

# Conformity, Consistency, and Cultural Heterogeneity

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## Abstract

In this paper, we construct a simple model that simultaneously produces inter cultural heterogeneity, distinct cultural signatures, and intra cultural heterogeneity. Our model assumes only that people pursue both *consistency* and *conformity*. We show that these two incentives produce distinct, diverse cultures but because they partially work at cross purposes they do not lead to fast intra cultural convergence. When we increase the relative strength of one of the forces, we exacerbate this tension. In an expanded version of the model that allows for errors, or what could be considered occasional idiosyncratic behavior, we find that small amounts of error result in substantial intra cultural differences. This result arises even though each force acting alone produces only moderate levels of intra cultural heterogeneity, thereby revealing the pitfalls of studying individual forces in isolation and extrapolating to their combined effects. Though here we apply our model to cultures, we could equally well apply some of its implications to other organized groups, including firms and political parties.

## 1 Introduction

Empirical research on cultural differences reveals three main findings. First, substantial inter-cultural differences exist (Inglehart 1997). People who belong to distinct cultures act differently: they possess different belief systems and exhibit distinct behaviors and mannerisms. Second, cultures have signature characteristics that that cannot be considered idiosyncratic collections of attributes. Individuals within a culture exhibit a behavioral consistency that allows others to anticipate and predict

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responses based on cultural affiliations. For example, French people tend to be more risk averse than Americans (Hofstede 1991) and across nations people differ in how much emphasis they place on the individual relative to the collective (Inglehart 1997). Third, this consistency notwithstanding, people within cultures differ. Not all French people are the same; nor are all members of the Itza' or the !Kung. In fact, differences across cultures are as substantial as the differences between them (Inglehart 1997).

In this paper, we construct a simple model that relies on the interplay between two empirically established forces that drive a person's behavior: a desire for *social conformity* and a desire for *individual consistency*. We first analyze a *pure conformity model* and a *pure consistency model*. We then create a *combined conformity/consistency model*. In all three of the models, we consider the individuals who interact as belonging to a culture. Our findings for the individual force models are intuitive. The model containing individuals driven only by the consistency produces consistent individuals but no intra-culture consistency; i.e. it produces a society consisting of consistent individuals each with a random collection of consistent behaviors. The model containing agents who only wish to conform to those around them produces individuals with identical, and inconsistent attributes. Whatever cultural differences exist arise from randomness (the odds of coordinating on the same attributes are low) or from different initial conditions (the attributes that are most prevalent initially tend to become the dominant cultural attributes). Thus, when we include only intra-cultural conformity within disjoint communities we can explain inter-cultural heterogeneity as distinct equilibria of the coordination dynamic, but we cannot produce intra-cultural heterogeneity. These latter findings agree with an extensive literature on conformity models, including those that allow for preferential interaction (Axelrod 1997, Rogers 1983, Hannan 1979, Barth 1969, Simmel 1955, Homans 1950).

Our combined model considers both forces in combination. It produces all three of the aforementioned empirical regularities: cultures differ, they have distinct signatures, and they exhibit heterogeneity. Thus, our model connects two well established individual level behavioral assumptions from psychology—the individual desires to exhibit consistent (reducing cognitive dissonance (Festinger 1957) and conforming behavior — with aggregate level empirical regularities long noticed by sociologists and political scientists: inter-cultural heterogeneity, intra-cultural consistency, and intra-cultural heterogeneity. In addition, to providing a candidate explanation for these regularities, our model also generates two unexpected results. First, when we vary the strength of the two forces, we find that contrary to our expectations, any imbalance between the desire to conform and to be consistent *slows* convergence. Further, that slowdown can be substantial. Second, when we introduce small errors, the model with both forces creates substantially more intra cultural heterogeneity than either of the single force models. Put differently, the combined effect of the forces far exceeds the sum of the effects of the individual forces. Thus, in addition to the substantive contributions we have highlighted, the paper highlights the danger of carving out individual effects and studying them in isolation, a standard practice in social science.

In the remainder of this section, we provide a brief overview of the literature on that underpins our main assumptions. We also summarize some of the empirical evidence on both inter- and intra-cultural heterogeneity and discuss the importance of a better understanding of the latter. The force for conformity—the idea that people become like those around them—can be unbundled into four distinct individual-level desires and incentives (i) the need to fit in with others (ii) the strategic benefit from coordination (iii) the incentive to free ride on the information of others, and (iv) the desire to interact with people similar to oneself. The first force has long been a staple of social psychology: people often mimic the behaviors, beliefs, and attributes of those with whom they interact. Social pressure can impart desire to fit in with others (Bernheim 1994, Kuran 1995). If others positively reinforce conforming behavior, then conformity can become a conditioned response (Pavlov 1903, Skinner 1974). In brief, people who interact frequently become similar. They act similarly, they dress similarly, they reveal similar preferences (Axelrod 1997), and when confronted with a new situation, they copy the behaviors of others rather than charting their own course (Simon 1982).<sup>1</sup>

Conforming behavior need not be divorced from incentives. When copying, individuals often do so selectively. They look to the behaviors of their more successful neighbors (Kennedy 1988). People who face similar problems may construct similar solutions without imitating just as students who enroll in the same class and take identical exams may produce similar answers without copying. Seminal works in psychology by Pavlov (1903) and Skinner (1974) connect positive reinforcement and the conditioning of learned responses. However, imitation only partly explains within-culture conformity. Institutions exert major influence, as they can create a common set of incentives and constraints on behavior and often encourage conformity (North 1990, Bednar and Page 2006, Young 1998). If everyone else in a community shakes hands upon greeting, drives on the left side of the road, and speaks English, an individual will benefit from doing the same.<sup>2</sup>

An additional force for conformity arises in situations where people take actions contingent on their beliefs. If people see that everyone else has taken some action, they cannot help but draw certain inferences about the beliefs of others. This tendency creates what has been called *herd behavior* (Banerjee 1992) and *information cascades* (Bikhchandani, et al 1993), or what is more colloquially referred to as “jumping on the bandwagon”.

In addition to people choosing to act like those around them, people also choose to

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<sup>1</sup>Banduras’ (1977) bobo doll experiments demonstrated that children imitate behavior they view on TV. More recently, Huesmann (1988, 1998) has shown that in the short term children copy behavior that they observe, which in the long run becomes encoded into their behavioral schemas.

<sup>2</sup>Coordination problems can be modeled as two-by-two games in which the players attempt to choose the same action. We can distinguish between conformity and coordination in terms of the measurability of the benefit. People coordinate on the side of the road they drive their cars. This decision has measurable costs and benefits. Alternatively, people can conform by wearing a certain type of pants. In this case, the benefits that come from wearing a particular style of pants, while more difficult to measure economically, are nevertheless real.

be around those who act similarly. Sociologists refer to this as *homophily*.<sup>3</sup> Homophily creates conformity within interacting groups and implies differences between those groups. If these differences did not exist, the two groups may as well merge and form a larger group.<sup>4</sup> In our model, we take the interacting groups as fixed and rule out the possibility of subcultures of this sort, acknowledging that the possibility of subcultures would create further intra-cultural heterogeneity.

The second fundamental force that motivates individual behavior is the desire to be consistent: to act according to a common set of principles and guidelines in different situations. This force can be explained using either of two lines of argument: one cognitive and one based on cost-benefit analysis. Psychological research shows that personal uneasiness with cognitive dissonance creates within individuals a desire for consistency. People find acting differently in every situation difficult (Festinger 1957). Psychologists generally agree that individuals can overcome cognitive dissonance by either restricting their behavior to be consistent with their attitudes or by changing their attitudes to match their inconsistent behavior.<sup>5</sup> The cognitive argument rests on current understandings of the physiology of the brain. Research shows that repeated behaviors create cognitive pathways (Gazzaniga 1999). For this reason, when confronted with a new situation, individuals often choose a behavioral response that belongs to their existing repertoire, especially if that response has been reinforced in the past (March 1991, Cavalli-Sforza and Feldman 1981).

The cost-benefit logic relies on informational advantages: an individual's consistency in behavior allows others to predict his/her next moves. Accurate predictions like this grease the wheels of economic and political institutions. In fact, one broadly-accepted role of culture is to help coordinate on equilibria. Some equilibria may be more focal than others based on their relationship to the wider culture (Calvert and Johnson 1997).<sup>6</sup>

To summarize, empirical evidence shows that individuals exhibit tendencies toward both consistency and conformity, each up to a point. The evidence also shows that circumstance plays a decisive role in when individuals adopt which strategy. People exhibit greater consistency in situations that are common, patterned, or part of a social role; in situations where individuals confront more radically new situations they become increasingly likely to turn to others for behavior clues (Tittle and Hill, 1967, as appears in Liska 1975). At the same time, the normative environment within which people make behavioral decisions also matters: in general, the more observable one's behavior is to others, the more likely one is to conform to the majority behavior

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<sup>3</sup>McPherson, M., L. Smith-Lovin and J. Cook. (2001) review the scores of empirical studies. See also Schelling's (1971) discussion of preferences and racial segregation.

<sup>4</sup>Sorting creates no end of empirical problems related to disentangling sorting effects from conforming effects (Brock and Durlauf 2006).

<sup>5</sup>The latter seems to have stronger empirical support. People tend to adopt attitudes to make their behavior seem consistent.

<sup>6</sup>We do not mean to imply that all strategic environments include incentives to coordinate in some way. Certainly, constant sum games do exist. But growth and progress hinge on positive interactions. To be successful, cultures must exploit those interactions.

and/or the standing social norm (Liska 1975, Ajzen and Fishbein 1969, DeFleur and Warner 1969, Bowers 1968).

We now turn briefly to the empirical regularities. Careful academic studies as well as a person's own casual observations reveal substantial differences between cultures. No one disputes that different patterns of behavior exist between the German and French cultures as well between the cultures of the Inuit and the Dutch. In fact, this inter-cultural variation provides a foundation for nearly all social scientific comparative studies. The nature of area studies research implies the assumed existence of recognizable and significant differences between behaviors of peoples in different geographical regions, be they informal societies, communities, cities, or countries. Inglehart, in summarizing The World Values Survey data, concludes that "cultural variation is . . . relatively constant within a given society, but shows relatively great variation between different societies" (Inglehart 1997, p. 166). In other words, Danish attitudes about well-being can be consistently distinguished from French, Italian, or Portuguese attitudes. He bases this conclusion on evidence gathered over many years.<sup>7</sup> These survey findings are supported by more recent experimental findings. Henrich et al (2001) conducted an extensive comparative study of fifteen small-scale societies across five cultures. They also found substantive evidence of inter-cultural variation in behavior. In another study Henrich (2000) finds that the economic behavior of Peruvian communities varies widely from the behavior of a Los Angeles control group, which suggests that "economic reasoning may be heavily influenced by cultural differences—that is, by socially transmitted rules about how to behave in certain circumstances (economic or otherwise) that may vary from group to group as a consequence of different cultural evolutionary trajectories" (Henrich 2000, p. 973).

The existence of inter-cultural differences does not imply people within cultures are the same. To the contrary, analyses of data from cross-cultural studies reveal substantial intra-cultural heterogeneity to be substantial (Au 1999, Pelto and Pelto 1975, Thompson 1975, Graves 1970). Au's (1999) Intra-Cultural Variation (ICV) measure considers six variables from The World Values Survey (three related to work - pride in work, job satisfaction, and freedom in decision making - and three related to change - change is good, a new idea is good, and new ideas are welcome). He then compares the standard deviations for each country on these variables. He finds that some countries that share similar cultural means exhibit substantial differences in ICV. He also uncovers some surprises: Contrary to popular lore, American culture is far more homogenous than Japanese culture. Hofstede (1991) offers possible reasons for this observed ICV as differences in colonial inheritance, language, ethnicity, and sub-regional customs. Pelto and Pelto (1975) refer to Harris (1970) when they summarize the ICV logic nicely: "the degree to which behavior is rule-bound varies a good deal from one situation to another" (Pelto and Pelto 1975, p. 10). We can

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<sup>7</sup>On most variables he finds significant variation between country means. On cross cultural differences in life satisfaction over 64 countries, for example, the United States life satisfaction mean is 7.7, based on a ten-point scale; across all 64 societies the means range from as low as 3.7 to as high as 8.2.

think of behavioral regularities within a population as part of a culture. In a given context, in a given society, behavior – such as accepting change – can vary widely. Hence, when presented with a survey question about their behavior, people within a culture respond differently.

To allow for this potential heterogeneity within cultures, our model relies on agents who possess vectors of *attributes*. We use the term attributes as a catchall: attributes might include behavior, dispositions for behavior, customs, attire and so on. Attributes, however, should not be confused with immutable characteristics; by assumption the attributes we consider are plastic. These attributes also have explicit meaning so that they can be consistent. Thus, our model extends Axelrod’s (1997) model of cultural formation in which attribute values are not compared across dimensions.

In our formal analysis, we first consider the time it takes for a population to converge to an equilibrium. We do this for all three models: the *pure conformity model*, the *pure consistency model*, and the *combined conformity /consistency model*. In the combined model, we vary the weight of the two forces. A priori, we have no reason to believe that conformity and consistency matter equally. If anything, our reading of the literature suggests that the weight on conformity may be larger, at least in the cultural context. Applications of our model to other contexts may require adjusting the relative weights on the two forces. We then derive the time to convergence mathematically for a simple model and also perform computational experiments. Both approaches show that the time to convergence to equilibrium increases dramatically in the combined model. This increase in time to convergence can result in sustained intra-cultural heterogeneity even if an equilibrium exists. One might argue that if an equilibrium exists, then the system would eventually reach it, but this argument rests on faulty logic. When the number of interactions required to attain an equilibrium is sufficiently large, we would expect that in real cultures other factors would intervene before the equilibrium could be attained. Furthermore, missteps along the path can result in substantial and perpetual deviations from the equilibrium.

To test for the effect of such mistakes, we emend our model and include a small probability that agents randomly change an attribute’s value. Given errors, the population of agents does not converge to full conformity and consistency, but instead to an equilibrium distribution over attribute values. Using Markov theory, we compare these limiting distributions in the single force models and the double force model. We find that errors in the two single force models create limiting distributions that lie close to the error-free equilibria but that the combined model produces an equilibrium which is much more disperse (see Table 2). Our analysis reveals that the interplay between the two forces creates an effect at least as large as each of the two forces on its own. In effect, one plus one equals three.

The rest of the paper is organized as follows. In Part 2 we introduce our models of conformity and consistency. In Part 3 we analyze the results by considering (1) the time to convergence, and (2) the equilibrium distribution in models with errors. In

Part 4 we use numerical experiments to test our analytic results. In Part 5 we summarize our findings and consider alternative explanations for the empirical observation of intra-cultural heterogeneity. We close the paper with a discussion of potential applications of the theory to understand heterogeneity in organizations, including firms and political parties.

## 2 Models of Conformity and Consistency

Our model consists of  $N$  agents, each of which has a vector of  $M$  attributes. Each attribute takes one of  $A$  values. Given this setup, we can characterize an agent as a vector  $(a_1, a_2, \dots, a_M)$ , where each  $a_i \in \{0, 1, \dots, A\}$ . We assume that all agents interact with each other with equal likelihood, what is called *random mixing*. Including network-structured interactions would complicate the analysis without providing any obvious benefit; an investigation into network effects is therefore left for future consideration.

### Modeling Agent Behavior

We assume that the agents follow *behavioral rules* that can be interpreted either as descriptions of what people do or as learning algorithms in a model in which agents attempt to maximize their payoffs.<sup>8</sup> We rely on simple characterizations of the two forces as embedded in these behavioral rules. The desire to conform leads agents to match their value on attributes with that of another agent. Examples of conforming behavior rules are: *If my neighbor shares, then I will share* and *My neighbor wears a hat, so I will wear a hat*. The desire to be consistent leads agents to match their values on one attribute to their value on another attribute. Examples of consistency-enhancing behavior are: *I punish deviators in this context, I will do so in this other context as well* or *I keep a clean office, so I will keep a clean house*. In the combined model, agents try to conform *and* they try to be consistent.

### Payoff Functions

Though not explicitly based on payoff functions, our behavioral rules converge to payoff maximizing configurations given natural characterizations of payoff functions. The desire for consistency can be captured in payoff form as an incentive to have as

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<sup>8</sup>A learning model begins from a payoff function and assumes that agents' responses depend on payoffs and expectations of payoffs. Ultimately, a learning model becomes a behavioral rule. However, the game form and the assumption of payoff maximization as a goal constrain the set of possible behavioral rules. Of course, rule-based models need not be consistent with any reasonable assumptions about the underlying game form and the learning rule. This critique may not be as damning as it sounds. Nothing constrains human behavior to be consistent with an underlying game form and a learning rule. People do use simple behavioral rules that are inconsistent with the rational underpinnings associated with formal game theoretic models.

many attributes as possible take on the same value. Formally, let  $s(a^j)$  equal the number of times the most common attribute appears in agent  $j$ 's vector of attributes. We can write

$$s(a^j) = \max_a \max_{i \in A} \{ |i| : a_i^j = a \}$$

This function offers a crude measure of consistency. We can think of it as a *consistency payoff function*. Given this payoff function, an optimizing agent would set all attributes to the same value. But, if the agent is not cognizant of all of its attributes' values that agent might randomly align its attribute values; we assume this behavioral rule. Such an assumption makes sense if we imagine attributes becoming activated and agents recognizing internal inconsistencies. Note that this behavioral rule results in a consistent set of attributes if applied for a sufficient number of periods.

In the single force models, our behavioral rules are consistent with behavior that optimizes a payoff function. In the conformity model, we define the payoff to agent  $j$  as  $f(a^j, a^{-j})$ , the percentage of other agents whose attributes match those of agent  $j$  averaged across all attributes.

$$f(a^j, a^{-j}) = \frac{\sum_{k \neq j} \sum_{i=1}^M \delta(a_i^j, a_i^k)}{NM}$$

where  $\delta(a_i^j, a_i^k) = 1$  if and only if  $a_i^j = a_i^k$ . We can call this the *conformity payoff function*. If agents cared only about conformity, then they would choose to acquire the most common value for each attribute. That sort of coordination is not easy to accomplish. A reasonable behavioral rule would be for an agent to switch one of its attribute values to match that of some other agent. This rule converges to full conformity if the agents update asynchronously (Page 1997).

For the combined model, we can write the payoff function to agent  $j$ ,  $\pi_j$  as a convex combination of these two functions.

$$\pi_j(a^j, a^{-j}) = \alpha s(a^j) + (1 - \alpha) f(a^j, a^{-j})$$

where  $\alpha \in [0, 1]$  denotes the relative weight on consistency.

In this combined model, the optimal solution would be for the agents to all choose the same values for each attribute. Consistent conformity at the societal level is far easier said than done. A natural question to ask is whether a given behavioral rule locates consistent conformity as an equilibrium. The rule we choose – a probabilistic combination of the consistency rule and the conformity rule – does. A myopic best response adjustment process in which an agent only switches an attribute's value if it leads to a higher payoff need not. That rule produces inefficient local optima. For example, an agent might be in a position such that it cannot become more consistent without reducing its payoff from conformity (Kuran and Sandholm 2003). Thus, our behavioral rule may make supporting heterogeneity more difficult than were agents to be optimizing.



## The Consistency Model

We now describe our models, beginning with the consistency model. In this model, the agents' only behavior is to adopt consistent values on attributes. In each period, we randomly select an agent. This agent then applies an *internal consistency rule*.

**Internal Consistency Rule:** *The agent randomly chooses two random distinct attributes and changes the value of the first attribute to match the value of the second.*

This rule produces an unbiased random walk where the probability of moving depends upon the state. To start we restrict attention to the case of binary attribute values. The extension to non binary attributes is notationally burdensome but straightforward. Let  $x$  denote the number of an agent's attributes with value one, so that  $M - x$  attributes have value zero. The variable  $x$  can take on any value in the set  $\{0, 1, 2, \dots, M\}$ . If  $x = 0$  or  $x = M$ , we say that the agent is *consistent*. For the moment, we assume no noise. We can think of an agent whose attributes all take the same value either as in an *equilibrium* or as in an *absorbing state*; we use these two terms interchangeably throughout this paper.

Consider the special case where  $x = 1$ . When we apply the internal consistency rule, the variable  $x$  could 1) fall to zero, 2) it could remain at one, or 3) it could increase to two. For  $x$  to fall to zero, the first attribute chosen must be the only attribute with value one. The probability of choosing this attribute equals  $\frac{1}{M}$ . The second attribute chosen necessarily has value zero (since " $x = 1$ "). The probability of choosing the one and a zero therefore equals  $\frac{1}{M}$ . The variable  $x$  remains at one if and only if both attributes chosen have value zero. The probability of the first attribute having value zero equals  $\frac{M-1}{M}$ . The probability that the second attribute has value zero equals  $\frac{M-2}{M-1}$ . Thus, the probability of both events occurring equals  $\frac{M-2}{M}$ . Finally,  $x$  increases to two only if the first attribute selected has value zero and the second attribute selected has value one. The probabilities of these two events equal  $\frac{M-1}{M}$  and  $\frac{1}{M-1}$  respectively. So the probability of both events occurring equals  $\frac{1}{M}$ . Therefore, the probability of  $x$  increasing equals the probability that it decreases when  $x = 1$ . We can now state the following claim, whose proof relies on an extension of this logic.

**Claim 1** *The internal consistency rule applied to  $M$  attributes that take on binary values produces an unbiased random walk in which the probability of movement slows near the two absorbing states. Let  $x \in \{1, 2, \dots, M-1\}$ , denote the number of attributes whose values equal one. The probability that  $x$  increases or decreases by one equals.*

$$\frac{(M-x)x}{M(M-1)}$$

pf. For  $x$  to increase, the first attribute must be one of the  $x$  attributes with value 0. This occurs with probability  $\frac{x}{M}$  and the second attribute must belong to one of the

$M - x$  attributes with value 1. This occurs with probability  $\frac{M-x}{M-1}$ . The proof for the case in which  $x$  decreases follows the same logic.

This claim implies that the internal consistency rule produces a random walk with two absorbing states. Moreover, the probability of movement decreases as the state approaches an absorbing state.

## The Conformity Model

We next consider a model in which agents want to conform. In each period, we randomly choose a pair of agents. The first agent chosen applies the *external conformity rule*.

**External Conformity Rule:** *The first paired agent randomly chooses an attribute and sets the value of that attribute equal to the value that the other agent assigns to that attribute.*

The external conformity rule also creates a random walk. The next claim applies to a single attribute version ( $M = 1$ ) of the model. The extension to the more general case is trivial.

**Claim 2** *If  $M = 1$  and if  $Y$  of the  $N$  agents assign value 0 to the lone attribute, then the probability that  $Y$  decreases after applying the external conformity rule equals  $\frac{(N-Y)Y}{N(N-1)}$  which also equals the probability that  $Y$  increases.*

The proof of this claim follows from the fact that this process is equivalent to the one described in the consistency model. This suggests a deeper symmetry that can be made formal.

**Observation:** *The internal consistency model applied to  $N$  agents with  $M$  attributes is equivalent to the external conformity model applied to  $M$  agents with a  $N$  attributes.*

It follows that in the Conformity Model, the time it takes for the process to converge increases with the number of agents in the population just as in the Consistency model the time it takes for the process to converge increases with the number of attributes.

## The Consistent Conformity Model

In the Consistent Conformity Model, agents apply both updating rules. We create a single parameter family of rules  $CC(p)$  where  $p$  denotes the probability that the agent applies the internal consistency rule. Note that the consistency and conformity models are just special cases of this model, where  $CC(1)$  is the consistency model and  $CC(0)$  is the conformity model.

**Consistent Conformity Rule CC(p):** *An agent is chosen at random and with probability  $p$  the internal consistency rule is chosen and with probability  $(1 - p)$  the external conformity rule is chosen.*

Describing the dynamics of  $CC(p)$  models are far more complicated. The only equilibria (absorbing states) of this model require that every agent assign the same value to every attribute. Let  $S_i$  equal the number of agents who assign value 0 to attribute  $i$ . The next claim describes the dynamics in the  $CC(p)$  models for  $p \in [0, 1]$  from the perspective of an agent with  $x$  attributes equaling one. Without loss of generality, we assume that these are the first  $x$  attributes.

**Claim 3** *Consider a population of  $N$  agents with  $M$  binary attributes, and an agent whose first  $x$  attributes take value one. Let  $S_i$  equal the number of other agents in the population who have value one on attribute  $i$ , the probability that  $x$  increases by one equals*

$$p \frac{x(M-x)}{M(M-1)} + (1-p) \frac{1}{M} \sum_{i=x+1}^M \frac{S_i}{N-1}$$

*and the probability that  $x$  decreases by one equals*

$$p \frac{x(M-x)}{M(M-1)} + (1-p) \frac{1}{M} \sum_{i=1}^x \frac{N-1-S_i}{N-1}$$

The proof follows directly from Claims 1 and 2.

## A Simple Example

Before presenting our analytic results, we construct an example that demonstrates the tension between consistency and conformity. Suppose that two members of a society interact in three distinct contexts. In each context, a person can take a *fair* action,  $F$ , that equally splits resources or take a *utilitarian* action,  $U$  that produces a higher total payoff. These actions play the role of the values in our more general model.

Given these assumptions, we can describe an agent by a vector of length three consisting of  $F$ 's and  $U$ 's. Let's call these people George and Laura. Suppose that they start from the following initial behavioral vectors.

George  $(F, F, U)$   
 Laura  $(F, U, U)$

Assume first that George and Laura apply the internal consistency rule. Under this assumption, George may switch his third attribute so that his vector of attributes

becomes  $(F, F, F)$ . Laura, in contrast, may switch her first attribute so that her vector becomes  $(U, U, U)$ . George and Laura both achieve internal consistency and do so quickly.<sup>9</sup>

Next suppose that George and Laura apply the external conformity rule. If we pick George first, and further pick his second attribute, then George switches his second attribute to  $U$  so that his vector becomes  $(F, U, U)$ . The two quickly conform.

Finally, assume that George and Laura desire both consistency and conformity. George may first switch to  $(F, F, F)$ . He may then meet Laura and switch to  $(F, U, F)$ . However, he may then realize that he is being inconsistent and switch back to  $(F, F, F)$ . Laura meanwhile may switch to  $(U, U, U)$  and then, hoping to conform, switch back to  $(F, U, U)$ . Eventually, both George and Laura will be consistent and conform with one another but it can take much longer. The desires to conform and to be consistent can pull in different directions thereby increasing the time required to attain an equilibrium.

### 3 Analytic Results

Our analytic results consider two questions. The time to convergence and the equilibrium distribution in models with errors. In computer science and physics the standard question to consider is the rate at which the time to convergence changes as you increase the number of states or variables. In our case, the analog would be the number of attributes in the consistency model and the number of agents in the conformity model. Using techniques developed by Bouchaud et al (1999), it can be shown that the time to convergence is of order  $M^2$ .<sup>10</sup>

**Claim 4** *The expected time to convergence for the consistency model with binary values and  $M$  attributes for a random starting point is of order  $M^2$  periods.*

pf: see appendix.

We can state a similar result for the conformity model.

**Corollary 1** *The expected time to convergence for the conformity model with binary values and  $N$  agents converges for a random starting point is of order  $N^2$  periods.*

pf: follows from our earlier observation of equivalence and the previous claim.

In a conformity model with more than one attribute, we can think of each attribute converging independently of the others. There are no interactions between the attributes. Therefore, the time it takes for conformity should increase linearly in the number of attributes.

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<sup>9</sup>Note that George could also change to  $(F, U, U)$  or  $(U, F, U)$  given the internal consistency rule, but at some point, he would have all three of his attributes taking the same value.

<sup>10</sup>We thank Len Sander for this proof.

The time to convergence for the Consistent Conformity Model can be shown to increase in order  $N^2M^2$  for  $p = 1/2$  (Sander, Schneider-Mizell, and Page 2006) One reason that we should expect the Consistent Conformity Model to take substantially longer to converge is that it has far fewer equilibria given the behavioral rules we assume. We capture this fact in the next three claims.

**Claim 5** *The number of equilibria in the Consistency Model equals  $A^M$ , where  $A$  equals the number of values per attribute and  $M$  is the number of agents.*

**Claim 6** *The number of equilibria in the Conformity Model equals  $A^N$ , where  $A$  equals the number of values per attribute and  $N$  is the number of attributes.*

**Claim 7** *The number of equilibria in the Consistent Conformity Model equals  $A$ , the number of values per attribute.*

## The Two Agent Two Attribute Model

In our analytic model, we consider the simplest interesting case: two agents, two attributes, and two values per attribute ( $A=2$ ,  $N=2$ ,  $M=2$ ). This model proves sufficient to show our two main results: that the Consistent Conformity model takes longer to converge than either of the other two models and that its equilibrium in the model with errors has greater dispersion.

### Time to Convergence

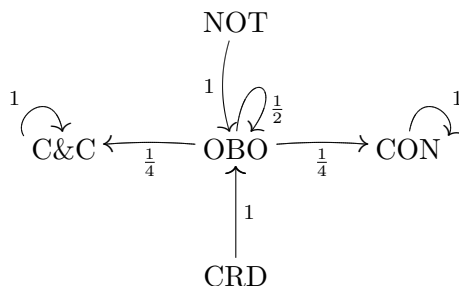
We first analyze time to convergence in the three models by calculating the time required for each of the three processes to converge. Given our assumptions, the two agents in this model can together be in any one of sixteen states which can be sorted into five categories. These categories correspond to the two agents being in conformity and internally consistent (C&C), consistent but not conforming (CON), conforming but not consistent (CRD), one agent consistent but the other not – what we call off by one (OBO), or both inconsistent and lacking conformity (NOT). Using the letters  $a$  and  $b$  to denote distinct attribute values, we can define each category and its probabilities as in Table 1:

For the internal consistency rule, the probability that  $x = 0$  equals the probability that  $x = 2$  which is  $\frac{1}{4}$ . The other half of the time  $x = 1$ . If  $x = 1$ , then in the first period the two attributes are selected and one matches the other and as a result, the agent becomes consistent. By the symmetry argument the expected time to equilibrium in the Consistency Model must equal the expected time to equilibrium in the conformity model. Nevertheless, making the calculation in both models is instructive.

Table 1: States of the System

<i>State</i>	<i>Agents</i>	<i>Prob</i>
Conformed & Consistent (C&C)	(a,a) (a,a)	$\frac{1}{8}$
Consistent Not Conformed (CON)	(a,a) (b,b)	$\frac{1}{8}$
Conformed Not Consistent (CRD)	(a,b) (a,b)	$\frac{1}{8}$
Off By One (OBO)	(a,b) (a,a)	$\frac{1}{2}$
Not Conformed Not Consistent (NOT)	(a,b) (b,a)	$\frac{1}{8}$

Figure 1: The Dynamics of the Internal Consistency Rule



### Consistency Model

We first calculate expected time to equilibrium in the Consistency Model. In this model, any configurations in the sets  $C\&C$  and  $CON$  are equilibria. We must first calculate the probability that any one of the other states moves to those states. If the initial state is in  $OBO$ , then the probability of staying in  $OBO$  equals one half, and the probability of moving to  $C\&C$  or to  $CON$  equals one fourth. If the initial state is  $NOT$  or  $CRD$ , then it moves into  $OBO$  with probability one. We can write this information diagrammatically as shown in Figure 1:

We can use the information in this diagram to calculate the expected time to convergence.

**Claim 8** *The expected time to equilibrium for the Internal Consistency Rule equals*

$1\frac{3}{4}$  interactions. <sup>11</sup>

pf: Let  $T_S$  denote the time (or expected time) to get to equilibrium from a given state. First, note that  $T_{CON} = T_{C\&C} = 0$ , since  $C\&C$  and  $CON$  are absorbing states. Second note that the time to reach an absorbing state from a state in  $CRD$  or  $NOT$  equals one plus the time it takes to reach an absorbing state from  $OBO$ .

$$T_{CRD} = T_{NOT} = 1 + T_{OBO}$$

We calculate the expected time to reach an absorbing state from  $OBO$  as follows. With probability one half, it takes only one time period. The other half of the time, the process remains in  $OBO$ , which means the time to an absorbing state equals one plus the time to an absorbing state. We can write this as follows:

$$T_{OBO} = \frac{1}{2}(1) + \frac{1}{2}(1 + T_{OBO}) = 1 + \frac{1}{2}T_{OBO}$$

Solving for  $T_{OBO}$  yields that  $T_{OBO} = 2$ . Therefore  $T_{CRD} = T_{NOT} = 3$ , so applying the internal consistency rule, the expected time to attain an absorbing state,  $T^{ICR}$ , equals  $T^{ICR} = \frac{1}{8}(0) + \frac{1}{8}(0) + \frac{1}{8}(3) + \frac{1}{8}(3) + \frac{1}{2}(2) = 1\frac{3}{4}$

### Conformity Model

We can construct a similar diagram for the dynamics created by the external conformity rule (see Figure 2). Notice that this diagram is the same as the one above, with the only difference being that the states  $CRD$  and  $CON$  have changed places. Therefore, by symmetry the expected time to an absorbing state in this model is also  $1\frac{3}{4}$  interactions.

**Claim 9** *The expected time to equilibrium for the External Conformity Rule equals  $1\frac{3}{4}$  interactions.*

pf: follows from above.

### CC(p) Model

Next, we consider the  $CC(p)$  model. In the diagram below, we show the case where  $p = \frac{1}{2}$ . The diagram for this model, Figure 3 combines the diagrams for the previous two models so that the only absorbing state is  $C\&C$ .

Using Figure 3, we can state the following claim.

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<sup>11</sup>time is measured by the number of interactions (an interaction is one application of a rule) with each interaction taking one time step. Hence time is really a measure of the iterations of the model irrespective of the computational complexity of the iteration.

Figure 2: The Dynamics of the External Conformity Rule

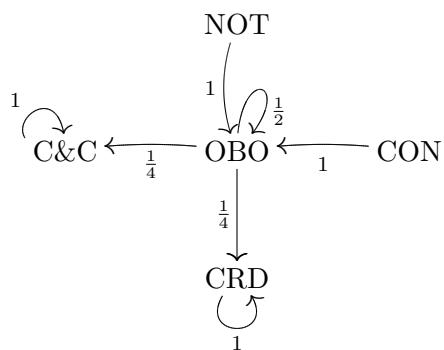


Figure 3: The Dynamics  $CC(\frac{1}{2})$

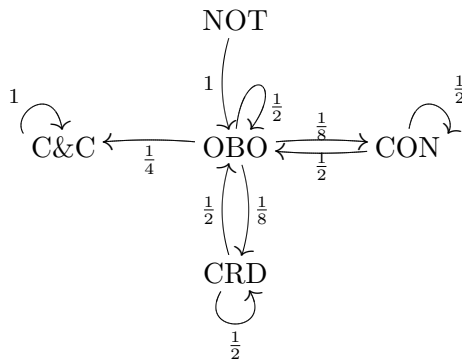
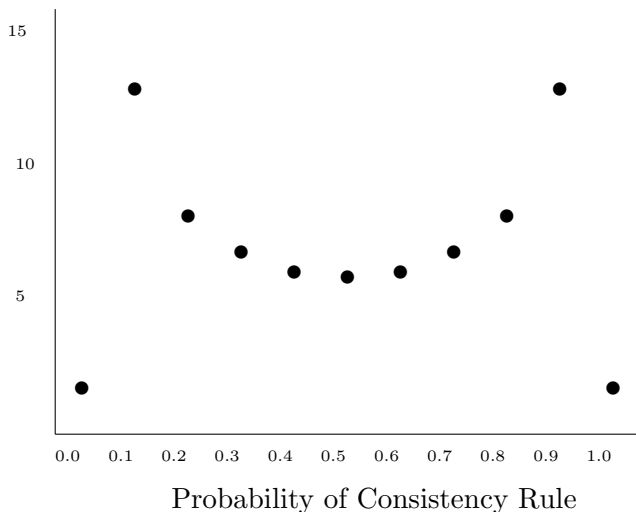




Figure 4: Expected Time To Equilibrium: Two Person Model



**Claim 10** *The expected time to equilibrium for the  $CC(p)$  Rule equals  $1\frac{7}{8} + \frac{1}{p(1-p)}$*

pf: see appendix.

We can compare the expected time to equilibrium in the three models graphically. Figure 4 shows the expected time to equilibrium as a function of the probability of applying the consistency rule. Note first that the expected time to equilibrium is far shorter in the conformity model and the consistency model than in the  $CC(p)$  model. Note also that the expected time to equilibrium is *minimized* in the  $CC(p)$  model at  $p = \frac{1}{2}$ . For comparison, the time to convergence at  $p = \frac{1}{2}$  is  $5\frac{7}{8}$  interactions; this value is more than three times the time to convergence in the other two cases.

The three flow diagrams reveal the two reasons why the consistent conformity model takes so much longer to converge than either the conformity model or the consistency model. First, as we already proved, the consistent conformity model has fewer absorbing states. Whereas Figures 1 and 2 both have two categories of absorbing states, Figure 3 has a single category of absorbing states. Second, the two individual processes both head directly to the two absorbing states. The only possible delay occurs if the system remains in state  $OBO$ . The consistent conformity model can move away from the lone absorbing state. It is possible for the process to go from  $CRD$  to  $OBO$  to  $CON$  and back to  $OBO$ . This can cause the system to take longer to converge. In an appendix, we also solve for the time to convergence in the three binary attribute, two agent model. We find that the Consistency Model takes approximately twice as long as the Conformity model and that the time to convergence in the  $CC(\frac{1}{2})$  model is more than double that of the Consistency Model and five times that of the Conformity model.

Our analysis so far has concentrated on the time to convergence. Thus, it would seem that our model produces intra cultural consistency and homogeneity (and not heterogeneity) and has nothing to say about inter cultural diversity. Two comments are in order. First, as different runs of the model produce different outcomes, the model naturally provides an explanation for inter cultural diversity – differences in initial conditions and different paths lead to diverse outcomes. Second, the combined model takes a long time to converge. When convergence is slow, we should not expect the system to be in equilibrium – especially if the systems is subject to shocks or errors. Thus, we can interpret the slow time to convergence as consistent with intra cultural heterogeneity. We next make that connection more formal, by explicitly introducing noise.

### Equilibrium Distributions in a Model With Errors

We now further elaborate the tension between consistency and conformity by considering the equilibrium distribution in models that include errors. The inclusion of errors is a standard assumption in learning and conformity models because they create *ergodicity* which guarantees a unique limiting distribution (Young 1998). That will also be the case here. In our models with errors, we obtain unique equilibrium distributions. However, these distributions will have levels of heterogeneity that far outstrip the amount of error introduced exogenously.

To capture errors, we assume that with some small positive probability,  $\epsilon$ , an agent randomly changes an attribute’s value rather than applying its behavioral rule. We are interested in how the two forces singly and jointly magnify these errors. We might expect that by adding noise at a level  $\epsilon$  creates an equilibrium distribution in which approximately  $\epsilon$  of the agents are out of equilibrium. In the Consistency Model and the Conformity Model, we find something close to that. In the Consistent Conformity Model, however, the behavioral rule can magnify the noise term substantially.

### Consistency Model

First, we consider the consistency model. It suffices to consider a single agent, which allows us to reduce our five states to three. We can let *CNS* denote the union of the states *CON* and *C&C*. These represent the states where the agents are consistent. We can then combine the *NOT* and *CRD* into the state *NCN*. In this state, neither agent is consistent. This gives a Markov Process defined over three states *CNS*, *NCN*, and *OBO*. We can write the Markov Transition Matrix as follows:

		$T + 1$		
		<i>CNS</i>	<i>OBO</i>	<i>NCN</i>
T	<i>CNS</i>	$1 - \epsilon$	$\epsilon$	$0$
	<i>OBO</i>	$\frac{1}{2}$	$\frac{1-\epsilon}{2}$	$\frac{\epsilon}{2}$
	<i>NCN</i>	$0$	$1$	$0$

This gives the following system of equations that characterize the equilibrium.

$$\begin{aligned}
P_{CNS} &= (1 - \epsilon)P_{CNS} + \frac{1}{2}P_{OBO} \\
P_{OBO} &= \epsilon P_{CNS} + \frac{1-\epsilon}{2}P_{OBO} + P_{NCN} \\
P_{NCN} &= \frac{\epsilon}{2}P_{OBO}
\end{aligned}$$

Solving these equations gives

$$\begin{aligned}
P_{CNS} &= \frac{1}{1+2\epsilon+\epsilon^2} \\
P_{OBO} &= \frac{2\epsilon}{1+2\epsilon+\epsilon^2} \\
P_{NCN} &= \frac{\epsilon^2}{1+2\epsilon+\epsilon^2}
\end{aligned}$$

### Conformity Model

To analyze the the conformity model, we also combine states. Let  $CDC$  equal the union of the two states in which the two agents have confromed,  $CRD$  and  $C\&C$ , and let  $NCD$  equal the union of the states in which they have not,  $NOT$  and  $CON$ . We can write the Markov Transition Matrix as follows

		$T + 1$		
		$CDC$	$OBO$	$NCD$
T	$CDC$	$1 - \epsilon$	$\epsilon$	$0$
	$OBO$	$\frac{1}{2}$	$\frac{1-\epsilon}{2}$	$\frac{\epsilon}{2}$
	$NCD$	$0$	$1$	$0$

This matrix is identical to the one for the Consistency Model up to a relabeling of the states. Therefore, the equilibrium equals

$$\begin{aligned}
P_{CDC} &= \frac{1}{1+2\epsilon+\epsilon^2} \\
P_{OBO} &= \frac{2\epsilon}{1+2\epsilon+\epsilon^2} \\
P_{NCD} &= \frac{\epsilon^2}{1+2\epsilon+\epsilon^2}
\end{aligned}$$

### CC(p) Model

For the Consistent Conformity Model, we require all five categories of states. We can write the Markov Transition matrix between those states as follows

		$T + 1$				
		<i>C&amp;C</i>	<i>OBO</i>	<i>CRD</i>	<i>CON</i>	<i>NOT</i>
T	<i>C&amp;C</i>	$1 - \epsilon$	$\epsilon$	0	0	0
	<i>OBO</i>	$\frac{1}{4}$	$\frac{(1-\epsilon)}{2}$	$\frac{p+\epsilon-\epsilon p}{4}$	$\frac{1-p-\epsilon p}{4}$	$\frac{\epsilon}{4}$
	<i>CRD</i>	0	$1 - p + \epsilon p$	$p - \epsilon p$	0	0
	<i>CON</i>	0	$p + \epsilon + \epsilon p$	0	$1 - p - \epsilon + \epsilon p$	0
	<i>NOT</i>	0	1	0	0	0

The following system of five equations characterizes the equilibrium.

$$P_{C\&C} = (1 - \epsilon)P_{C\&C} + \frac{P_{OBO}}{4}$$

$$P_{OBO} = P_{OBO} + \frac{(1-\epsilon)P_{OBO}}{2} + (1 - p + \epsilon p)P_{CRD} + (p + \epsilon - \epsilon p)P_{CON} + \frac{\epsilon P_{OBO}}{4}$$

$$P_{CRD} = \frac{(p+\epsilon-\epsilon p)P_{OBO}}{4} + (p - \epsilon p)P_{CRD}$$

$$P_{CON} = \frac{(1-p+\epsilon p)P_{OBO}}{4} - (1 - p - \epsilon + \epsilon p)P_{CON}$$

$$P_{NOT} = \frac{\epsilon P_{OBO}}{4}$$

Solving gives the following

$$P_{C\&C} = \frac{1}{1+4\epsilon+\epsilon^2+\alpha\epsilon+\alpha^{-1}\epsilon}$$

$$P_{OBO} = \frac{4\epsilon}{1+4\epsilon+\epsilon^2+\alpha\epsilon+\alpha^{-1}\epsilon}$$

$$P_{CRD} = \frac{\alpha\epsilon}{1+4\epsilon+\epsilon^2+\alpha\epsilon+\alpha^{-1}\epsilon}$$

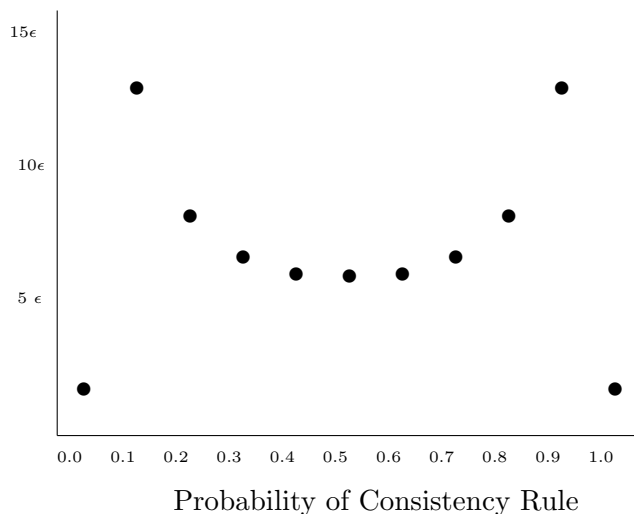
$$P_{CON} = \frac{\alpha^{-1}\epsilon}{1+4\epsilon+\epsilon^2+\alpha\epsilon+\alpha^{-1}\epsilon}$$

$$P_{NOT} = \frac{\epsilon^2}{1+4\epsilon+\epsilon^2+\alpha\epsilon+\alpha^{-1}\epsilon}$$

Where  $\alpha = \frac{(p+\epsilon-\epsilon p)}{(1-p+\epsilon p)}$  which equals the ratio of the probability of moving from *OBO* to *CON* to the probability of moving from *OBO* to *CRD*. The higher  $\alpha$ , the more time the system will spend in *CON*. The lower  $\alpha$ , the more time that the system will spend in *CRD*. Setting  $p = \frac{1}{2}$  maximizes the time spent in the consistent conformity state (*C&C*). Figure 5 shows the percentage of the time the system spends outside of state *C&C* as a function of  $p$  for a given error level  $\epsilon$ . If we let  $p$  go to 0 then  $\alpha$  converges to  $\epsilon$  and the system spends half of the time outside of the state *C&C*. Similarly, if we let  $p$  go to 1 then  $\alpha$  converges to  $\frac{1}{\epsilon}$ , and the system again spends half of the time outside of the state *C&C*.

Note that except for the units on the y-axis, this figure matches figure 4 exactly. The equivalence, modulo a rescaling, of the time to equilibrium and the distance to the perfectly conformed and consistent equilibrium is an artifact of our assumptions. But the correlation between the two generally hints at an important insight: the longer the time to equilibrium, the more complex the dynamics. The more complex the dynamics, the larger the potential effects of error.

Figure 5: Distance to Conformed and Consistent Equilibrium: Error Model



## 4 Numerical Experiments

To test whether the results from our simple model extend to larger numbers of agents, attributes, and attribute values, we ran numerical experiments in which we varied the number of agents from two to one thousand, the number of attributes from two to ten, and the number of values per attribute from two to six.<sup>12</sup> The results that we found were consistent with the analytic results from our two-person, two-attribute model.

We present here two sets of computational experiments. In the first set, we measure the time to convergence. In the second set, we measure levels of consistency and conformity in the models with errors.

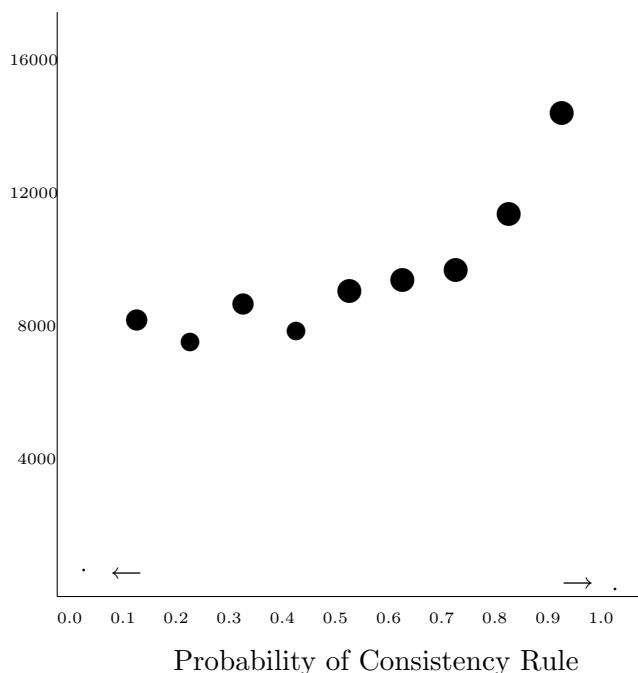
### Time To Convergence Experiments

Figure 6 shows the time to convergence as a function of  $p$  for a model with one hundred agents, ten attributes, and six values per attribute. The results are averages of over fifty trials. All of the differences are statistically significant. The arrows point to the values for  $p = 0$  and  $p = 1$ , which are otherwise easy to overlook.

Our theoretical results suggested that the time to convergence should increase as  $p$  approaches zero and one. Here, we only see that phenomenon as  $p$  approaches one.

<sup>12</sup>We wrote two separate programs, one in *C* and one in Repast (a java-based modeling toolkit). We used the faster *C* program to sweep the attribute values, and the Repast program to generate the graphs that you see in the paper. We also tested our models against the analytic results presented in the paper.

Figure 6: Time to Convergence in Number of Periods



The asymmetry can be explained by the fact the number of agents is far larger than the number of attributes. The probability of applying the consistency rule must be very small before we would expect to see the time to convergence to increase given the greater need for conformity.

Even though all of the models converge, the magnitude of these differences appears meaningful. In the Conformity Model and the Consistency Model, the system converges in a few hundred periods. The Consistent Conformity model can take more than fifteen thousand periods to converge. Our model is abstract enough that we need not attach any specific span of time to a period; time is simply the number of agent actions. However, if we set periods equal to day, then this difference is between around a year and more than forty years.

## Experiments in Models with Error

In the next set of experiments, we test to see whether errors have a much larger effect in the Consistent Conformity Model. To make this comparison, we need some measures of consistency and conformity. In constructing these measures, we refer back to notation we used in constructing possible utility functions. Recall that  $s(a^j)$  equals the number of times the most common attribute appears in agent  $j$ 's vector of attributes. We can write

$$s(a^j) = \max_{i \in A} \{ |i| : a_i^j = a \}$$

$$\text{pconsistent} = \frac{\sum_{j=1}^M s(a^j)}{AM}$$

Thus, *pconsistent* takes on values between 0 and 1. We define *pconformity* to be the average of the *conformity payoff functions*. Recall that the conformity payoff function equals the average number of agents who agree with the agent's attribute values.

$$f(a^j, a^{-j}) = \frac{\sum_{k \neq j} \sum_{i=1}^M \delta(a_i^j, a_i^k)}{NM}$$

where  $\delta(a_i^j, a_i^k) = 1$  if and only if  $a_i^j = a_i^k$

$$\text{pconformity} = \frac{\sum_{j=1}^M f(a^j, a^{-j})}{M}$$

Thus, if the entire population has conformed, then the value of *pcoordinate* equals one. The table below gives the values of *pconsistent* and *pconformity* for each of the three models under various levels of agent error for a model with ten attributes and five values per attribute and 100 agents.

		probability of consistency check					
		p = 0.0		p = 0.5		p = 1.0	
		pconformity	pconsistent	pconformity	pconsistent	pconformity	pconsistent
noise	0	1	0.360	1	1	0.200	1
	0.005	0.736	0.373	0.354	0.556	0.199	0.970
	0.01	0.585	0.376	0.299	0.510	0.200	0.946
	0.02	0.482	0.376	0.269	0.483	0.201	0.904

Table 2: **Consistency and Conformity Environments.** Average percent values and standard deviations of inter-agent value difference (pconformity) and intra-agent value difference (pconsistent) over the last 1000 interactions of 100 runs with 100 agents, 10 attributes, 5 values per attribute and a total run time of 5,000,000 interactions per run.

Notice that with no errors, the  $CC(\frac{1}{2})$  model converges to a consistent and coordinated state as we expect. Further, for the  $CC(\frac{1}{2})$  model, the introduction of even the tiniest bit of noise (0.005) leads to substantial heterogeneity both between agents (0.354) and within agents (0.556), far more than in the other two models (0.736 and 0.970 respectively). A little noise has a much larger effect when both forces

operate.<sup>13</sup> These computational experiments show that the insight generated in the simpler mathematical model – that the effect of noise when both forces are in play greatly exceeds the sum of the individual effects – becomes even more pronounced for larger systems. Thus, even small amounts of error may prevent a society of people who wish to conform and be consistent from achieving those two goals. Instead, the society may exhibit substantial intra cultural heterogeneity.

## 5 Discussion

In this paper, we have shown how a simple model that includes forces for consistency and conformity can produce three empirical regularities: inter cultural diversity, cultural signatures, and intra cultural heterogeneity. The model also reveals how varying the weights of the forces slows converges and increases heterogeneity. In addition, in a version of our model that includes errors, the equilibrium distribution includes substantial heterogeneity.

Of course, other candidate explanations exist for intra-cultural heterogeneity. Within a culture people differ in their preferences, experiences, and ambitions, which, too, can create behavioral differences within a culture. Moreover, just as people choose to conform their attributes to be like others, they also try to distinguish themselves. And, as we already mentioned, people typically interact in small groups, so within-group conformity and consistency need not necessarily lead to conformity and consistency at the societal level. We do not dispute or challenge these other causes of within-culture heterogeneity, nor do we think that their inclusion would have straightforward implications. Such an inference would run counter to the main methodological contribution of this paper: the *non-linear* additivity of dynamical systems. That methodological insight—that the whole differs from the parts when we look at forces—may be as important as its application within our model to culture.

In addition to providing a possible explanation for cultural differences, our analysis also suggests some testable hypotheses and a possible rethinking of how we measure intra-cultural heterogeneity. First, the greater the likelihood of error, the less conformity we should see. We might speculate that informational systems provide a crude proxy for the transmission error of cultural traits but that closer relations between individuals push in the opposite direction. Thus, whether advanced economies should exhibit more or less intra cultural heterogeneity is difficult to predict. Second, in a society in which the relative tendency to conform is high relative to the tendency to be consistent, people may be less consistent but more similar. Thus, whether one culture appears more or less heterogeneous depends on the type of questions asked in a survey. If the questions ask about an existing behavior, we'd expect a higher conforming society to appear less heterogeneous. However, if the questions are hypothetical, the

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<sup>13</sup>Comparing results for cases with noise = 0.005, the p-value for a test of the difference of means for conformity for the p=0.0 and p=0.5 models is  $2.23 \times 10^{-304}$  and the p-value for a test of the difference of means for consistency for the p=0.5 and p=1.0 models is  $1.61 \times 10^{-831}$ .



lack of consistency may give respondents a variety of possible behaviors to apply in the novel context. Thus, a less individualistic society, like Japan, could appear more heterogeneous than a highly individualistic society like the United States.

Though we focus in this paper on ethnic and national cultures, we might also apply our model to corporate and organizational cultures. Within corporations and organizations, people face incentives to conform as well as to be consistent, though for reasons that differ slightly from those we described above. Finally, our model could be apply to the creation of party ideology. Members of a political party also desire conformity and consistency, and these two desires may result in the analogous effects: differences within and between parties as well as party ideology. In the party model, attribute values could represent participants' ideal points in policy or preference space. The internal consistency rule would capture the individual desire for a consistent ideology, and the external conformity rule would capture the collective desire for party cohesiveness. The model suggests that a consistent cohesiveness would not emerge quickly without top down encouragement or even enforcement. We can push this insight even further. Within any organization or collection of people, be it an interest group, a community organization, or an academic department these same two forces may operate. People seek common ground—they want to conform—and they also want to be consistent. Yet, we've seen that even with a little bit of error, these two forces do not result in a coherent, consistent set of attributes. This finding agrees with what we see in the real world. Few, in any, groups and organizations converge to a state of consistent conformity. Relatedly, we might apply our model to the question of cultural integration (Kuran and Sandholm 2003). When people from two cultures interact in a common society, they face these two pressures, a desire to be consistent with their culture and a desire to conform to the wider culture.

The existence of intra-cultural variation and our proposed explanation leave open the question of whether it plays any significant role. Within-culture variation has empirical relevance for prediction. Durham (1991) demonstrates variety in types of marriage custom within Tibetan culture. Thompson (1975) provides evidence of significant intra-cultural variation in willingness to accept delayed economic gratification between three communities in Uganda. A study of a series of six cultures across four continents by Mintun and Lambert (1964) and Whiting (1963) found that all but one variable on child rearing behavior was better captured by intra- rather than inter-cultural variation. Pelto and Pelto (1975) cite a study of residents of Northern Minnesota to illustrate their argument that “even in supposedly homogenous communities there is a wide range of variation in most aspects of belief and behavior” (Pelto and Pelto 1975, p. 6). Moreover, even ritual and ceremonial practices, which are usually treated as encapsulating the most salient elements of inter-cultural variation, exhibit variation between members of a single culture. Adler and Graham (1989) demonstrate that businessmen negotiate more differently with people from within their own culture than with people from other cultures.

In general, the existence of intra-cultural, or intra-organizational, heterogeneity may be seen as advantageous. It may promote innovation in the form of cultural

evolution. The tension between conformity and consistency maps to related tensions between “exploiters versus explorers”, “conformers versus nonconformers”, and “scroungers versus producers” and may balance stability and variation (Kameda and Nakanishi 2002, Boyd and Richerson 2001, Rogers 1995, Nisbett and Ross 1980, Tindall 1976, March 1991, Weick 1969, Campbell 1965, Roberts and Zuni 1964). As individuals have incentives to conform with the behavior of the most successful actors in a system, successful strategies persist. Likewise, because individuals also have incentives to be consistent, deviance also persists; thus allowing for the discovery of new and better strategies that will in turn be adopted by others in the system. Furthermore, systems with both conforming and consistent individuals can both transmit and produce learned knowledge. Cognitive diversity may result in productive and robust societies (Wallace 1991, Page 2007).

We must be careful not to attach normative significance to reducing intra-group heterogeneity. This lack of convergence, be it in a society, a political, party, or an organization, may, on balance, be a good thing. Intra-group heterogeneity allows for experimentation. It allows a collection of individuals to balance exploration with exploitation by maintaining the variation necessary for further exploration (March 1991, Axelrod and Cohen 2000) and better problem solving and prediction (Page 2007). Thus, diversity may make societies more robust by providing the potential to adapt to changing circumstances (Bednar 2006). Societies that lack intra-cultural diversity may be prone to collapse (Diamond 2005). In sum, the persistence of diversity in the face of two homogenizing forces might be seen as not only counterintuitive but serendipitous.

## Appendix

**Claim 4** *The time to convergence for the consistency model with binary values and  $M$  attributes of order  $M^2$ .*

pf:<sup>14</sup> Let  $x$  denote the number of attributes with value 1. Let  $T_x$  be the time to convergence if at location  $x$ . Let  $m_x$  be the probability of increasing or decreasing the number of attributes with value 1. By the previous claim, these probabilities are equal. After one time period, the expected time has to be one period less. Therefore, we have the following equation:

$$T_x - 1 = m_x T_{x+1} + m_x T_{x-1} + (1 - 2m_x) T_x$$

This reduces to

$$-1 = m_x [(T_{x+1} - T_x) - (T_x - T_{x-1})]$$

Recall from Claim 1 that  $m_x = \frac{(M-x)x}{M(M-1)}$ . For large  $M$  we can approximate this as  $m_x = \frac{(M-x)x}{M^2}$ . Let  $p(x) = \frac{x}{M}$ , so that  $m_x = p(x)[1 - p(x)]$ . We then can rewrite  $T_{x+1} - T_x$  as

$$\frac{1}{M} \cdot \frac{(T(p(x+1))) - T(p(x))}{\frac{1}{M}}$$

For large  $M$ , this converges to  $\frac{\partial T(p(x))}{\partial p}$ . It follows that we can write the following approximation:

$$(T_{x+1} - T_x) - (T_x - T_{x-1}) \sim \frac{1}{M} \left[ \frac{\partial T(p(x))}{\partial p} - \frac{\partial T(p(x-1))}{\partial p} \right]$$

Which in turn we can approximate as

$$\frac{1}{M^2} \frac{\partial^2 T(p(x))}{\partial p^2}$$

We can therefore approximate our initial difference equation as

$$-1 = p(x)[1 - p(x)] \frac{1}{M^2} \frac{\partial^2 T(p(x))}{\partial p^2}$$

Rearranging terms and simplifying notation gives

$$\frac{\partial^2 T(p)}{\partial p^2} = -\frac{M^2}{p(1-p)}$$

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<sup>14</sup>We provide a somewhat loose proof here that requires approximations. The result has been verified in simulations frequently by computer scientists and physicists.

We also have that  $T(0) = T(1) = 0$ . The solution to this differential equation is

$$T(p) = M^2 \left[ p \log\left(\frac{1}{p}\right) + (1-p) \log\left(\frac{1}{1-p}\right) \right]$$

which completes the proof.

**Claim 10:** *The expected time to equilibrium for the CC(p) Rule equals  $1\frac{7}{8} + \frac{1}{p(1-p)}$*   
 pf: We can write the following equations.

$$\begin{aligned} T_{C\&C} &= 0 \\ T_{OBO} &= 1 + \frac{1}{4}T_{C\&C} + \frac{1}{2}T_{OBO} + \frac{p}{4}T_{CON} + \frac{(1-p)}{4}T_{CRD} \\ T_{CON} &= 1 + (1-p)T_{OBO} + pT_{CON} \\ T_{CRD} &= 1 + pT_{OBO} + (1-p)T_{CRD} \\ T_{NOT} &= 1 + T_{OBO} \end{aligned}$$

By substitution, these equations imply that

$$\begin{aligned} T_{CON} &= \frac{1}{1-p} + T_{OBO} \\ T_{CRD} &= \frac{1}{p} + T_{OBO} \end{aligned}$$

These in turn imply that

$$T_{OBO} = 1 + \frac{1}{2}T_{OBO} + \frac{p}{4(1-p)} + \frac{(1-p)}{4p} + \frac{1}{4}T_{OBO}$$

This reduces to

$$T_{OBO} = 4 + \frac{(1-2p+2p^2)}{p(1-p)}$$

Substituting back into the other equations gives

$$\begin{aligned} T_{CON} &= 4 + \frac{(1-p+2p^2)}{p(1-p)} \\ T_{CRD} &= 4 + \frac{(2-3p+2p^2)}{p(1-p)} \\ T_{NOT} &= 5 + \frac{(1-2p+2p^2)}{p(1-p)} \end{aligned}$$

Therefore the average time to convergence equals

$$\frac{1}{2} \left( 4 + \frac{(1-2p+2p^2)}{p(1-p)} \right) + \frac{1}{8} \left( 4 + \frac{(1-p+2p^2)}{p(1-p)} + 4 + \frac{(2-3p+2p^2)}{p(1-p)} + 5 + \frac{(1-2p+2p^2)}{p(1-p)} \right)$$

Which reduces to

$$1\frac{7}{8} + \frac{1}{p(1-p)}$$

For the special case  $p = \frac{1}{2}$ , these equations become

$$T_{OBO} = 1 + \frac{1}{4}T_{C\&C} + \frac{1}{2}T_{OBO} + \frac{1}{8}T_{CON} + \frac{1}{8}T_{CRD}$$

$$T_{CON} = 1 + \frac{1}{2}T_{OBO} + \frac{1}{2}T_{CON}$$

$$T_{CRD} = 1 + \frac{1}{2}T_{OBO} + \frac{1}{2}T_{CRD}$$

$$T_{NOT} = 1 + T_{OBO}$$

By substitution, these equations imply that  $T_{CON} = T_{CRD} = 2 + T_{OBO}$ . Which in turn implies that  $T_{OBO} = 1 + \frac{1}{2}T_{OBO} + \frac{1}{2} + \frac{1}{4}T_{OBO}$ . This is an equation in a single variable,  $T_{OBO}$ . Solving gives equation gives  $T_{OBO} = 6$ . Substituting back into the other equations gives  $T_{CON} = T_{CRD} = 8$  and  $T_{NOT} = 7$ . Therefore the average time to convergence equals  $\frac{1}{2}(6) + \frac{1}{8}(8 + 8 + 7) = 5\frac{7}{8}$

### Three Attribute Model

We can extend our model to include a third attribute. This increases the number of possible states from sixteen to sixty four. To describe the dynamics of this system, we create eight categories:

<i>State</i>	<i>Agents</i>	<i>Prob</i>
Coordinated & Consistent (C&C)	(a,a,a) (a,a,a)	$\frac{1}{32}$
Consistent Not Coordinated (CON)	(a,a,a) (b,b,b)	$\frac{1}{32}$
Coordinated Not Consistent (CRD)	(a,b,b) (a,b,b)	$\frac{3}{32}$
Off By One (OBO)	(a,a,b) (a,a,a)	$\frac{6}{32}$
Off By Two (OBT)	(a,b,b) (a,a,a)	$\frac{6}{32}$
Two By Two (TWO)	(a,a,b) (a,b,b)	$\frac{6}{32}$
Switch Two (SWI)	(a,a,b) (a,b,a)	$\frac{6}{32}$
Mirror States (MIR)	(a,a,b) (b,b,a)	$\frac{3}{32}$

We can then prove similar claims for time to convergence.

**Claim 11** *With two agents and three binary attributes, the expected time to equilibrium for the Internal Consistency Rule equals  $7\frac{5}{16}$ .*

pf: If we apply the internal consistency rule we get the following system of equations

$$T_{OBO} = 1 + \frac{2}{3}T_{OBO} + \frac{1}{6}T_{OBT}$$

$$T_{OBT} = 1 + \frac{2}{3}T_{OBT} + \frac{1}{6}T_{OBO}$$

$$T_{CRD} = 1 + \frac{1}{3}T_{CRD} + \frac{1}{3}T_{TWO} + \frac{1}{3}T_{OBO}$$

$$T_{MIR} = 1 + \frac{1}{3}T_{MIR} + \frac{1}{3}T_{SWI} + \frac{1}{3}T_{OBT}$$

$$T_{TWO} = 1 + \frac{1}{3}T_{TWO} + \frac{1}{6}T_{CRD} + \frac{1}{6}T_{SWI} + \frac{1}{3}T_{OBT}$$

$$T_{SWI} = 1 + \frac{1}{3}T_{SWI} + \frac{1}{6}T_{MIR} + \frac{1}{6}T_{TWO} + \frac{1}{3}T_{OBO}$$

The solution to this set of equations equals  $T_{OBO} = 6$ ,  $T_{OBT} = 6$ ,  $T_{CRD} = 9$ ,  $T_{TWO} = 9$ ,  $T_{SWI} = 9$ ,  $T_{MIR} = 9$ . Plugging these back into the probabilities of each initial state gives the result.

**Claim 12** *With two agents and three binary attributes, the expected time to equilibrium for the External Conformity Rule equals  $3\frac{1}{2}$ .*<sup>15</sup>

pf: If we apply the external conformity rule we get the following system of equations

$$T_{OBO} = 1 + \frac{2}{3}T_{OBO}$$

$$T_{TWO} = 1 + \frac{2}{3}T_{TWO}$$

$$T_{CON} = 1 + T_{OBT}$$

$$T_{OBT} = 1 + \frac{1}{3}T_{OBT} + \frac{1}{3}T_{TWO} + \frac{1}{3}T_{OBO}$$

$$T_{SWI} = 1 + \frac{1}{3}T_{SWI} + \frac{1}{3}T_{OBO} + \frac{1}{3}T_{TWO}$$

$$T_{MIR} = 1 + \frac{2}{3}T_{SWI} + \frac{1}{3}T_{OBT}$$

The solution to this set of equations equals  $T_{OBO} = 3$ ,  $T_{TWO} = 3$ ,  $T_{CON} = \frac{11}{2}$ ,  $T_{OBT} = \frac{9}{2}$ ,  $T_{SWI} = \frac{9}{2}$ ,  $T_{MIR} = \frac{11}{2}$ . Plugging these back into the probabilities of each initial state gives the result.

Our final claim considers the CC(p) model. Here, we provide a numerical result for the case  $p = 1/2$ .

**Claim 13** *With two agents and three binary attributes, the expected time to equilibrium for the CC( $\frac{1}{2}$ ) equals approximately 17.91.*

pf: Using the notation from above, we can write the equations for the time to convergence as follows:

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<sup>15</sup>We thank Casey Schneider-Mizell for correcting an earlier proof and providing the matrix representation

$$\begin{aligned}
T_{CON} &= 1 + (1-p)T_{CON} + pT_{OBT} \\
T_{CRD} &= 1 + (1-p)T_{CRD} + p\left(\frac{1}{3}T_{OBO} + \frac{1}{3}T_{TWO} + \frac{1}{3}T_{CRD}\right) \\
T_{OBO} &= 1 + (1-p)\left(\frac{2}{3}T_{OBO} + \frac{1}{6}T_{CRD}\right) + p\left(\frac{2}{3}T_{OBO} + \frac{1}{6}T_{OBT}\right) \\
T_{OBT} &= 1 + (1-p)\left(\frac{1}{3}T_{OBT} + \frac{1}{3}T_{OBO} + \frac{1}{3}T_{TWO}\right) + p\left(\frac{2}{3}T_{OBT} + \frac{1}{6}T_{CRD} + \frac{1}{6}T_{OBO}\right) \\
T_{TWO} &= 1 + (1-p)\left(\frac{2}{3}T_{TWO} + \frac{1}{3}T_{CRD}\right) + p\left(\frac{1}{3}T_{OBT} + \frac{1}{6}T_{CRD} + \frac{1}{6}T_{SWI} + \frac{1}{3}T_{TWO}\right) \\
T_{SWI} &= 1 + (1-p)\left(\frac{1}{3}T_{SWI} + \frac{1}{3}T_{OBO} + \frac{1}{3}T_{TWO}\right) + p\left(\frac{1}{3}T_{SWI} + \frac{1}{3}T_{OBO} + \frac{1}{6}T_{MIR} + \frac{1}{6}T_{TWO}\right) \\
T_{MIR} &= 1 + (1-p)\left(\frac{1}{3}T_{OBT} + \frac{2}{3}T_{SWI}\right) + p\left(\frac{1}{3}T_{MIR} + \frac{1}{3}T_{SWI} + \frac{1}{3}T_{OBT}\right)
\end{aligned}$$

We can write this in matrix form as follows:

$$\begin{pmatrix} T_{CON} \\ T_{CRD} \\ T_{OBO} \\ T_{OBT} \\ T_{TWO} \\ T_{SWI} \\ T_{MIR} \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{pmatrix} + \begin{pmatrix} 1-p & 0 & 0 & p & 0 & 0 & 0 \\ 0 & 1-\frac{2}{3}p & \frac{1}{3}p & 0 & \frac{1}{3}p & 0 & 0 \\ 0 & \frac{1}{6}(1-p) & \frac{2}{3}p & \frac{1}{6}p & 0 & 0 & 0 \\ 0 & \frac{1}{6}p & \frac{1}{3} - \frac{1}{6}p & \frac{1}{3} + \frac{1}{3}p & \frac{1}{3}(1-p) & 0 & 0 \\ 0 & \frac{1}{3} - \frac{1}{6}p & 0 & \frac{1}{3}p & \frac{2}{3} - \frac{1}{3}p & \frac{1}{6}p & 0 \\ 0 & 0 & \frac{1}{3} & 0 & \frac{1}{3} - \frac{1}{6}p & \frac{1}{3} & \frac{1}{6}p \\ 0 & 0 & 0 & \frac{1}{3} & 0 & \frac{2}{3} - \frac{1}{3}p & \frac{1}{3}p \end{pmatrix} \begin{pmatrix} T_{CON} \\ T_{CRD} \\ T_{OBO} \\ T_{OBT} \\ T_{TWO} \\ T_{SWI} \\ T_{MIR} \end{pmatrix}$$

Solving these equations and multiplying each  $T_x$  by the probability of starting in state  $x$  produces the result.

		probability of consistency check											
		p = 0.0				p = 0.5				p = 1.0			
noise		pconformity		pconsistent		pconformity		pconsistent		pconformity		pconsistent	
		mean	stdev	mean	stdev	mean	stdev	mean	stdev	mean	stdev	mean	stdev
0		1	0	0.360	0.082	1	0	1	0	0.200	0.016	1	0
0.005		0.736	0.064	0.373	0.044	0.354	0.081	0.556	0.067	0.199	0.012	0.970	0.009
0.01		0.585	0.052	0.376	0.030	0.299	0.037	0.510	0.033	0.200	0.012	0.946	0.012
0.02		0.482	0.044	0.376	0.023	0.269	0.017	0.483	0.017	0.201	0.012	0.904	0.017

Table 3: **Consistency and Conformity Environments with Error.** Average percent values and standard deviations of inter-agent value difference (pconformity) and intra-agent value difference (pconsistent) over the last 1000 interactions of 100 runs with 100 agents, 10 features, 5 values per feature and a total run time of 5,000,000 interactions per run.



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