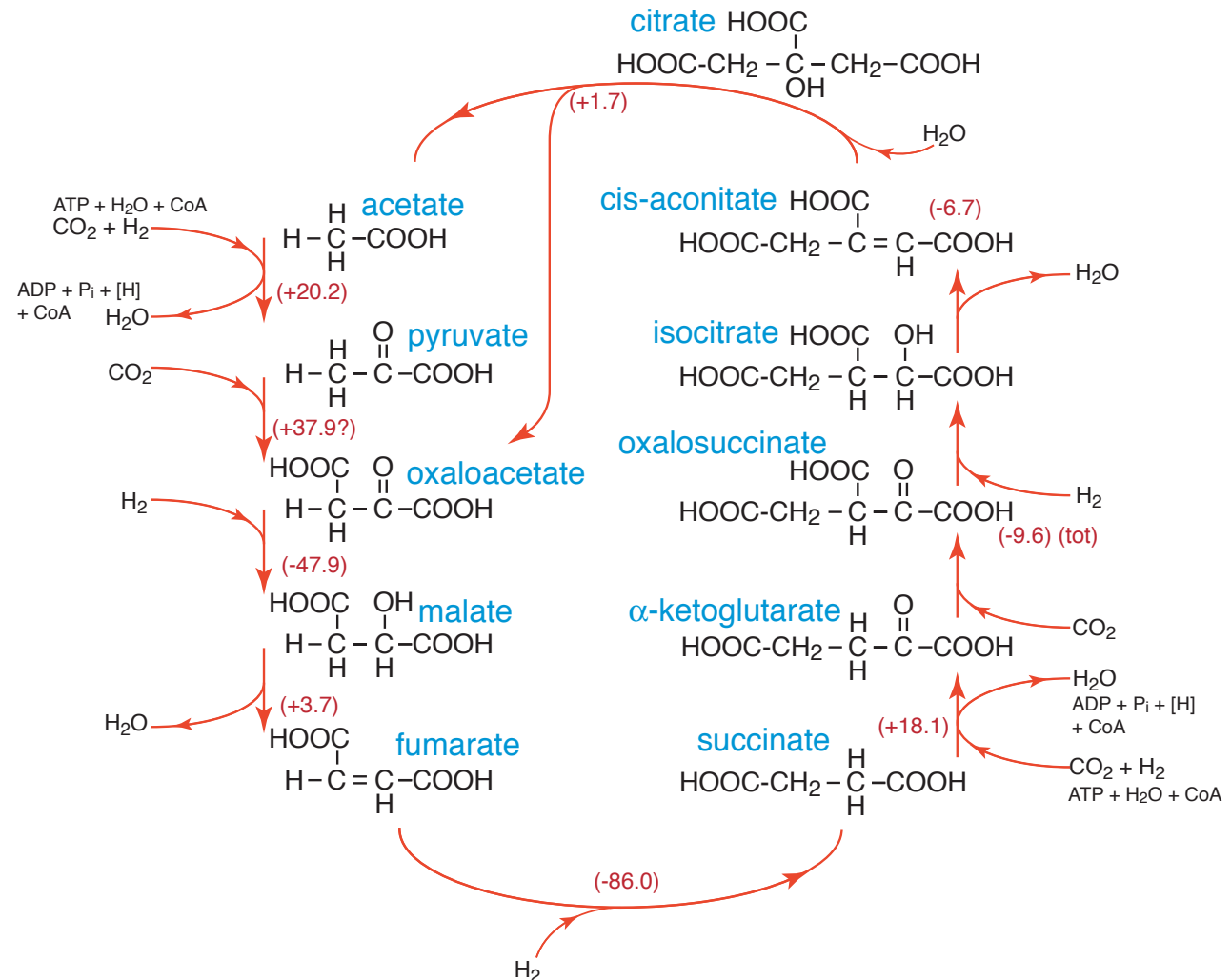
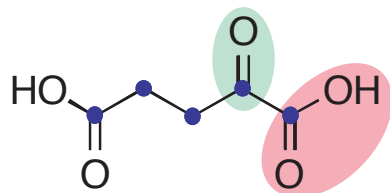
(Explain *why* biomolecules exist before Darwinian selection)

rTCA molecules favor reactions to capture CO₂ as a carbon source (difficult to do)

Compounds in the cycle are known as “alpha-keto” acids



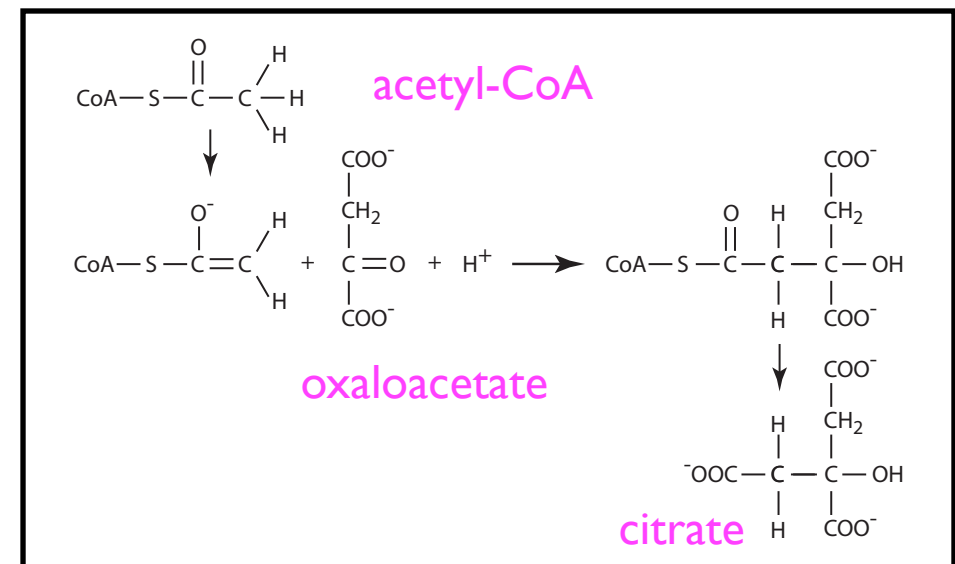
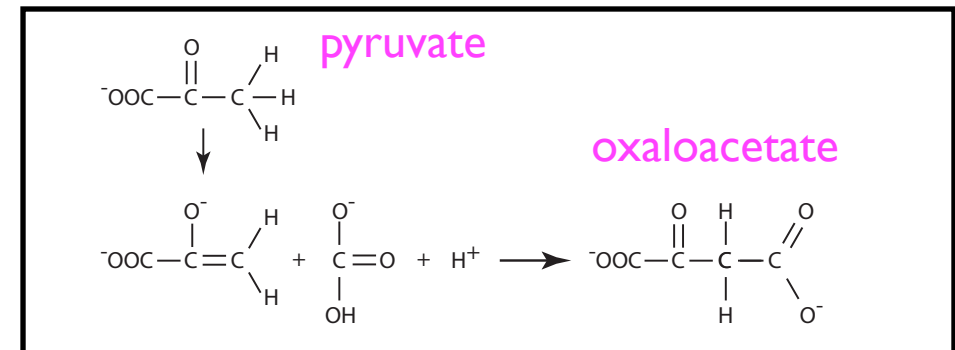
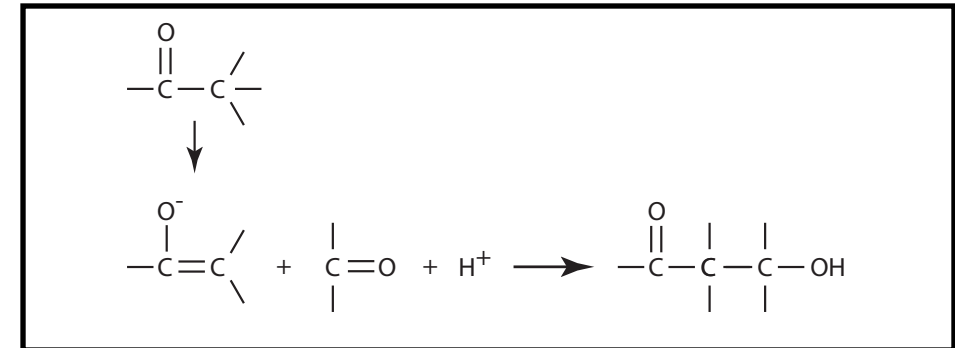
Reactive groups are **carboxyl** and **alpha-ketone**



Why alpha (or beta) ketone structure is important for carbon uptake

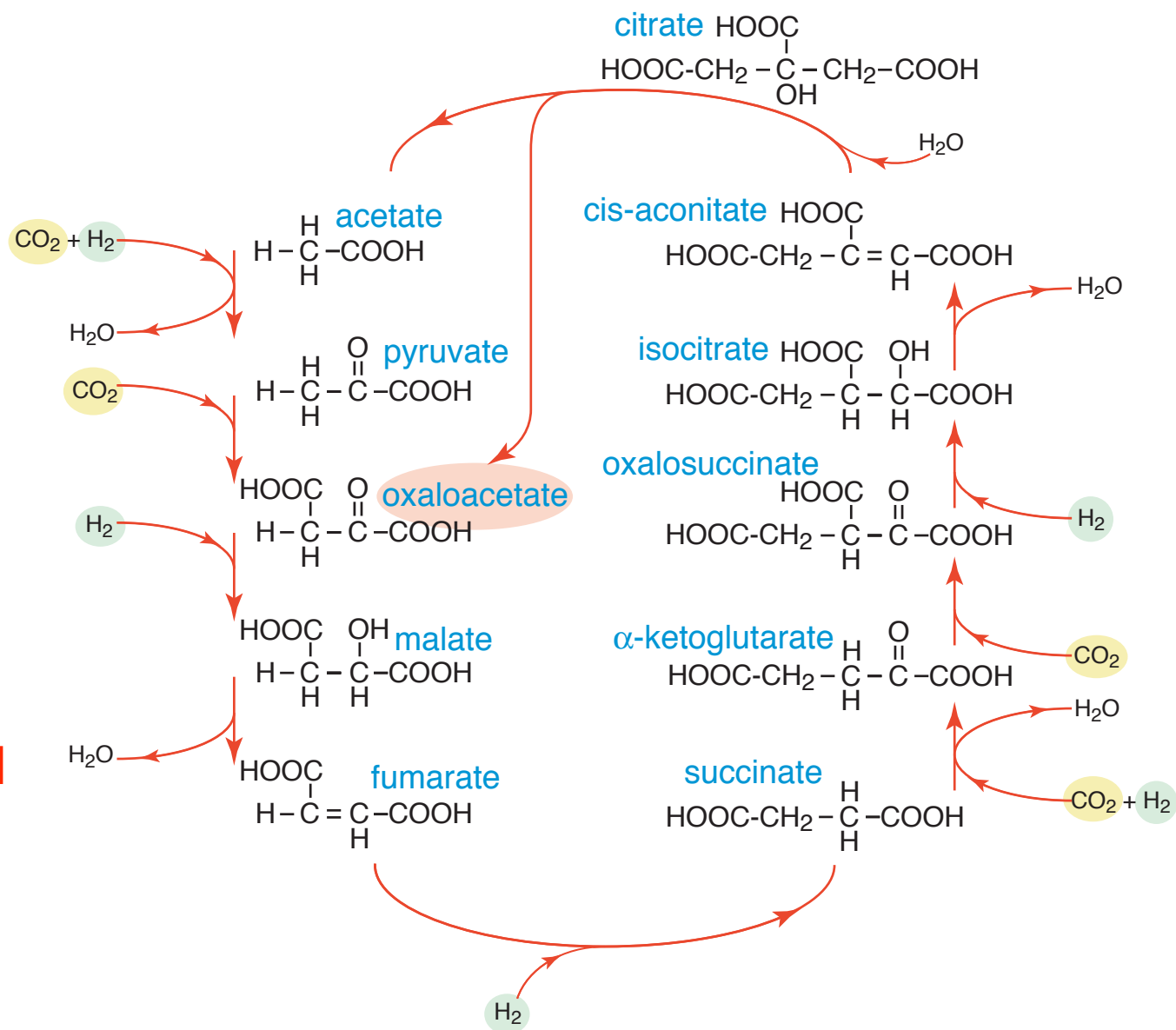
- How do we put electron density on a carbon to form a C-C bond? (Aldol condensation)
- A related reaction incorporates bicarbonate into pyruvate to form oxaloacetate
- The aldol condensation and its reverse are responsible for citrate formation or cleavage (which solve problems in oxidative and reductive worlds respectively)

These reactions make rTCA reactions “low-resistance”



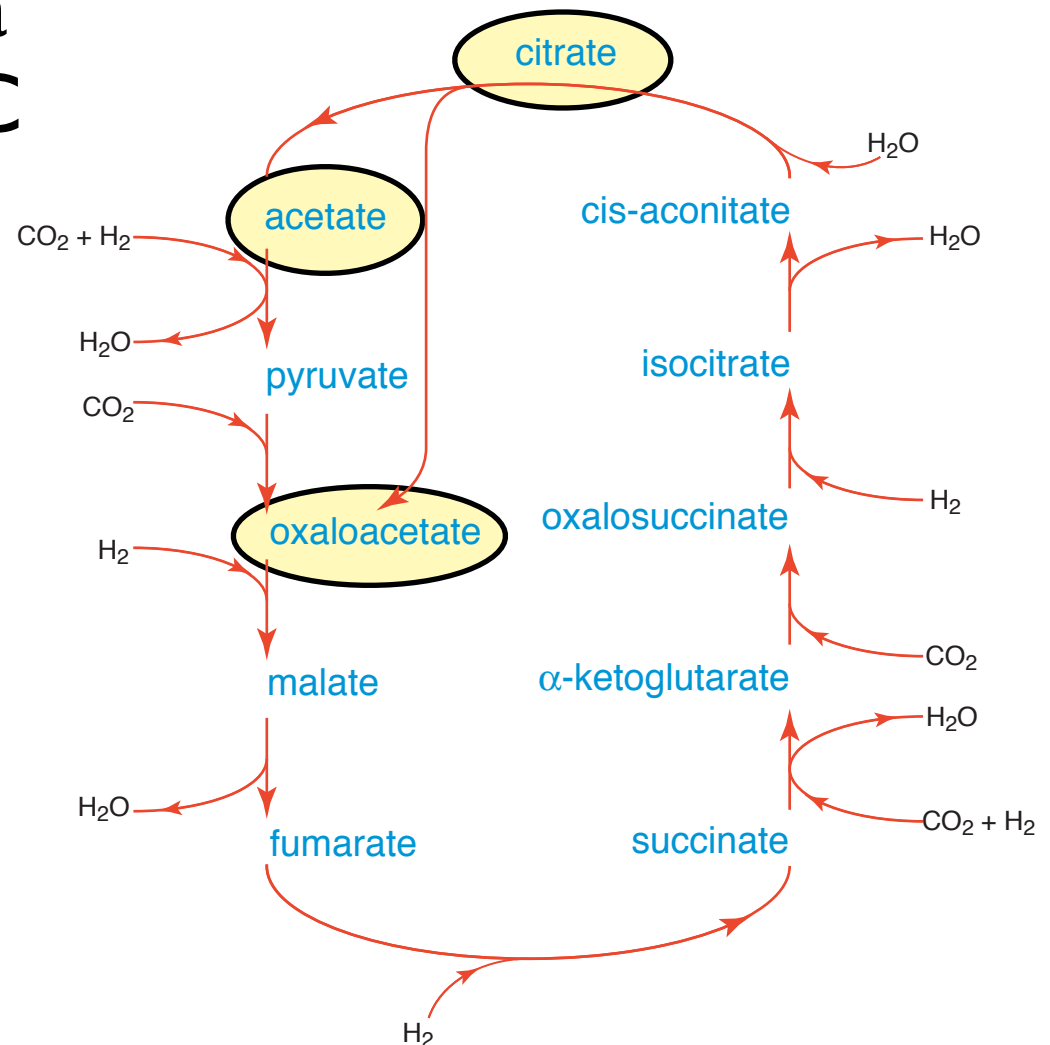
rTCA reactions are *first order* in complex molecules

- Oxaloacetate converts a 6-body reaction for CO_2 reduction to acetate into a sequence of simpler reactions
- No benefit from compartmentation in a pre-enzymatic world
- Suggests the cycle could have been a pre-cellular bulk-phase process



Network autocatalysis (from topology) potentially creates exponential growth from small numbers

- Oxaloacetate (C₄) is a network catalyst for C reduction
- Fission of citrate generates *two* cycle intermediates
- Regeneration of Oxa from Ace gives *two* seeds from one



Interpreting carbon fixation in terms of self-organization

- Energy flow through a system orders that system
- The onset of order can be a phase transition
- Creation of order lowers the impedance to flow (idea of a “bottleneck”)

Nonequilibrium states can be stable when they are *energy channels*

- Weather is powered by absorption of sunlight in the oceans
 - Converts visible to microwave photons
 - However, too diffuse to power chemistry
- Lightning (dielectric breakdown of atmosphere) driven by charge separation (created in turn by convective weather)
- Both create stable nonequilibrium states



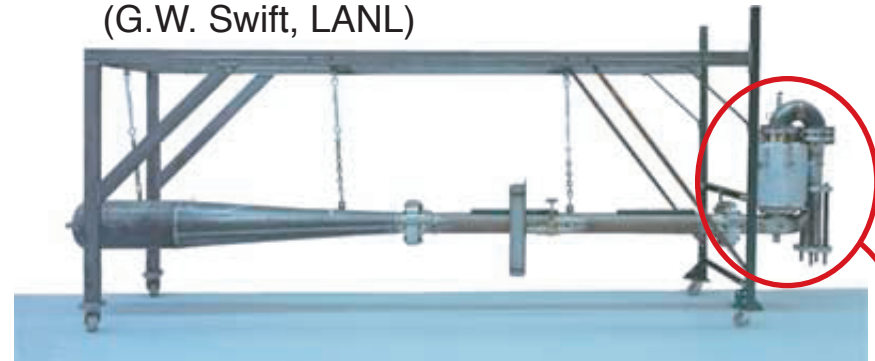
A simple reversible model for self-organizing energy channels

- Heat engines with no (mechanical) moving parts
- Self-starting, *self-organizing*
- Form order in the limit of *reversible thermodynamics*
- Order forms by *phase transition*, consistent with maximum uncertainty

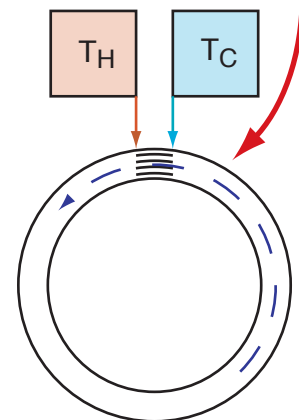
Tempest



Traveling-Wave Thermoacoustic Engine
(G.W. Swift, LANL)

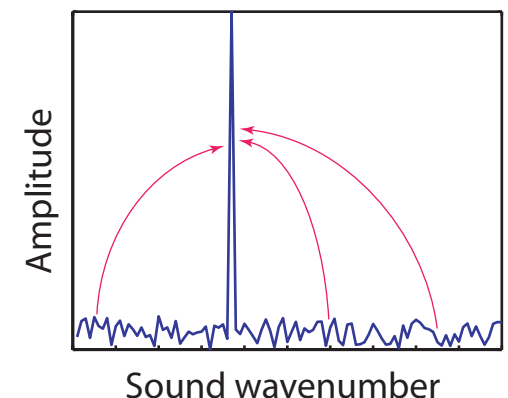
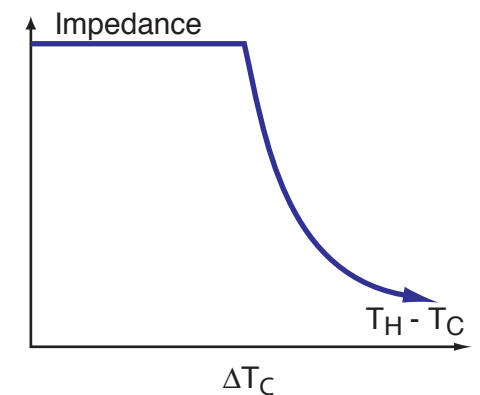
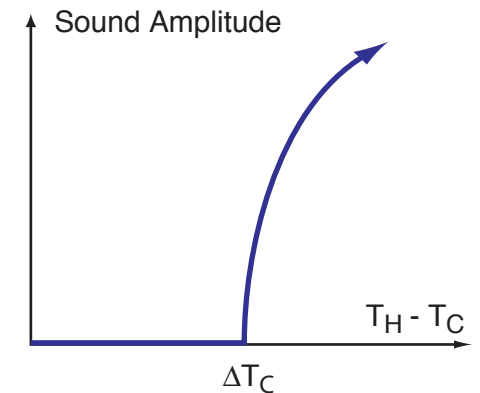


Tempest in a teapot



Emergent order lowers impedance to energy flow by a *phase transition*

- Sound amplitude is the “order parameter”
- Onset of order lowers system resistance to energy transfer:
 - “Off” impedance is high;
 - “On” Impedance decreases as the square of the sound amplitude
- Order forms by a process of “acoustic lasing”

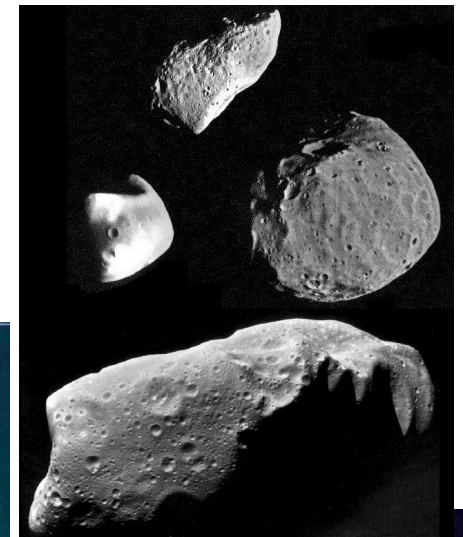
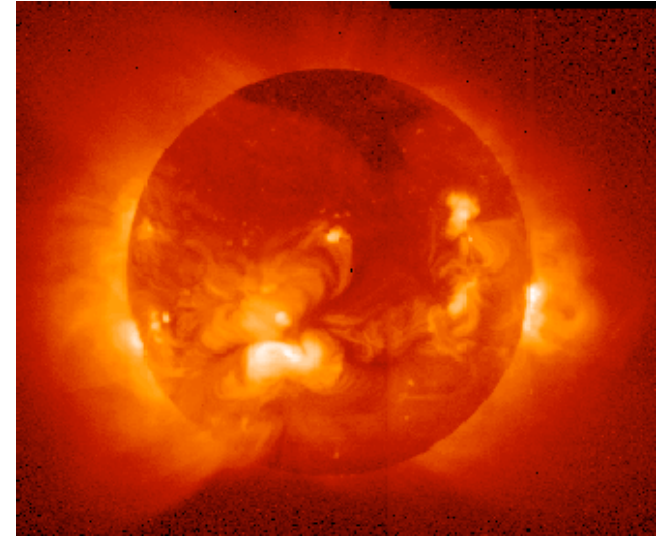


So can we apply the same idea to chemistry?

- What kinds of energy are relevant?
- Did the emergence of life create a low-resistance energy channel?

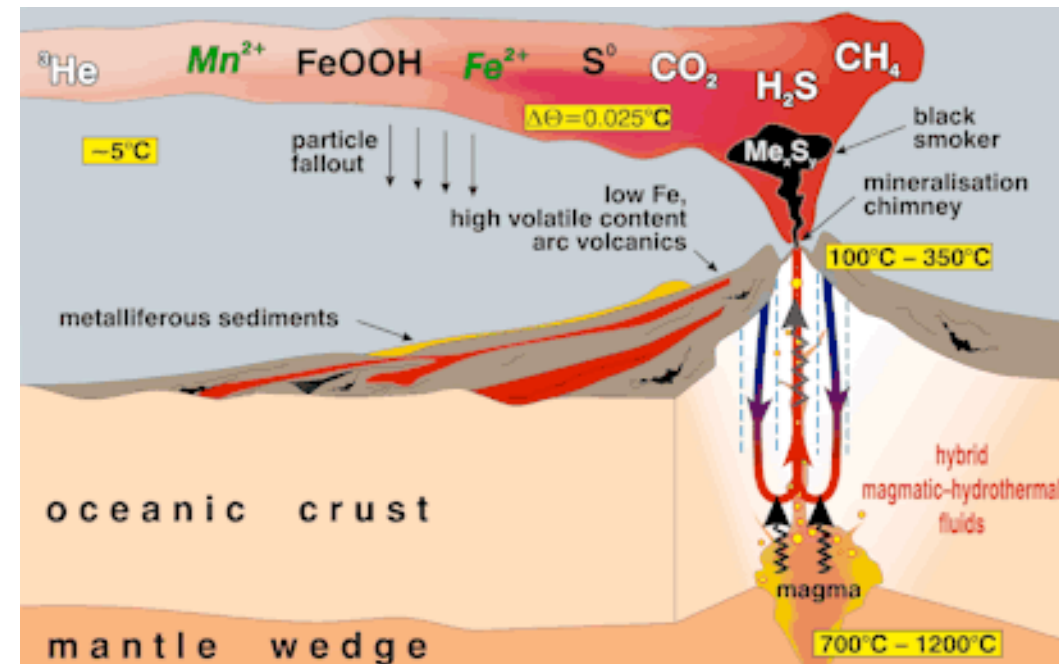
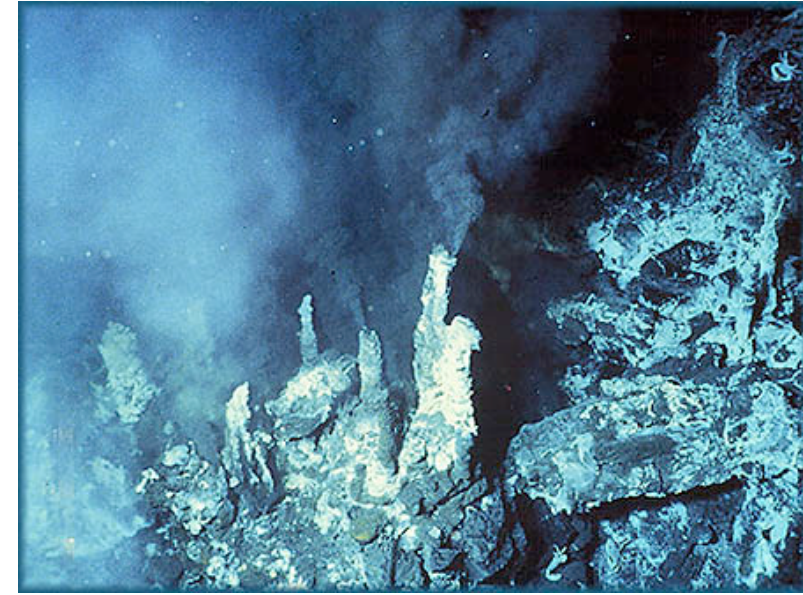
One energy source comes from stars (fusion)

- Stellar radiation can directly excite chemical bonds
 - Very high energy source
 - Difficult to capture, difficult to use
- Secondary reactions in comets, asteroids, and weather creates reactive organic species
- However, bio-molecules are *not special* in the resulting mixtures



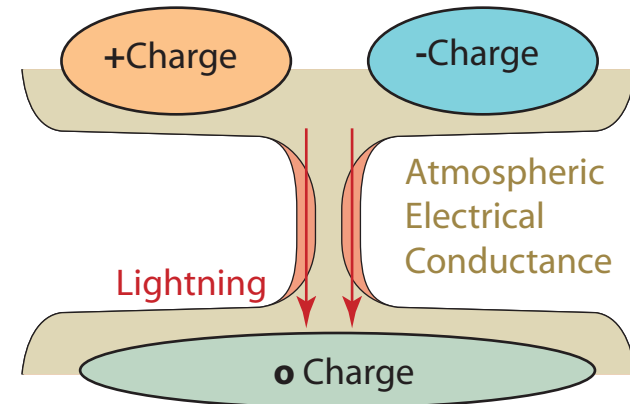
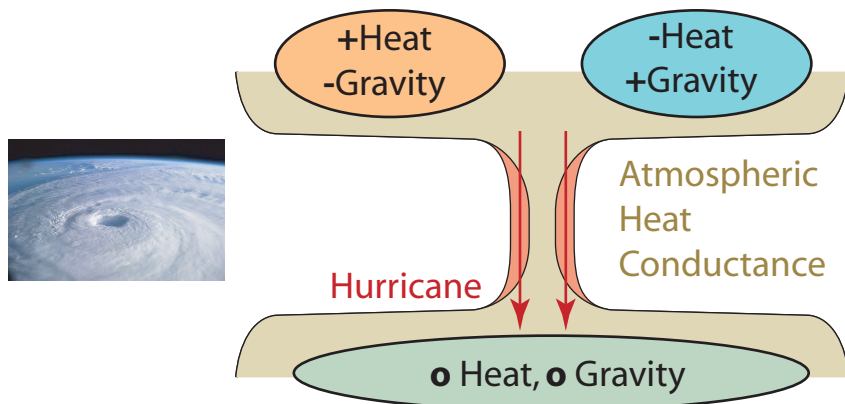
Direct chemical energy comes from earth (fission)

- Mantle convection (powered by heat transfer) trades gravitational for chemical energy
- Reduced metals in contact with seawater generate reductant (H), carbon sources and reduced metals
- Good food for life, but not so reactive that they make many molecules

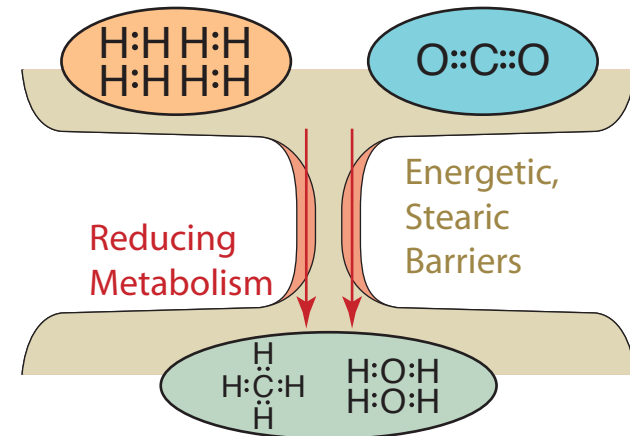
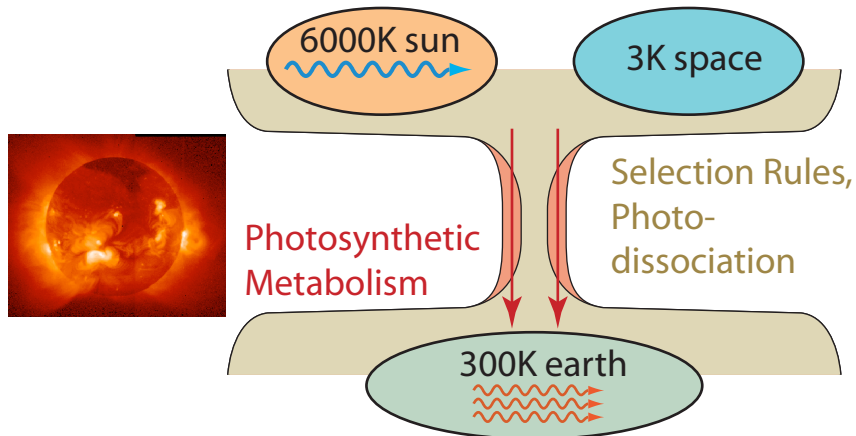


Compare energy channels from weather and life

The atmosphere is a poor conductor of heat and electricity

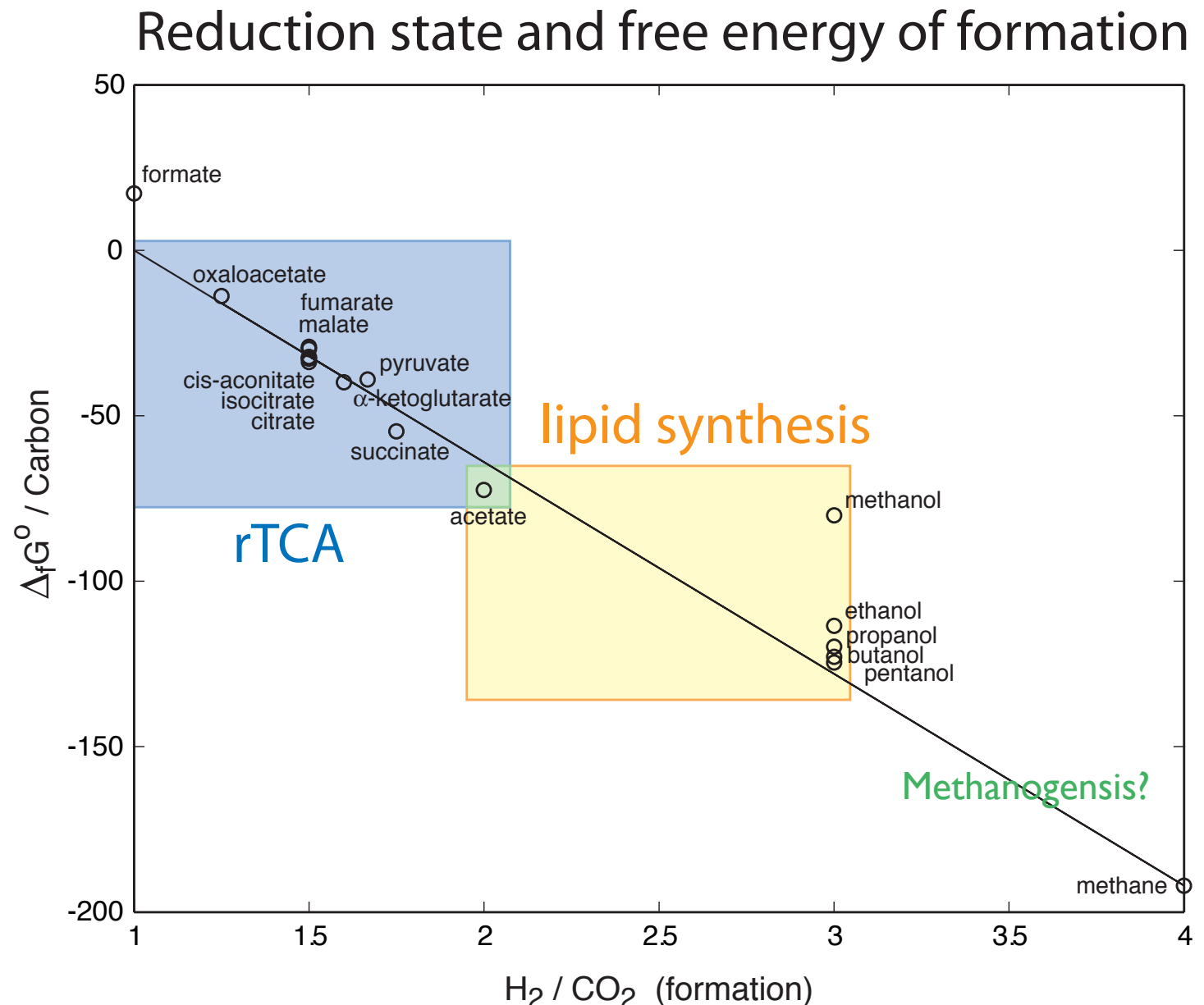


Non-living matter is a poor “conductor” of light across spectral bands, and electron pairs among bond types



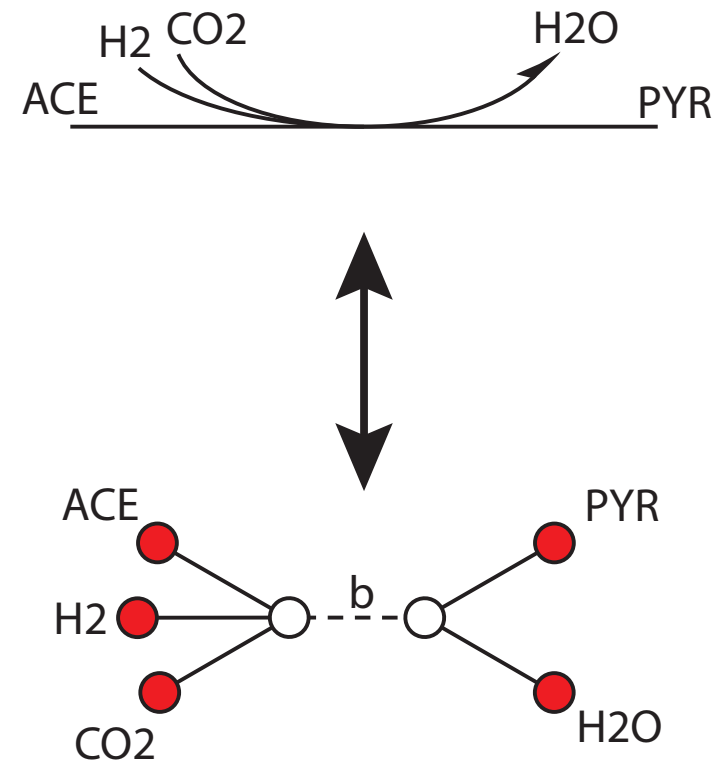
Can we analyze reducing metabolism explicitly as a self-organized channel?

- Break up the problem of CO₂ reduction into stages
- Each stage corresponds to a distinctive class of biomolecules and pathways
- Understand the emergence of the biomolecules as an energetic necessity



It is convenient to introduce a formal graph theory for chemical reactions

- Convert from chemical “hypergraphs” to formal bi-partite graphs
- Each graphical element corresponds to a mathematical term in a rate equation
- Reduction of graphs corresponds to aggregation of rate equations



Such representations are the basis of Flux Balance Analysis

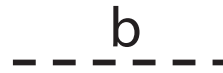
How to construct reaction rate graphs

Graph elements

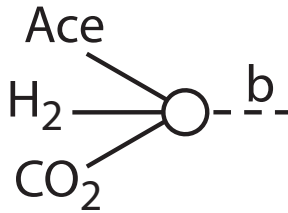
A concentration: [ACE]



A particular transition state, with current J_b



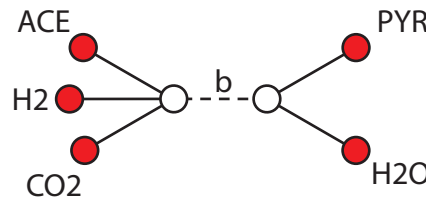
The forward reaction rate constant k_b



One mole of species ACE



A well-formed graph corresponding to the rate equation



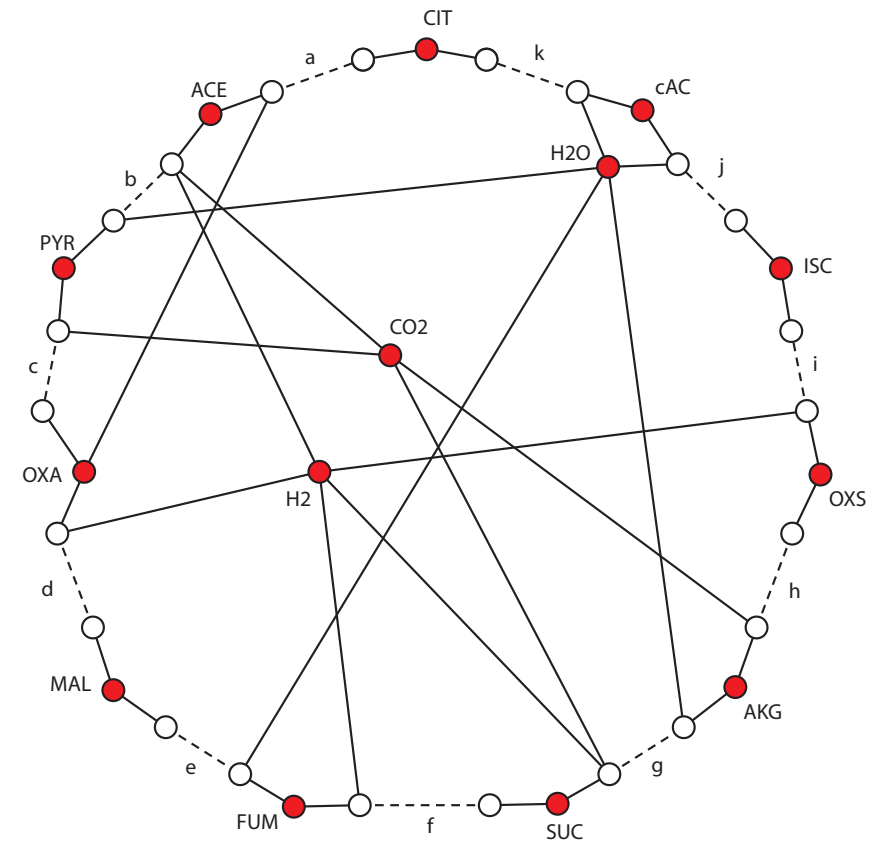
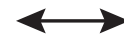
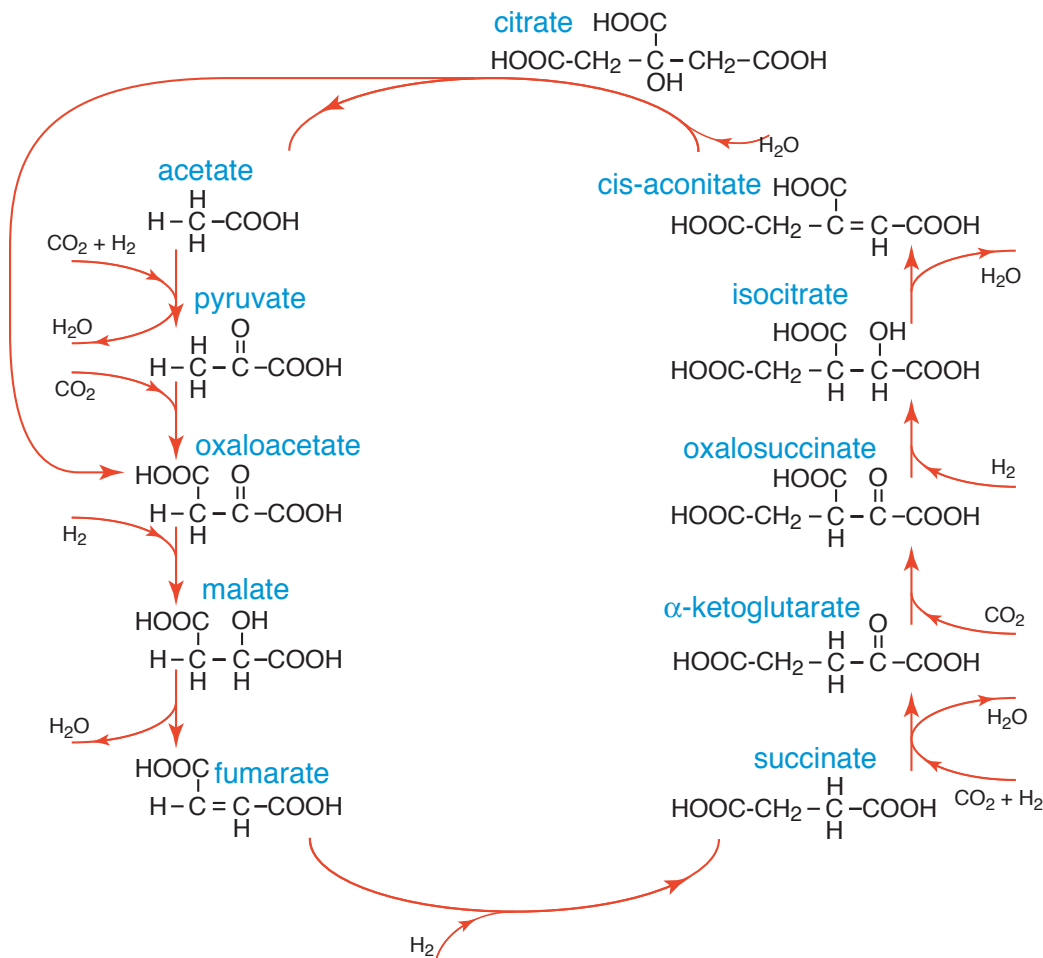
Graph rules

- Connect each species label on an open circle to the appropriate concentration with a solid line: one mole per line
- Connect the input and output circles for a reaction with a dashed line
- Compute transition state current as sum of forward and backward rates from its open circles
- Flows out of concentration dots equal transition currents times numbers of connecting lines

$$[ACE][H_2][CO_2] k_b - [PYR][H_2O] \bar{k}_b = J_b$$

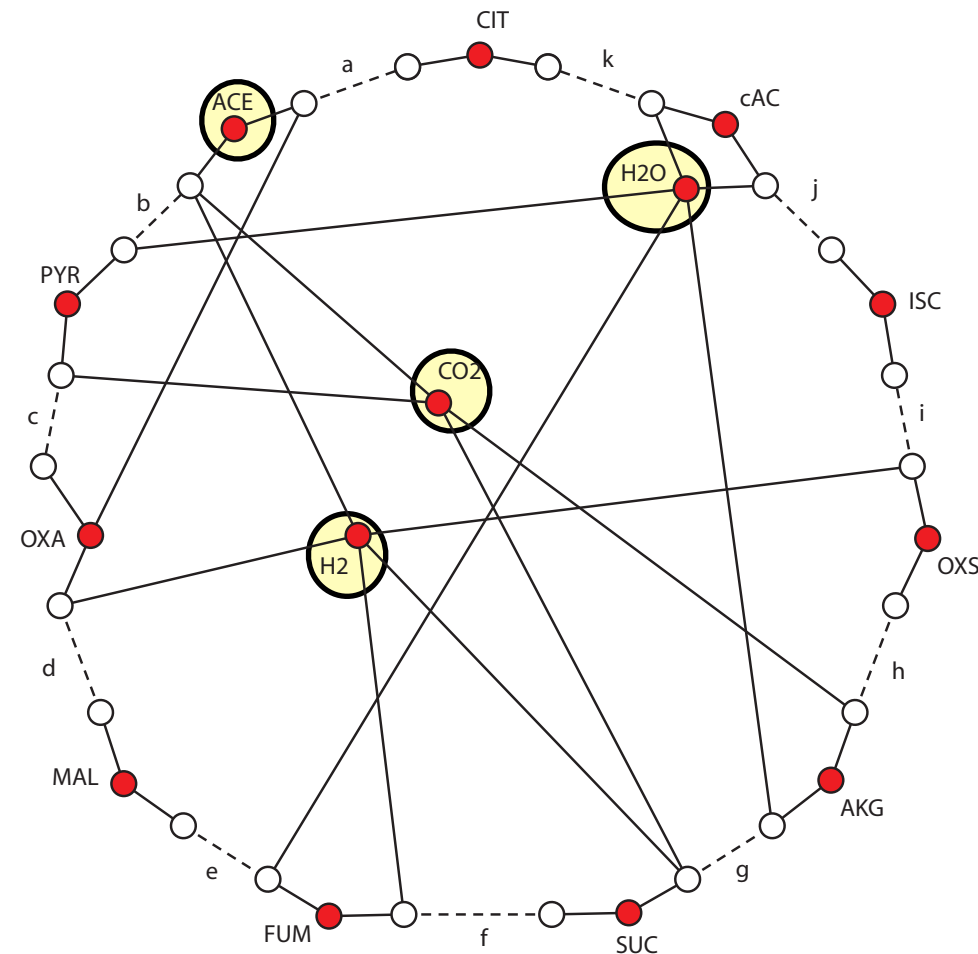
$$d[ACE] / dt = - J_b \quad \text{etc.}$$

The graph conversion provides a symbolic decomposition of all of the rTCA rate equations



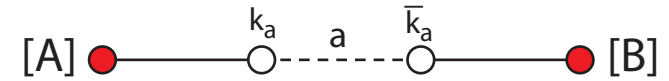
The statistical mechanics problem of network autocatalysis

- The problem of carbon reduction is specified by four molecular chemical potentials (or concentrations)
- CO_2 is the most oxidized form in the network; Acetate is the most reduced
- In Gibbs equilibrium only three (atomic species) concentrations could independently be specified, so this system is overconstrained
- Rate constants convert the excess constraint into a steady-state **current**



Graph reduction reduces the number of equations while aggregating their coefficients

Start with rate equations for a basic reaction



$$[A] k_a - [B] \bar{k}_a = J_a.$$

Two basic reactions with intermediate species
X imply a conservation law in steady state

$$[\dot{A}] = -J_a$$

$$[\dot{B}] = J_a,$$

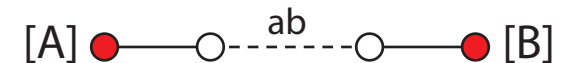
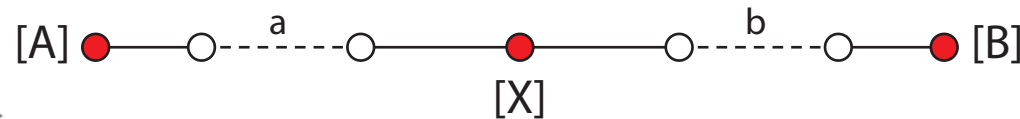
$$[A] k_a - [X] \bar{k}_a = J_a$$

$$[\dot{A}] = -J_a$$

$$[X] k_b - [B] \bar{k}_b = J_b,$$

$$[\dot{X}] = J_a - J_b$$

$$[\dot{B}] = J_b,$$



Remove species X and aggregate rate constants in an effective reaction

$$[A] k_{ab} - [B] \bar{k}_{ab} = J_{ab}$$

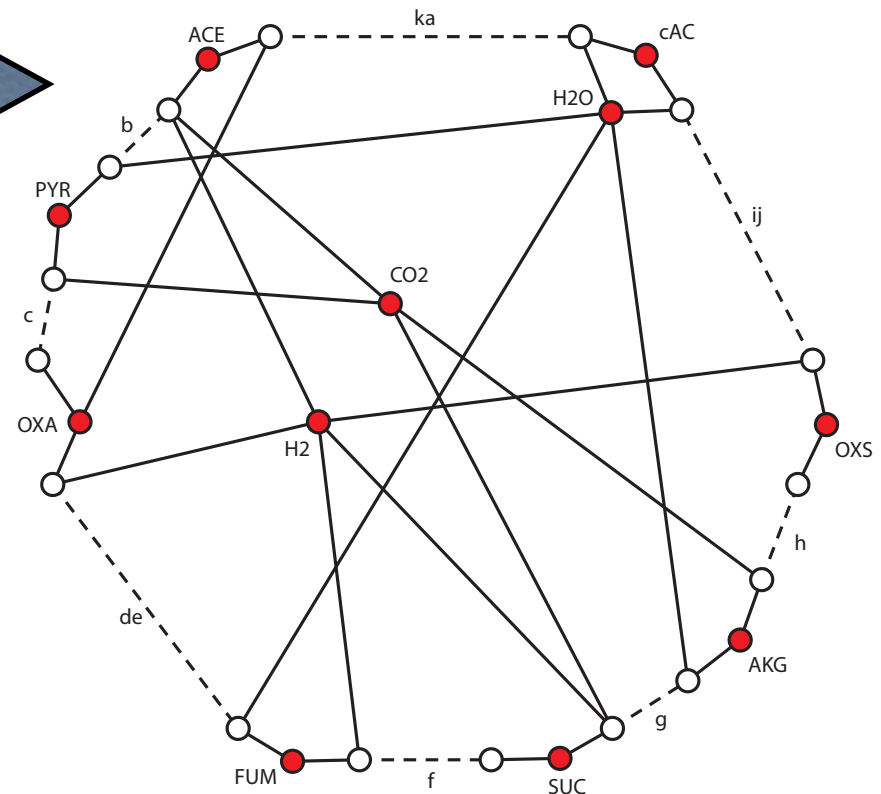
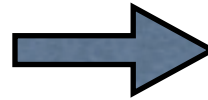
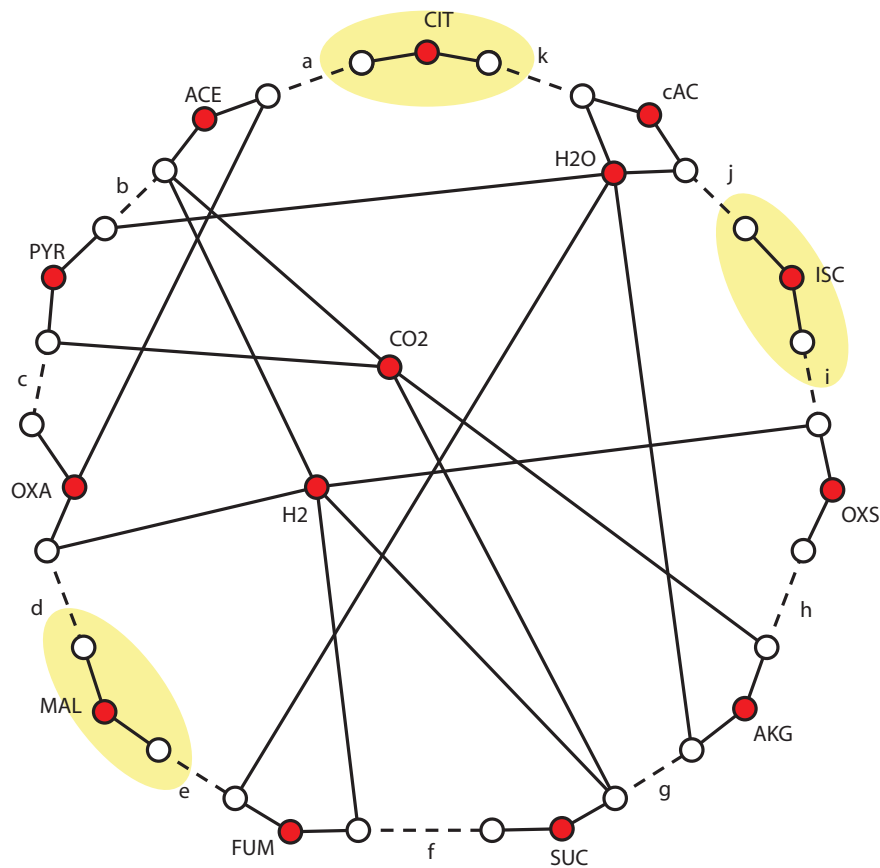
$$(k_a, \bar{k}_a) \circ (k_b, \bar{k}_b) = (k_{ab}, \bar{k}_{ab})$$

$$k_{ab} = \frac{k_a k_b}{\bar{k}_a + k_b}$$

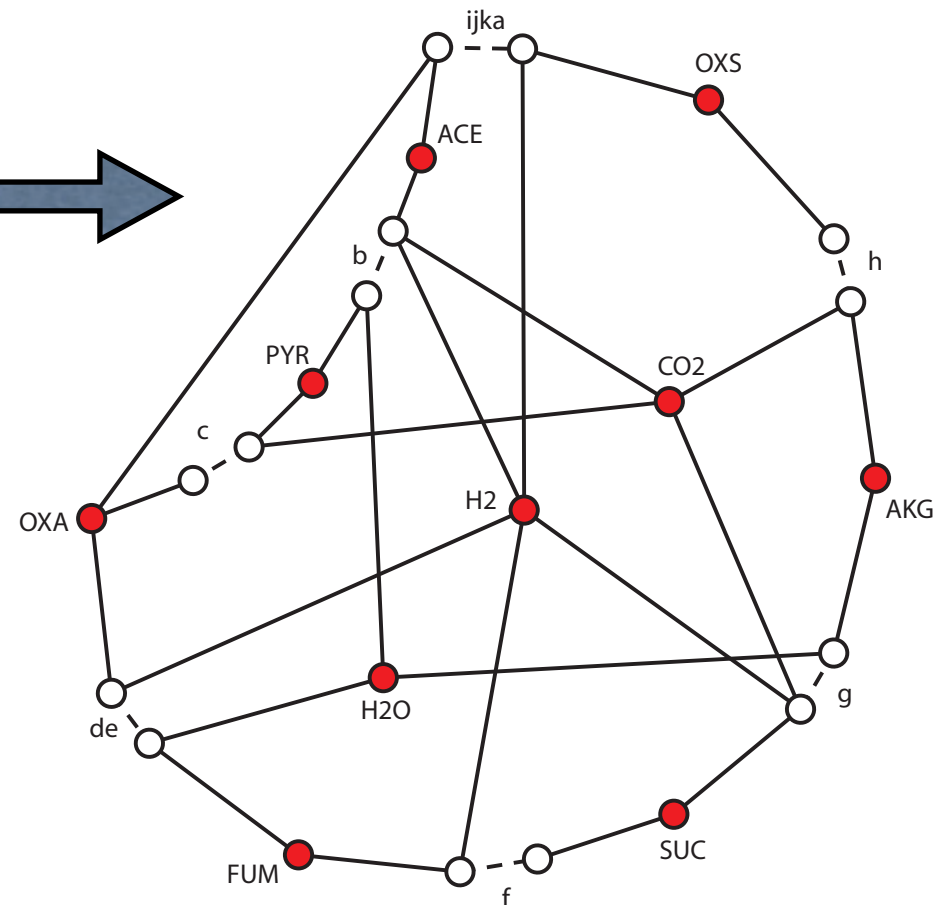
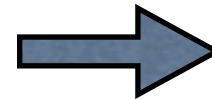
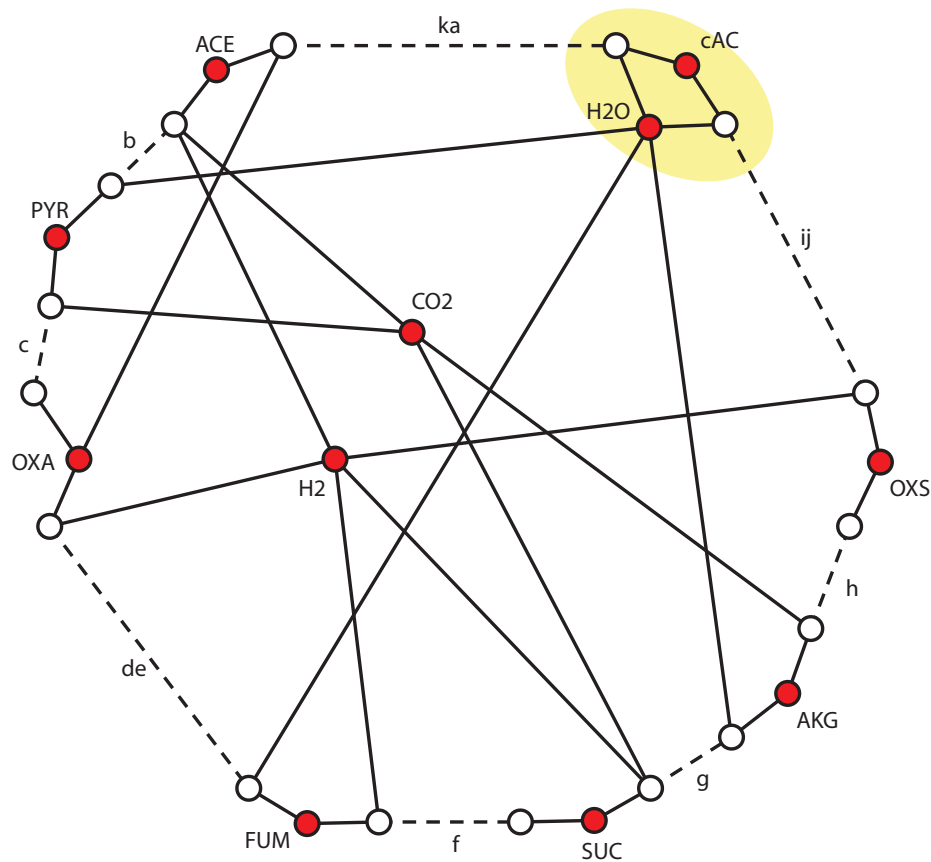
$$\bar{k}_{ab} = \frac{\bar{k}_a \bar{k}_b}{\bar{k}_a + k_b}$$

Begin the analysis of rTCA:

Remove nodes with no internal structure

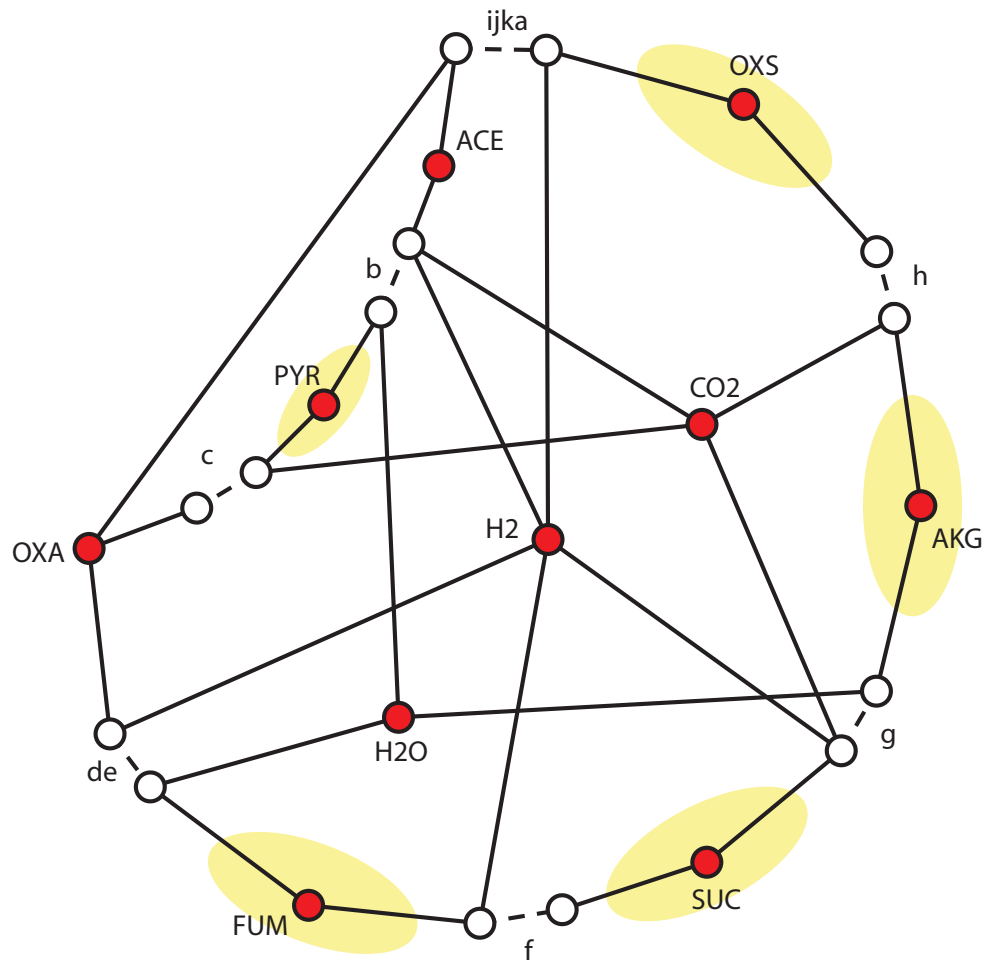


Remove an elementary isomerization

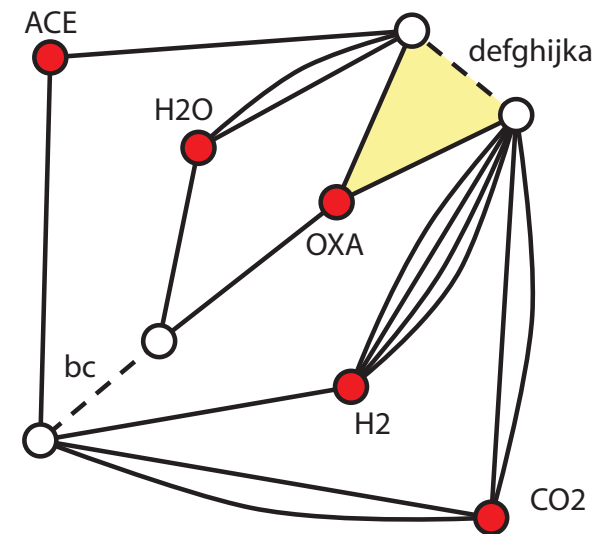
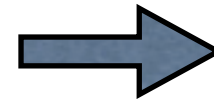


Formally, the dehydration/re-hydration of cis-Aconitate has internal structure, but it is of a trivial nature

Remove all remaining nodes, except boundary conditions and branches



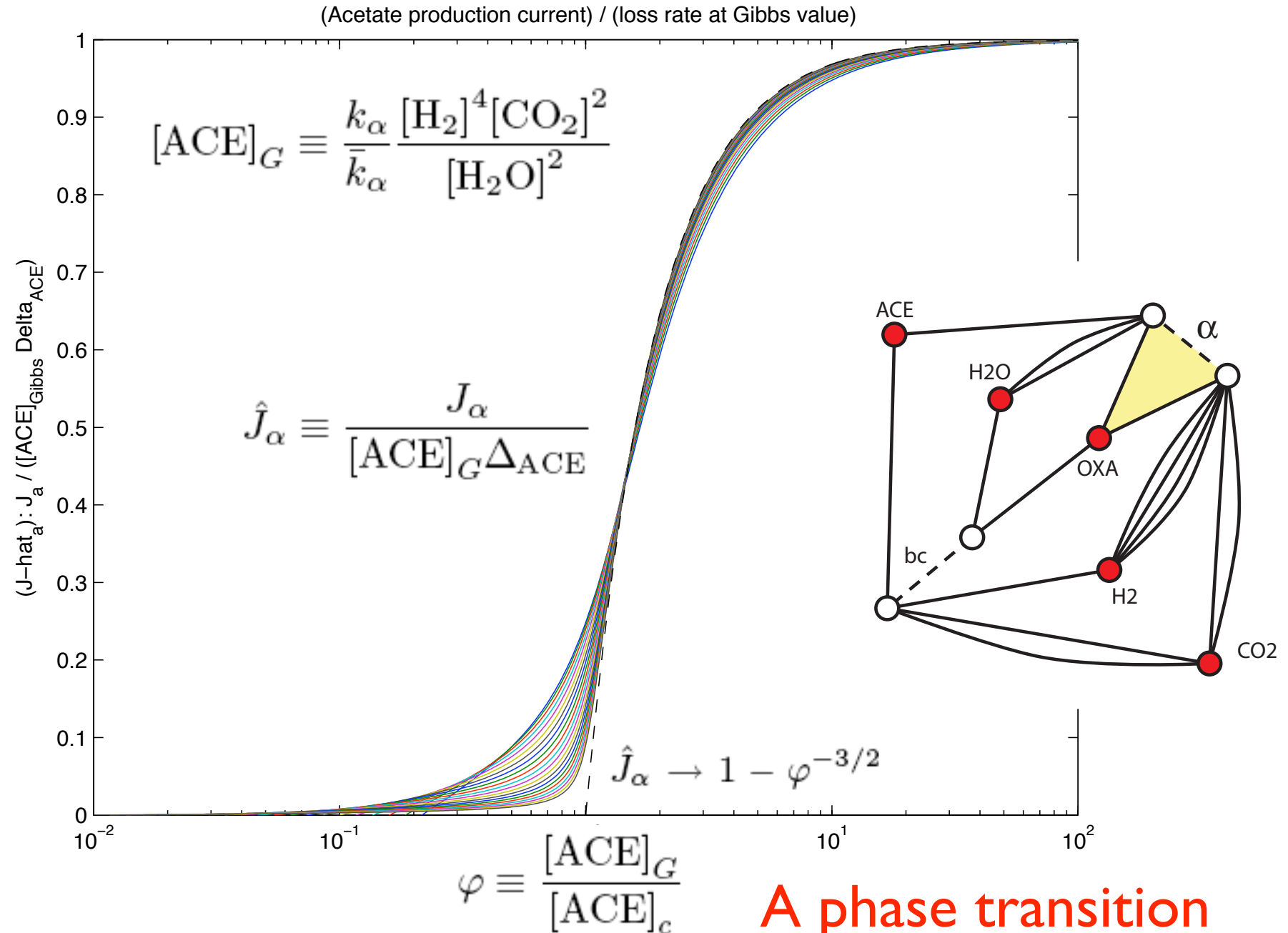
Arrive at the essential description of rTCA network autocatalysis



$$J_{bc} = [ACE] [H_2] [CO_2]^2 k_{bc} - [OXA] [H_2O] \bar{k}_{bc}$$

$$J_{defghijka} = [OXA] [H_2]^4 [CO_2]^2 k_{defghijka} - [OXA] [ACE] [H_2O]^2 \bar{k}_{defghijka}$$

The effective equations are easily solved analytically



**A phase transition
to carbon fixation !**

Summary for Day II

- We can isolate carbon fixation as a core problem on which all the rest of biochemistry depends
- Energetic, chemical, and network properties of the TCA cycle suggest a spontaneous process
- Can understand (some kinds of) self-organization as channel formation by phase transition
- A dynamical model of TCA cycling shows this kind of phase transition

Further reading

- [Smith, Eric and Morowitz, Harold J](#) **Universality in intermediary metabolism** Proc. Nat. Acad. USA **101**, 2004, 13168
- [Morowitz, Harold J](#) **Foundations of bioenergetics** New York : Academic Press, 1978
- [Morowitz, Harold J](#) **Energy flow in biology; biological organization as a problem in thermal physics** New York, Academic Press, 1968
- [Fenchel, Tom](#) **Origin and early evolution of life** New York : Oxford University Press, 2002
- [Fry, Iris](#) **The emergence of life on earth: a historical and scientific overview** New Jersey : Rutgers University Press, 2000
- [Jaynes, E. T.](#) **E.T. Jaynes : papers on probability, statistics, and statistical physics; R.D. Rosenkrantz ed.** Dordrecht, Holland : D. Reidel 1983
- [Smith, Eric](#) **Statistical mechanics of self-driven Carnot cycles** Phys. Rev. E**60**,1999, 3633; **Self-organization from structural refrigeration** Phys. Rev. E**68**,2003, 046114; **The thermodynamic dual structure of linearly dissipative driven systems** Phys. Rev. E**72**, 2005, 36130
- [Sinanoglu, Oktay and Lee, Lih-Syng](#) **Finding the possible mechanisms for a given type of overall reaction. The case of the (A+B to C+D) overall reaction types** Theoretica Chimica Acta **51**, 1979, 1; **On the algebraic construction of chemistry from quantum mechanics. A fundamental valency vector field defined on the euclidean 3-space and its relation to the Hilbert space** Theoretica Chimica Acta **65**, 1984, 249