

Opportunities in quantitative historical linguistics

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work with

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collaborative with

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Outline

- Brief history of languages at SFI
- The steps toward quantitative phylogenetics
 - Example I: lexical reconstruction
 - Example II: inferring models of word-order change
- New opportunities for empirical discovery

● The Evolution of Human Languages Program at SFI

<<http://ehl.santafe.edu/>>

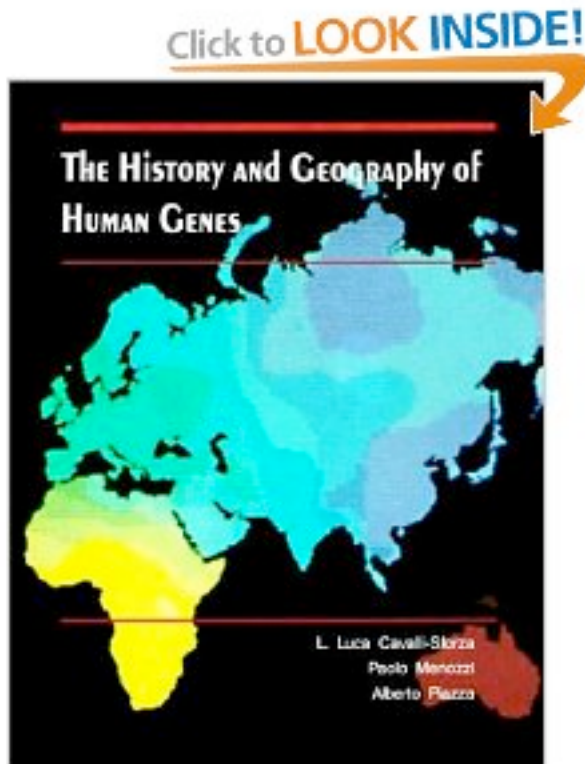
<<http://starling.rinet.ru/main.html>>

Goals: Deep reconstruction of language history and connection with genes and the archaeological record



Murray Gell-Mann

George Starostin

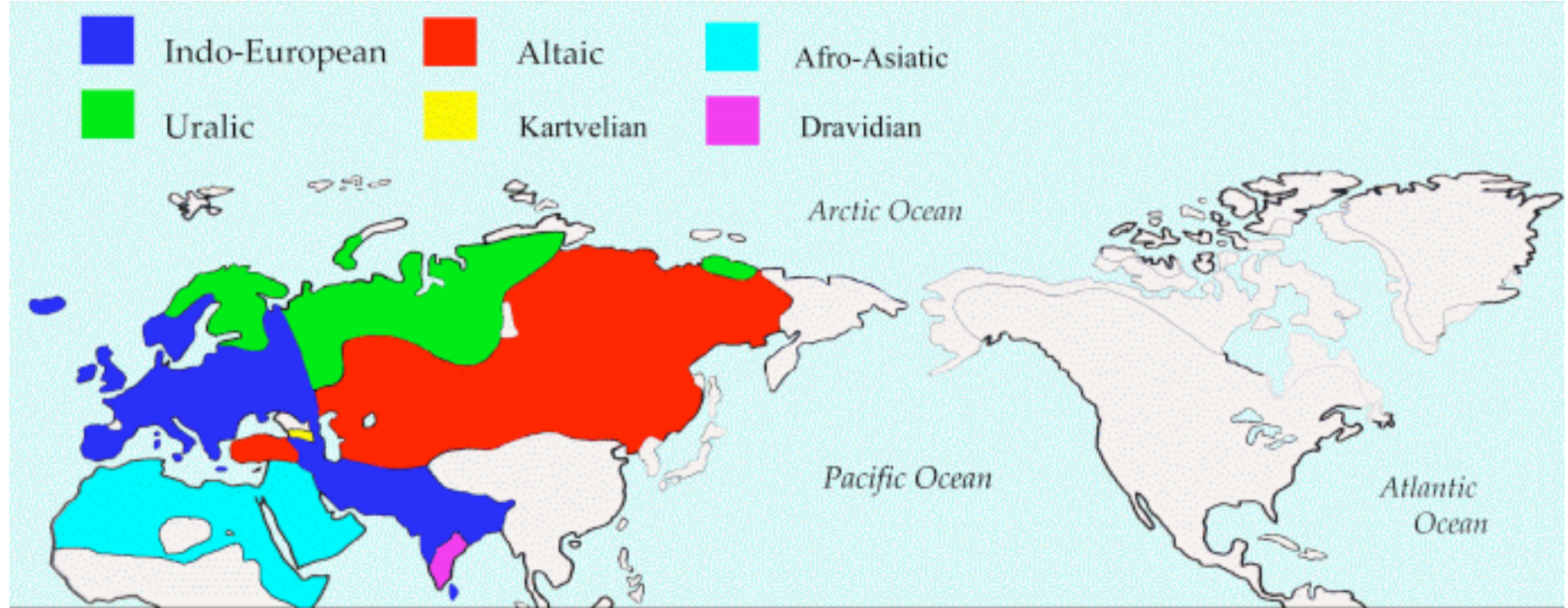


Ilia Peiros



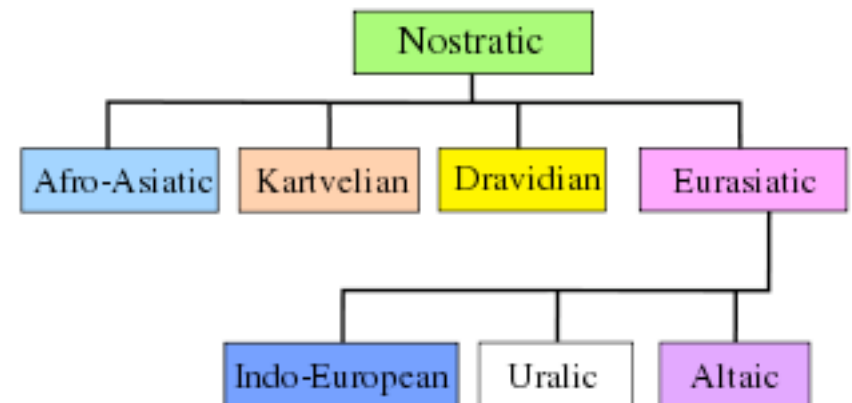
Sergei Starostin

Deep reconstruction: the Nostratic hypothesis



<http://starling.rinet.ru/maps/maps.php?lan=en>

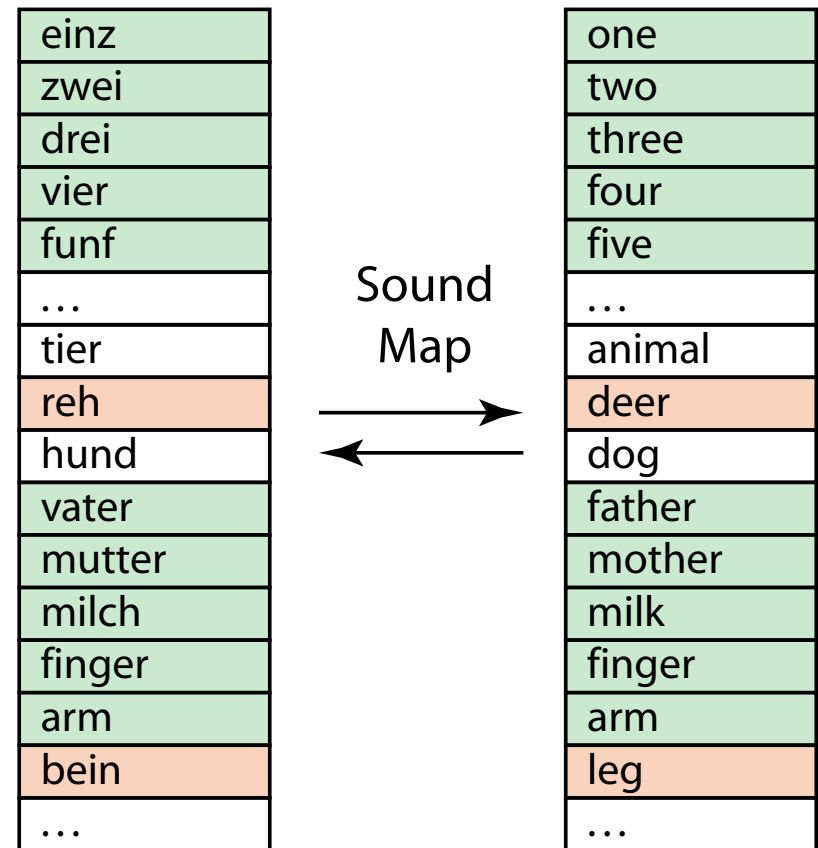
- Coined by Holger Pedersen (1903)
- Modern form of the hypothesis by Vladislav Ilitch-Svitych and Aharon Dolgopolsky (1960s -- present)
- Estimated 12,000-15,000 BCE



http://en.wikipedia.org/wiki/Nostratic_languages

Methods: **lexicostatistics** and **glottochronology**

- Assign any sound map without penalty, but require regularity
- Exclude borrowed items in either language from consideration
- **Identify fraction preserved cognates;**
convert to separation time (penalty)
- Attempt to fit separation times to an ultrametric structure (tree)

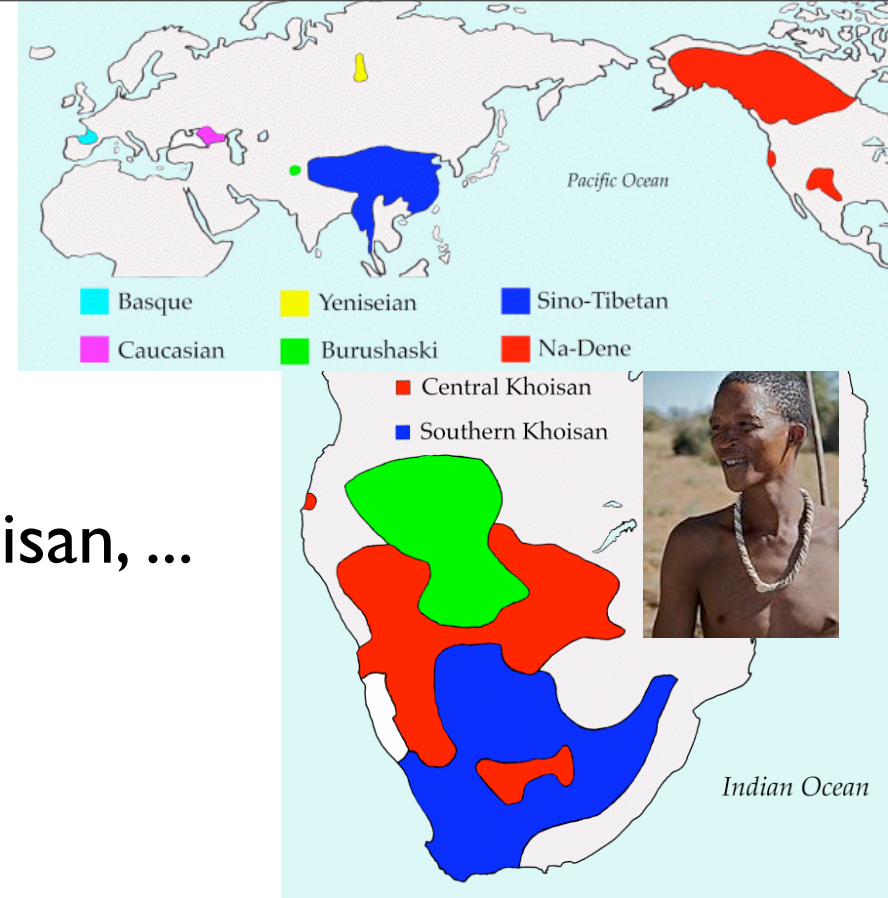


$$P_{\text{Preserve}}(\text{word}) = e^{-t/\tau}$$

$$\Delta t_{\text{sep}} = -\tau \log (\text{frac. preserved})$$

EHL today

- The Dene-Caucasion hypothesis
- Borean? Relic of the last ice-age?
- Reconstructions of Dravidian, Khoisan, ...
- The EHL database and Starling



Turkic etymology :

New query

Total of 2017 records 101 page

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<http://starling.rinet.ru/cgi-bin/response.cgi?root=config&morpho=0&basename=\data\alt\turcet&first=1>

Proto-Turkic	Altaic etymology	Meaning	Russian meaning	Old Turkic	Karakhanid	Turkish	Tatar	Middle Turkic	Uzbek	Uighur	Sary-Yughur	Azerbaidzhan	Tur.
*Ab ☐	Altaic etymology ☐	hunt, chase	охота	ab (Orkh.), av (OUygh.)	av (MK)	av	aw	aw (Pav. C.)	av	aw, dial. o		av	av
*ab- ☐	Altaic etymology ☐	to crowd, come together	собираться, встречаться	av- (OUygh.)	av- (MK, KB)								
					avut (MK),								

● Concepts and steps in a quantitative phylogenetics

- Roles of Likelihood and Bayesian methods
 - Frequent-pattern versus rare-feature innovations
 - Bayes's theorem and prior prejudice
 - Typological constraints and Bayesian priors
 - Information criteria and significance of parameters
- The likelihood part of a phylogenetic algorithm
 - Overall structure of sound and meaning change
 - Alignment, sound correspondence, and errors
 - Context discovery, detection of borrowings
 - Classification and reconstruction

Rare innovations versus clusters of common innovations

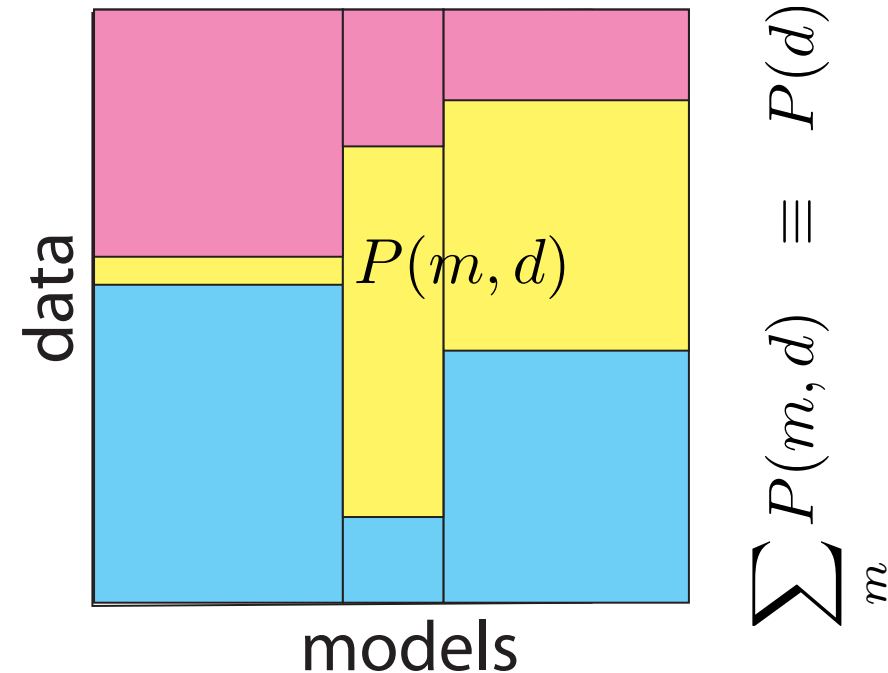
- Rare innovations: single features with ~ 0 probability to occur by chance (go in Bayesian priors)
 - Imply common descent or borrowing, even w/o mathematics
 - Only seen once: hard to assign probabilities from frequencies
 - Common in morpho-syntactic features
 - Useless for dating; do not support induction
- Common variations: (estimate with likelihood)
 - Examples: sound shift and meaning shift in core lexicon
 - Individually uninformative, but can assign probabilities from data
 - Require math to handle, but do support induction, and can be informative about dates if change processes are regular

Bayes's Theorem and model comparison

- Represent both data *and* models with a joint probability
- Split joint probability into conditionals either of two ways

$$\begin{aligned} P(m, d) &= P(m \mid d) P(d) \\ &= P(d \mid m) P(m) \end{aligned}$$

$$\sum_d P(m, d) \equiv P(m)$$



- Bayes's theorem: priors and likelihoods

$$\begin{aligned} P(m \mid d) &= \frac{P(d \mid m) P(m)}{P(d)} \text{ Bayesian prior} \\ \text{Bayesian posterior} &= \frac{P(d \mid m) P(m)}{\sum_{m'} P(d \mid m') P(m')} \end{aligned}$$

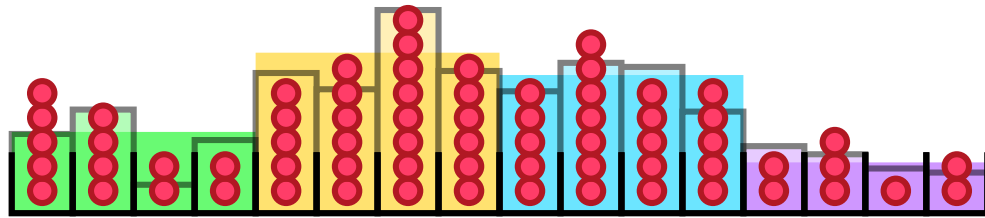
Typological constraints are a natural domain for priors (Ian's lecture)

- Three roles for priors
 - Include frequency evidence from outside this sample
 - Include non-frequency evidence (rare innovations)
 - Represent out-of-field evidence (molecular phylogenies)
- On states
 - phoneme inventory, word order, ...
 - implicational relations (pronouns, time, color, aspect)
- On transitions
 - phoneme contexts, intermediate word-order states (NDO)
 - geometric models of phonology or semantics?

Akaike and Bayesian Information Criteria

$$\text{AIC} \equiv -2 \log (L) + 2k$$

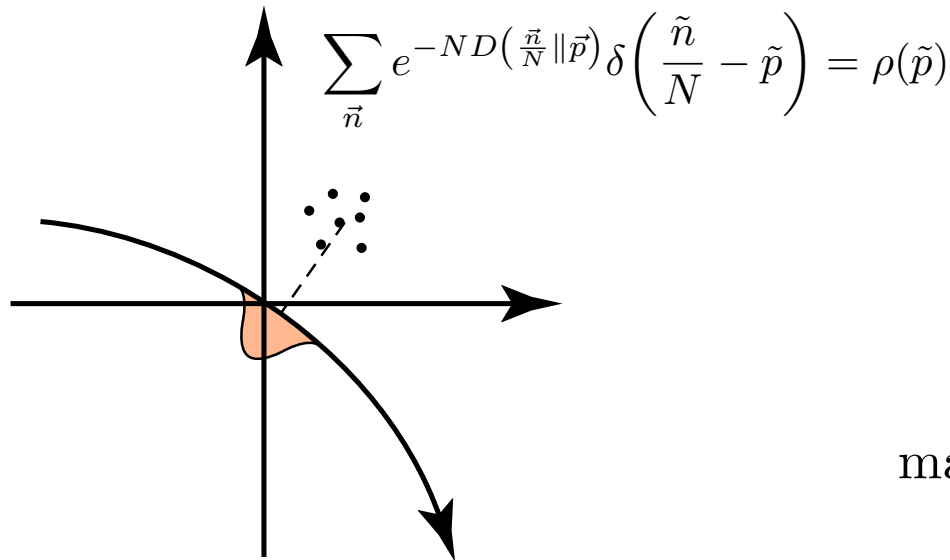
$$\text{BIC} \equiv -2 \log (L) + k \log (n)$$



$$\begin{aligned} P(n_1, \dots, n_K) &= \prod_{i=1}^K p_i^{n_i} \left(\frac{N!}{n_1!, \dots, n_K!} \right) \\ &= e^{-ND(\frac{\vec{n}}{N} \parallel \vec{p})} \end{aligned}$$

$$D\left(\frac{\vec{n}}{N} \parallel \vec{p}\right) \equiv \sum_{i=1}^K \frac{n_i}{N} \log \frac{\frac{n_i}{N}}{p_i}$$

**Kullback-Leibler divergence,
or Relative Entropy**



$$\mathcal{L}(\tilde{n}_1, \dots, \tilde{n}_k) = \prod_{j=1}^k \tilde{p}_j^{\tilde{n}_j}$$

$$\max_{\tilde{p}} \log \mathcal{L}(\tilde{n}_1, \dots, \tilde{n}_k) = N \sum_{j=1}^k \frac{\tilde{n}_j}{N} \log \frac{\tilde{n}_j}{N}$$

$$\sum_{\vec{n}} e^{-ND(\frac{\vec{n}}{N} \parallel \vec{p})} ND(\vec{p} \parallel \tilde{p}(\vec{n}/N)) \approx ND(\vec{p} \parallel \tilde{p}(\vec{p})) + \sum_{\vec{n}} e^{-ND(\frac{\vec{n}}{N} \parallel \vec{p})} \frac{N}{2} \sum_{j=1}^k \frac{(\tilde{p}(\vec{n}/N) - \tilde{p}(\vec{p}))^2}{\tilde{p}_i(\vec{p})}$$

**Sample-mean KL-divergence
of model from reality**

$$= -\log(\mathcal{L}) + \frac{k}{2}$$

Word lists are the starting point for lexical (= phonological / semantic) reconstruction

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Turkic etymology :

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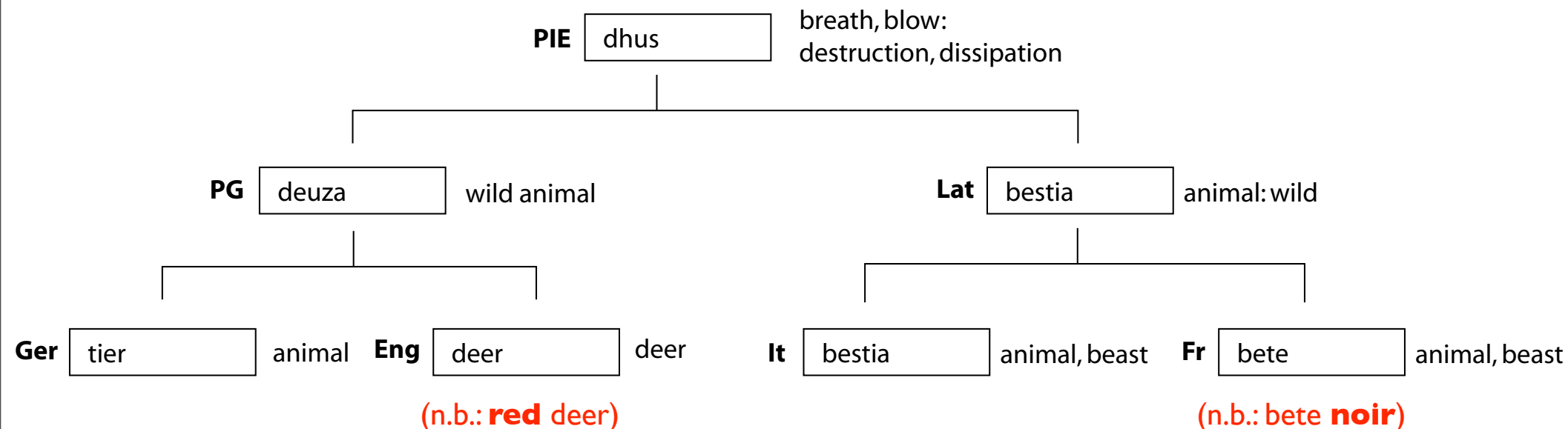
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*ab- +	Altaic etymology +	to crowd, come together	собираться, встречаться	av- (OUygh.)	av- (MK, KB)								
*abuč +	Altaic etymology +	handful	пригоршня		avut (MK), avut-ča, avuč-ča (KB), avuč (Tefs.)	avuč	uč	avuč (MA, Sangl, Бор. Бад.)	хавуш	oč	oš	ovuč	ovu jan-
*Abuč-ka +	Altaic etymology +	1 husband, old man 2 foster- mother 3 elder sister 4 uncle	1 муж, старик 2 кормилица 3 старшая сестра 4 дядя	avičya, abučya 1, abučqa 2 (OUygh.)	avičya 1 (MK, KB)	abus 3 dial.	abusqa, awucqa 1 dial. (Sib.)	abusqa, avušqa 4 (Abush, Sangl.)					

Objects that must be modeled are joint histories of sound and meaning for a collection of words

- n.b., word forms are attested; meanings are indirectly inferred, and often ambiguous
- easy to trace a form; but inadequate to infer history from forms alone

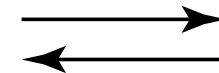


Representing sound and meaning “innovation” in the comparative method (Bill’s lecture)

- Suppose that some stable meaning categories can be identified
- Identify primary words for each meaning
- Try to exclude “borrowed” terms; suppose that what is left has been transmitted through vertical descent
- Identify systematic sound relations and try to infer historical sound changes
- Associate semantic innovations with in-language substitutions within meaning categories

einz	one
zwei	two
drei	three
vier	four
funf	five
...	...
tier	animal
reh	deer
hund	dog
vater	father
mutter	mother
milch	milk
finger	finger
arm	arm
bein	leg
...	...

Sound
Map



Preserved meanings suggest sound maps

PIE	Hoi-(wo, ko, no)
	duoh
	trei
	k ^w etuor
	finfi

(Numbers give an example in which we can treat primary meanings as language-universal and historically relatively stable)

PG	ainaz
	twai
	δrjiz
	fidwor
	finfi

(Innovation)



(Sound similarity)

Use preservation of meaning to infer regular relations of sounds: here, e.g., thr <> tr

Lat	unus
	duo
	tres
	quattuor
	quinque



(Sound similarity)

Ger	einz
	zwei
	drei
	vier
	funf



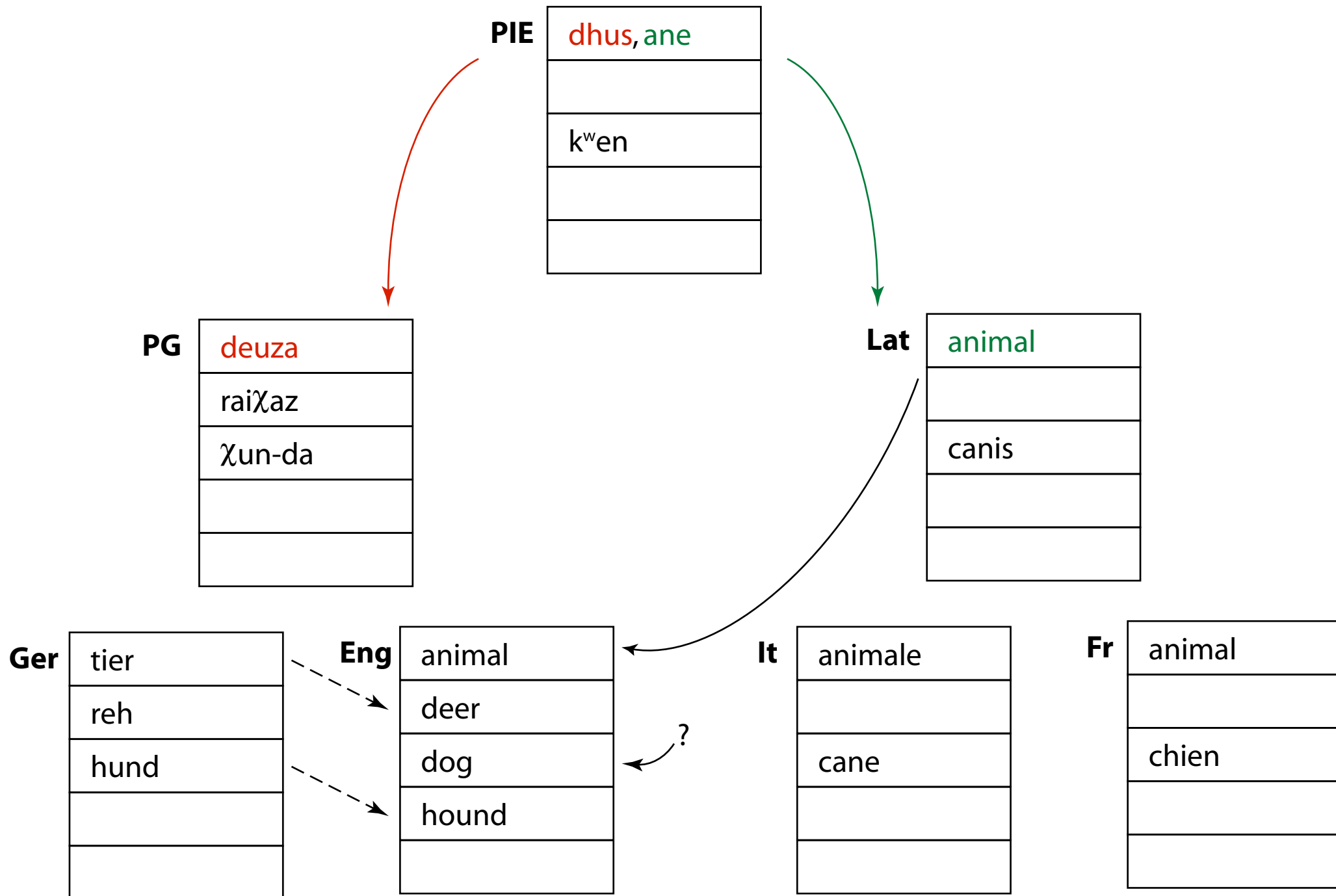
Eng	one
	two
	three
	four
	five



It	uno
	due
	tre
	quattro
	cinque

Fr	un
	duex
	trios
	quatre
	cinque

Sound maps help identify meaning shifts



The “alignment problem”: what to compare w/ what?

Etymology 4 “belly”

q	q	k	q	q	q	q	q	G	G	x	q	q	q	x	x		x	x	q	q	q	q	q	q	q	q	q	q	q	q			
a	a	a	a	a	o	e	a	a	a	a	a	a	$\bar{a}$	i	a		i	i	a	a	a	a	a	a	a	a	a	a	a	a			
r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r		r	r	r	r	r	r	r	r	r	r	r	r	r	r			
i	i	i	i	i	i	i	i	i	i	i		i	i	ɤ	i		i	i	i	i	i	i	i	i	i	i	i	i	i	i			
n	n	n	n	n	n	n	n	n	n	n	n	n	n	m	n		n	n	n	n	n	n	n	n	n	n	n	n	n	n			
																i																	

Etymology 5 “big, high”

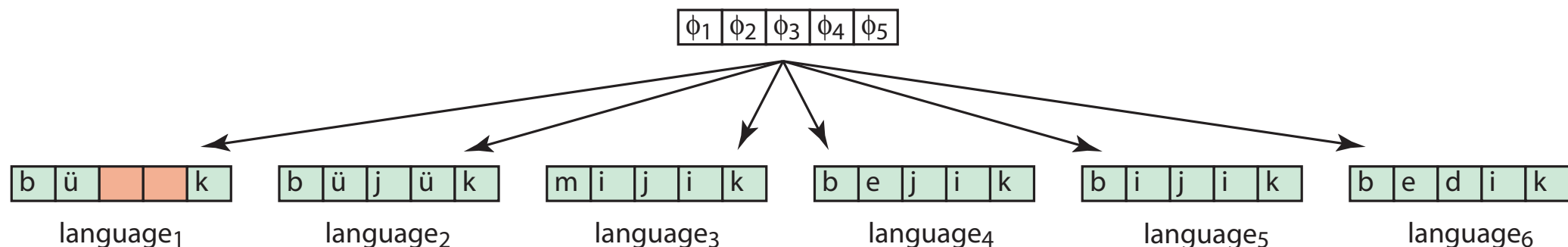
[illegible]

Etymology 12: “Breast, nipple”

m	m		m	m	m		m	m		m	m	m
e	ε		ä	ä	ā		ā	ē		ä	ä	ä
m	m		m	m	m		m	m		m	m	m
												m
e	i		ä	ä	e		ä	ē		ä	ä	ä
							k			j	j	

Maximum-likelihood estimation of history and process (phonological only, here)

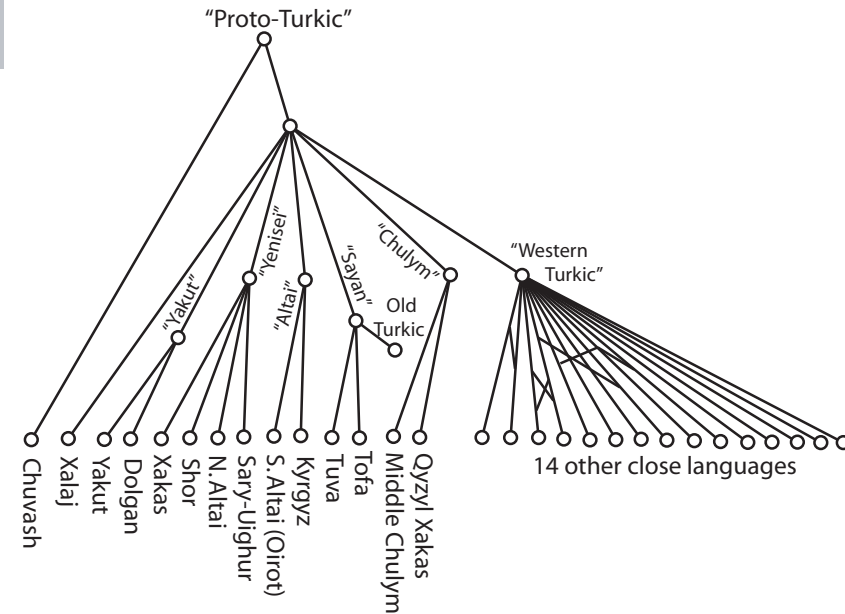
- Suppose we have proposed an alignment of positions in the daughter languages
- Propose phoneme assignments to aligned positions in the ancestor (with probabilities)
- Estimate regular correspondence of ancestor to daughter phonemes (w/ or w/o probabilities)
- Estimate random violations (with probabilities)



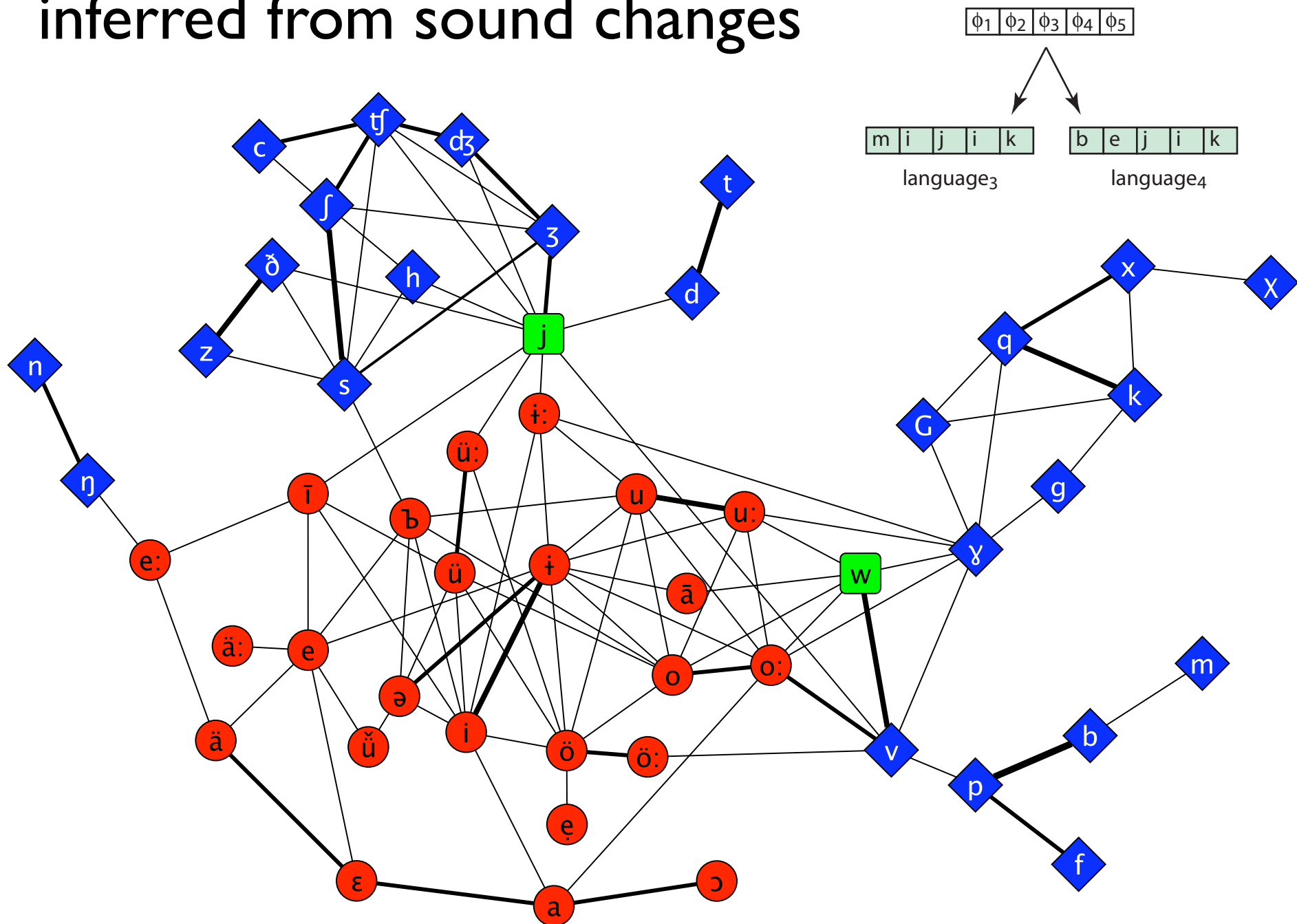
Sound correspondences among the languages

ancestor	prob	ATU	KRH	JAK	DOLG	TUV	TOF	HAK	SHR	ALT	KRG	UIG	UZB	KAZ	KLPX	NOGX	BAS	TAT	QUM	BLKX	KRMX	TRM	AZB	GAGX	TRK	KHAL	CHV
97	0.097	a	a	a	a	a	a	a	a	a	a	a	ɔ	a	a	a	a	a	a	a	a	a	a	a	a	a	o
616	0.042	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	i	ə
101	0.042	e	e	e	e	e	e	i	e	e	e	ä	e	e	e	e	i	i	e	e	e	e	ä	e	e	ä	ь
117	0.041	u	u	u	u	u	u	u	u	u	u	u	u	u	u	u	o	o	u	u	u	u	u	u	u	u	ь
105	0.029	i	i	i	i	i	i	ə	i	i	i	i	i	i	i	i	e	e	i	i	i	i	i	i	i	i	ə
61948	0.026	ü	ü	ü	ü	ü	ü	ü	ü	ü	ü	ü	u	ü	ü	ü	ö	ö	ü	ü	ü	ü	ü	ü	ü	i	ə ^w
111	0.018	o	o	o	o	o	o	o	o	o	o	u	o	o	o	o	u	u	o	o	o	o	o	o	o	o	ь
61942	0.016	ö	ö	ö	ö	ö	ö	ö	ö	ö	ö	ö	u	ö	ö	ö	ü	ü	ö	ö	ö	ö	ö	ö	ö	e	ь
113	0.058	q	q	x	k	q	q	x	q	q	q	q	q	q	q	q	q	q	q	q	q	G	G	q	k	q	x
106	0.048	j	j	s	h	č	č	č	č	j	ž	j	j	ž	ž	j	j	j	j	j	j	j	j	j	j	j	s
116	0.044	t	t	t	t	d	d	t	t	t	t	t	t	t	t	t	t	t	t	t	t	d	d	d	d	t	t
114	0.043	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r	r
108	0.032	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	l	
107	0.031	k	k	k	k	k	x	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k	k
98	0.023	b	b	b	b	b	b	p	p	b	b	b	b	b	b	b	b	b	b	b	b	b	b	b	b	b	p
110	0.021	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n	n
61850	0.019	š	š	s	s	š	š	s	š	š	š	š	š	s	s	s	š	š	š	š	š	š	š	š	š	š	l
109	0.019	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m	m
122	0.018	z	z	s	s	s	s	s	s	s	z	z	z	z	z	z	δ	z	z	z	z	z	z	z	z	z	r
8240	0.017	č	č	s	s	š	š	s	š	č	č	č	č	š	š	š	s	č	č	č	č	č	č	č	č	č	s
611	0.016	ɣ	ɣ	0	0	ɣ	ɣ	ɣ	ɣ	0	ō	ɣ	ɣ	w	w	w	w	w	w	w	ɣ	G	ɣ	0	ɣ	ɣ	v
115	0.015	s	s	0	0	s	s	s	s	s	s	s	s	s	s	s	s	h	s	s	s	s	s	s	s	s	s
103	0.012	g	g	ɣ	g	g	g	g	ɣ	ɣ	g	g	k	g	k	k	g	g	k	g	g	g	g	g	g	g	g
112	0.01	p	p	b	b	v	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p	p
62111	0.009	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	ŋ	n	ŋ	n	n	n	ŋ	n
118	0.008	b	v	b	s	g	g	v	b	v	j	v	v	j	j	j	j	j	v	j	j	v	v	v	v	v	v

SA Starostin, AV Dybo and OA Mudrak 2003. An Etymological Dictionary of Altaic Languages. Leiden: Brill



Typology I: sound relations and features inferred from sound changes



Context dependence: an Artificial Intelligence problem

Split of Old English /k/

Stage I	katt	keaff	kinn
Stage II	katt	tʃeaff	tʃinn
Stage III	katt	tʃaff	tʃinn

Split of Latin /s/

Stage I	ka:ra	flo:s	flo:ses
Stage II	ka:ra	flo:s	flo:zes
Stage III	ka:ra	flo:s	flo:res

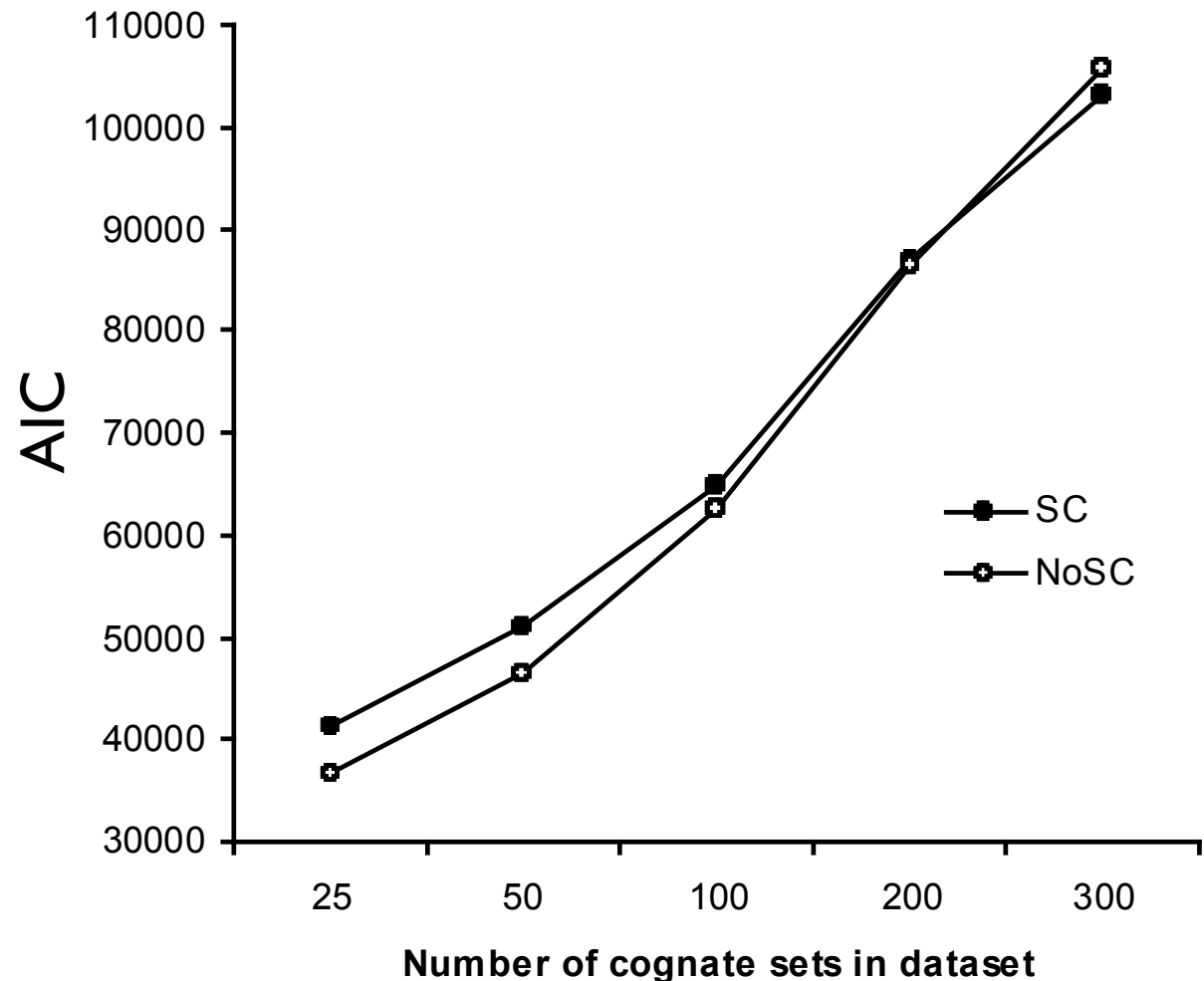
From R.L.Trask,
“Language change”

- Sound change can be regular, but not at single-phoneme level
- Conditioning contexts can be lost; must be guessed
- AIC and BIC can be used to judge guesses

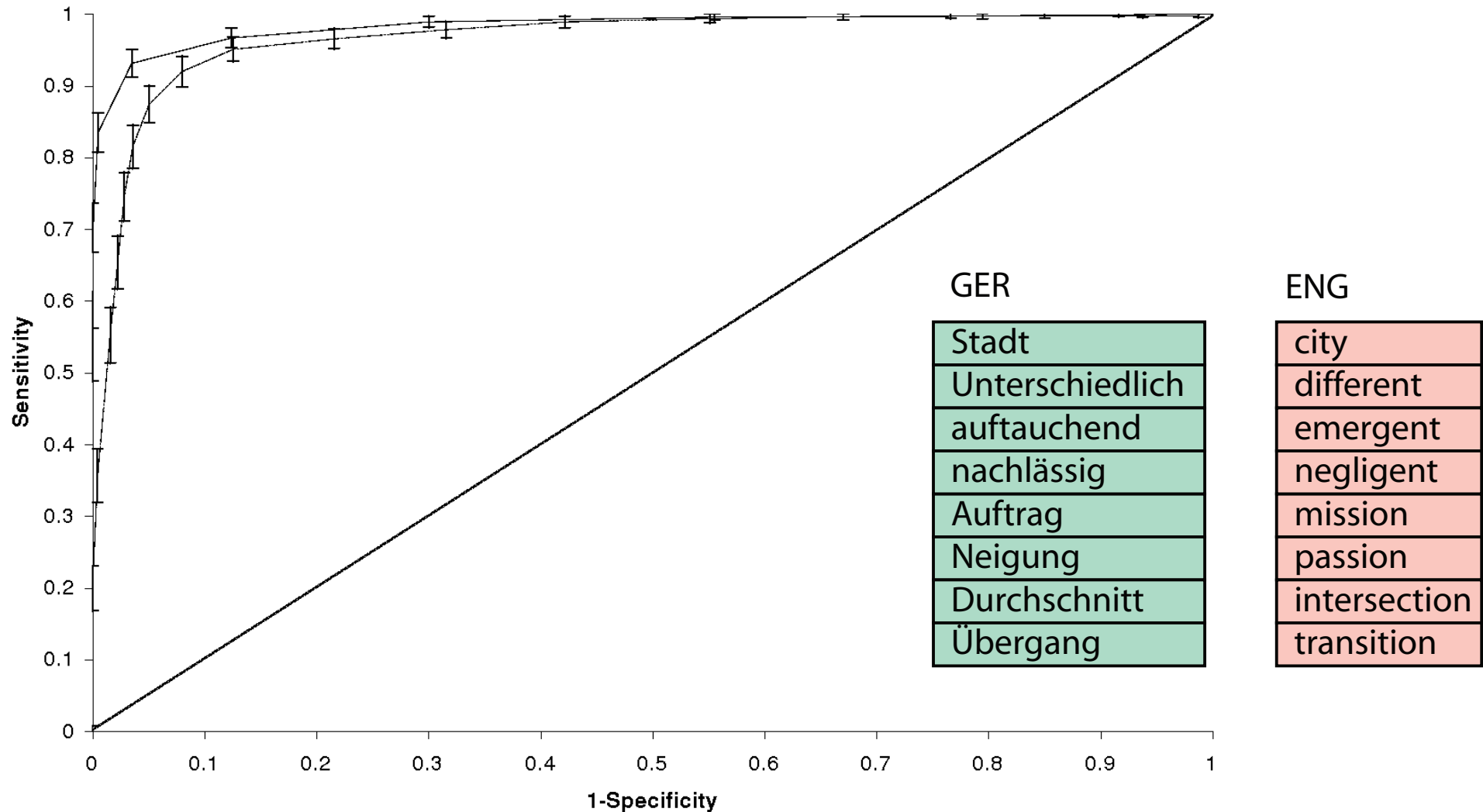
Vowel harmony in the Turkic language family: a predictive supra-segmental context

Front/back agreement
in roots and affixes

nom	a book
inek	a cow
nomnar	books
inekter	cows



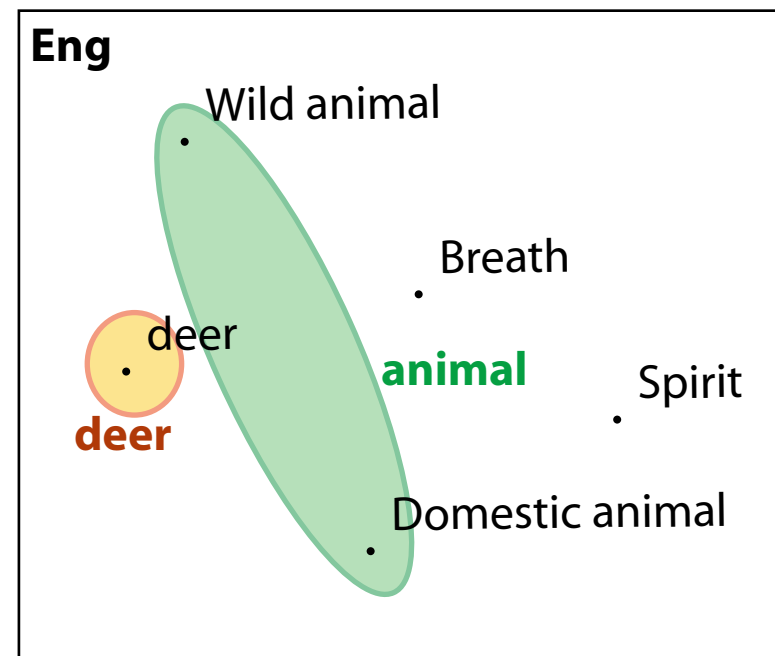
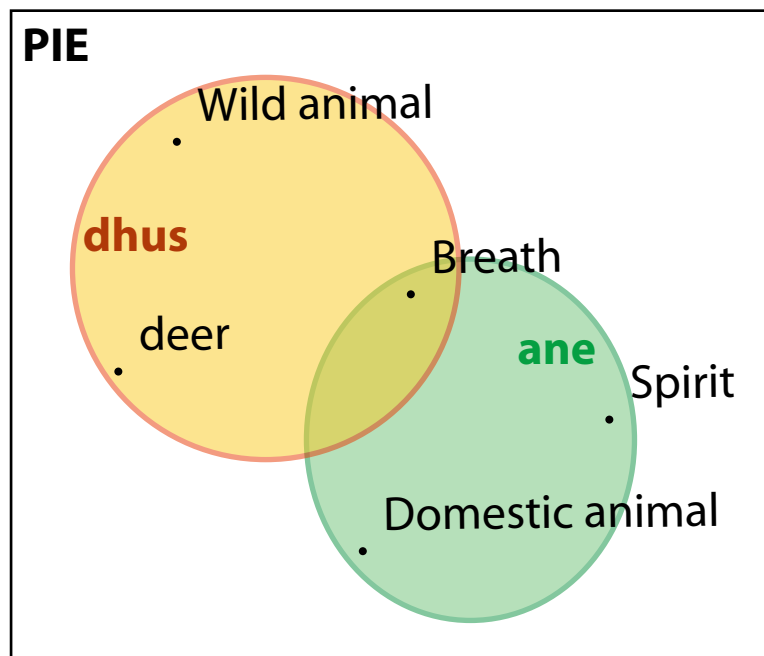
Identification of borrowings: words that do not fit the system pattern



Receiver Operating Characteristic curve

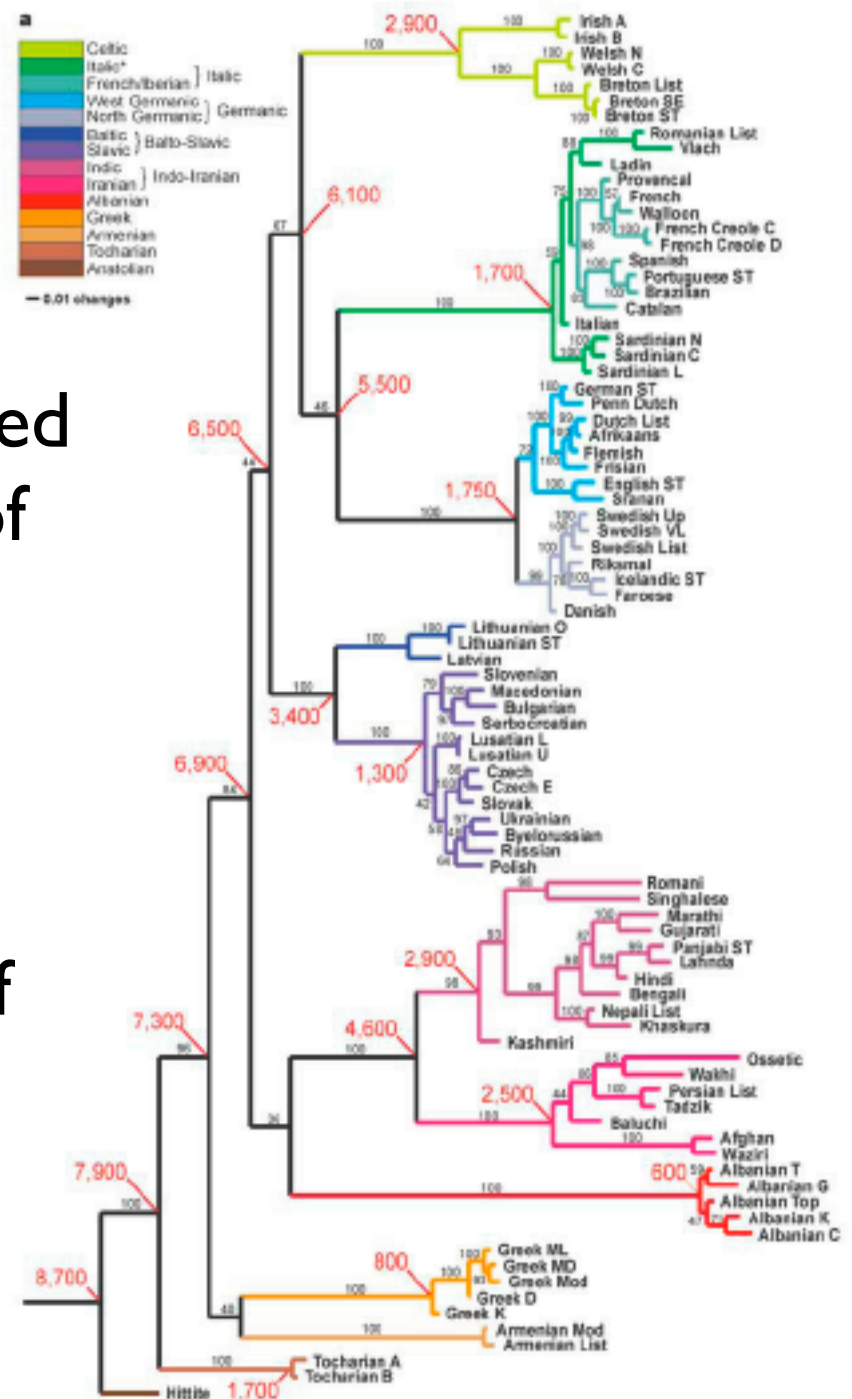
New conceptual domain: mathematical likelihood modeling of semantic shift

- Phonological and semantic constraints interact with polysemy and synonymy to structure sound and meaning change
- Semantic categories, split, join, and move in some “space” which we do not know



Phylogeny and reconstruction

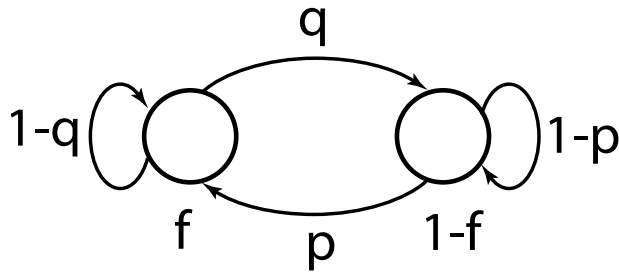
- Modern glottochronology applied to expert linguists' judgments of cognate classifications
- Presence/absence data format modeled after genes
- *Not yet a model of processes of sound and meaning change*



Russell D. Gray & Quentin D. Atkinson

NATURE | VOL 426 | 27 NOVEMBER 2003 | www.nature.com/nature

Maslova: how much can you do with incomplete reconstructions of the past?

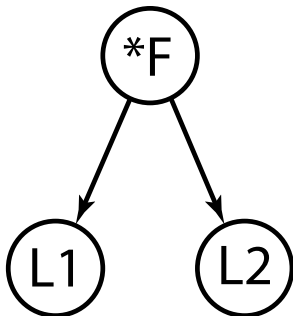


Two quantities: stationary frequency
typical number of pairs

$$\bar{f} = \frac{p}{p + q}$$

$$\bar{h} = (p + q)^2 [2 - (p + q)] 2\bar{f} (1 - \bar{f})$$

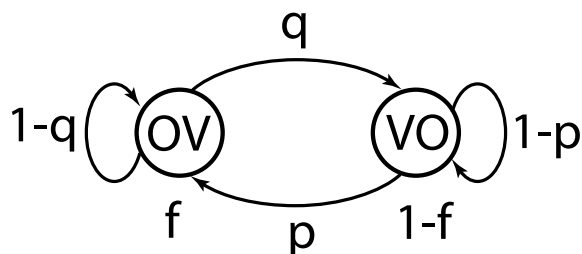
Regression model for observed frequencies estimate (p/q): $f_i = \bar{f} + \epsilon_i$



Fit of number of pairs against mean,
in children of a common family ancestor:
put bounds on (p+q), p/q

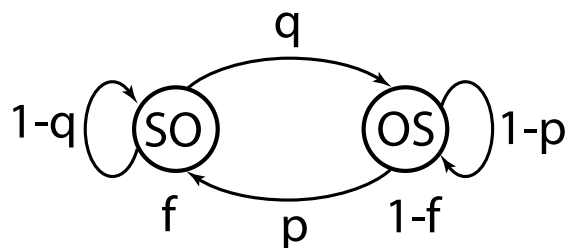
$$h_i - \bar{h} = (f_i - \bar{f}) 2 (p + q) (1 - 2\bar{f}) + \epsilon_i$$

Three partitions of standard word order



$$f(OV) \approx 0.53$$

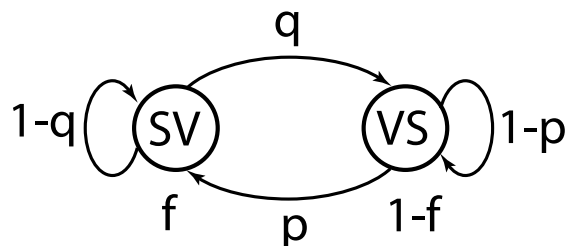
$$\frac{1}{p+q} \approx 24\text{ky}$$



$$f(SO) \approx 0.96$$

$$\frac{1}{p+q} \leq 11\text{ky}$$

$$p/q \geq 15$$



$$f(SV) \approx 0.86$$

$$\frac{1}{p+q} \in (10\text{ky}, 30\text{ky})$$

$$p/q \geq 3$$

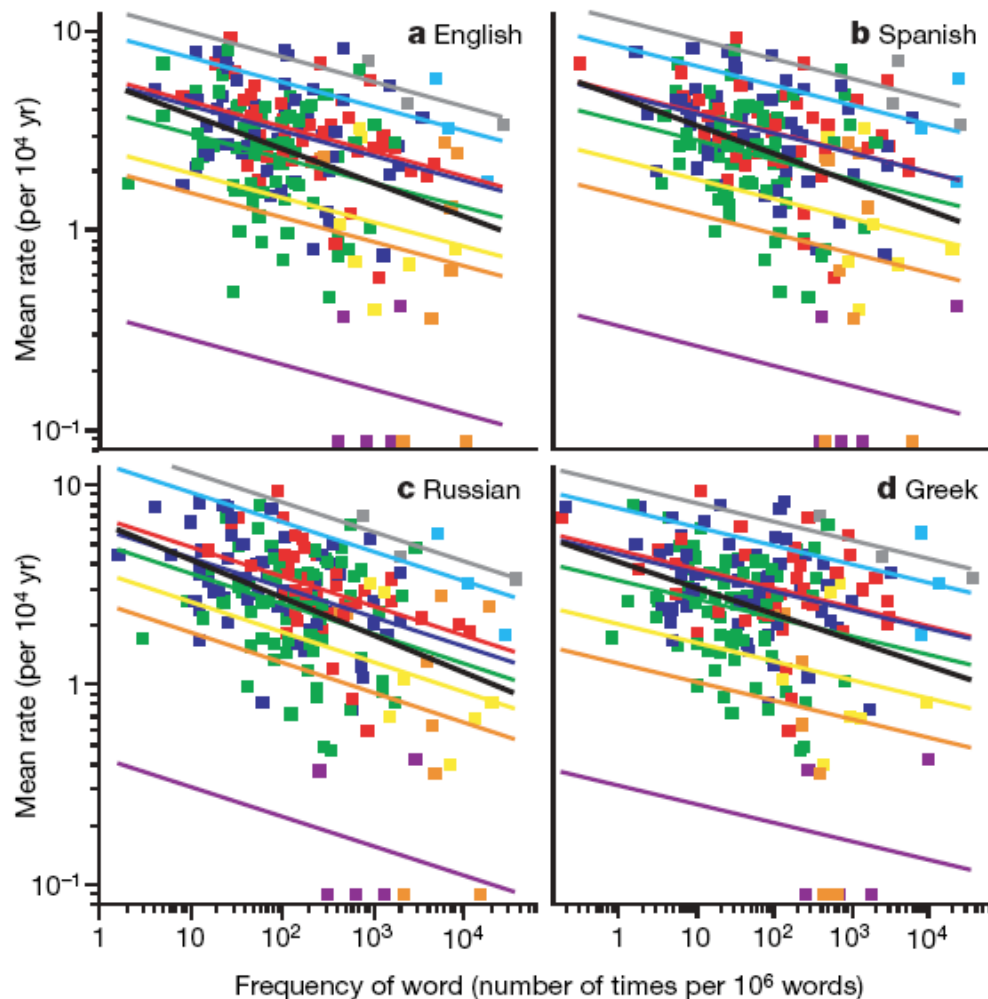
- New opportunities for quantitative characterization of regularities
- Cross-linguistic regularities in frequency of use, and relations to rates of change
- Punctuated equilibrium and correlations of the “clock” of language change with culture
- Polysemy, synonymy, and semantics
- Full speaker-corpus archives (Norquist et al.), formant-based analysis (Labov), ...

Typology II: frequency of use and rates of change

Frequency of word-use predicts rates of lexical evolution throughout Indo-European history

Mark Pagel^{1,2}, Quentin D. Atkinson¹ & Andrew Meade¹

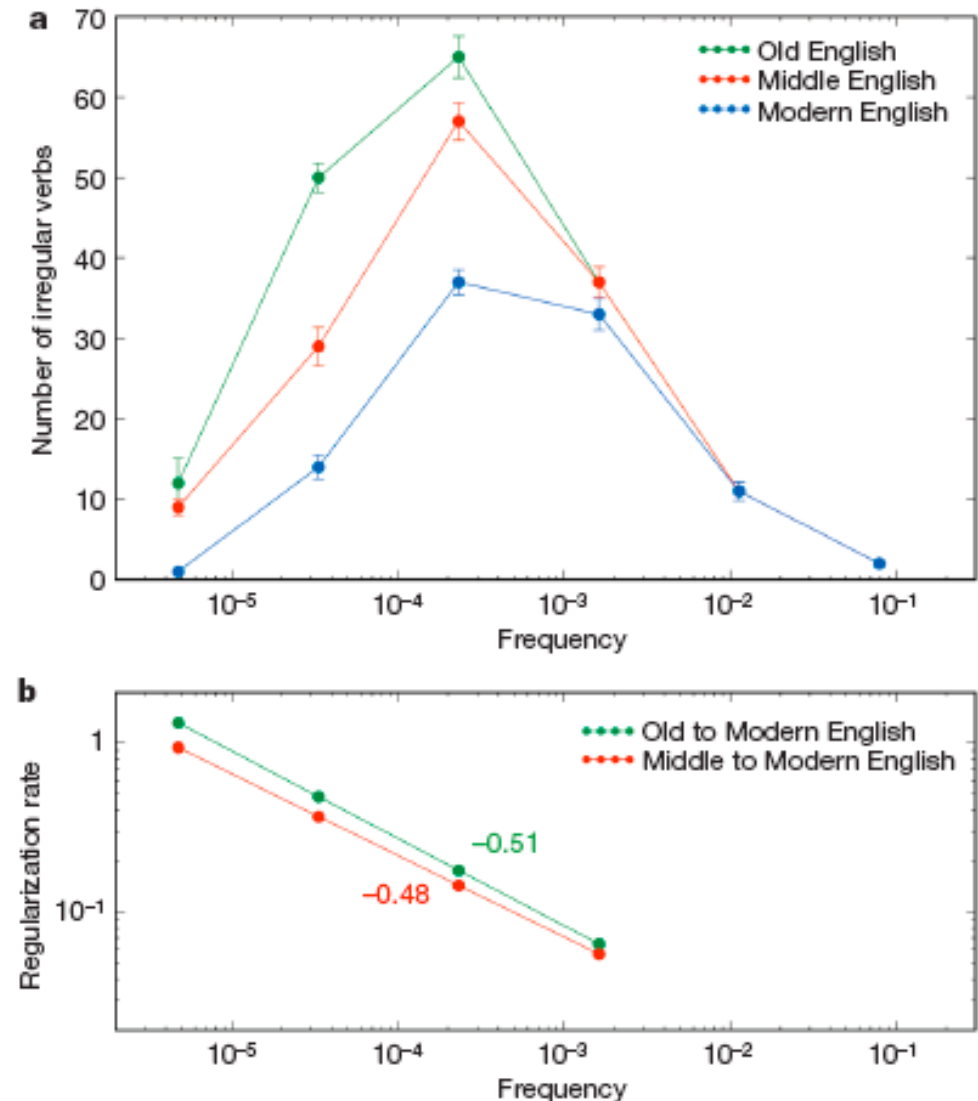
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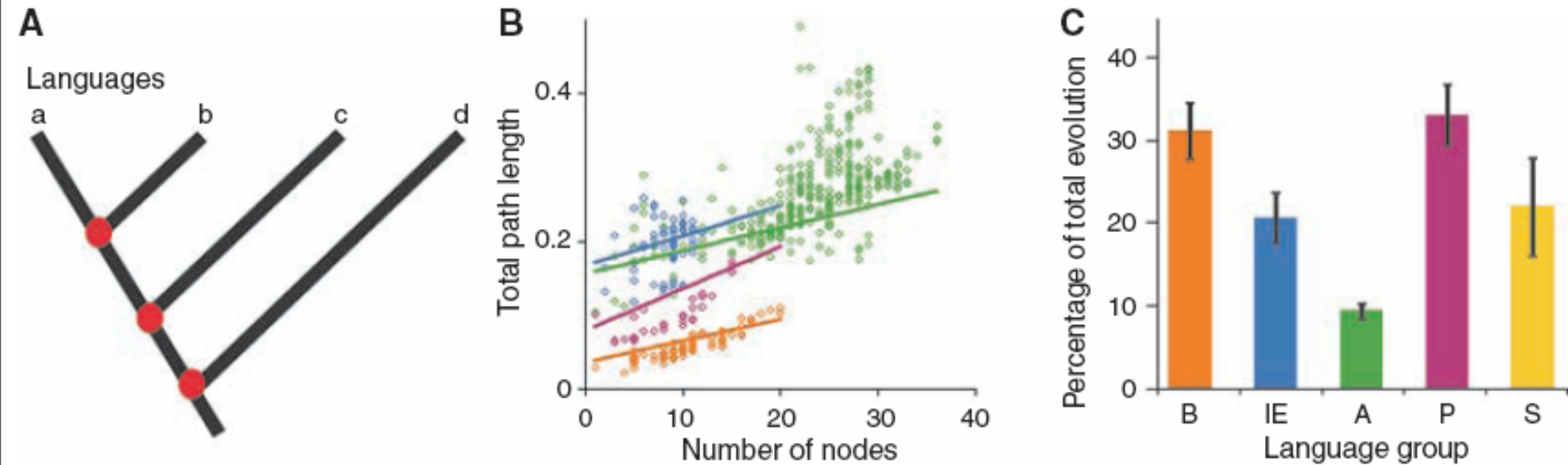
Quantifying the evolutionary dynamics of language

Erez Lieberman^{1,2,3*}, Jean-Baptiste Michel^{1,4*}, Joe Jackson¹, Tina Tang¹ & Martin A. Nowak¹

NATURE | Vol 449 | 11 October 2007



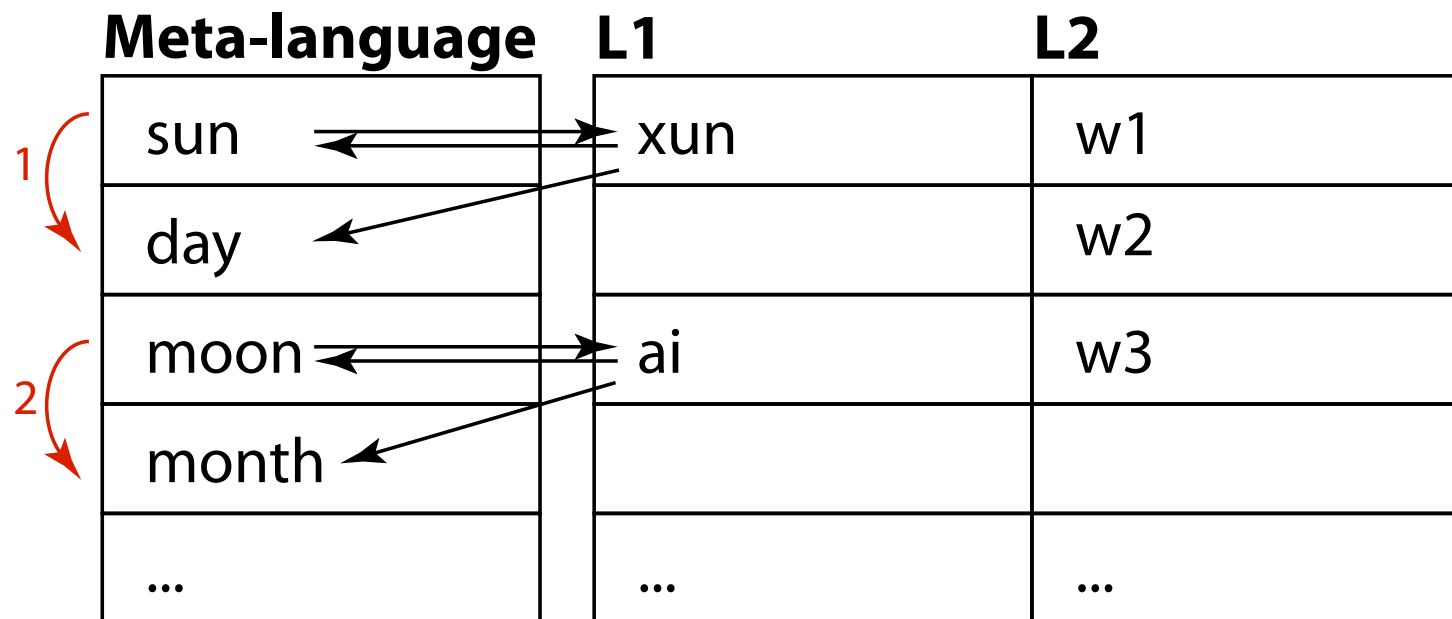
Linguistic punctuated equilibrium: do cultural phenomena like splitting drive language divergence?



Languages Evolve in Punctuational Bursts

Quentin D. Atkinson,^{1*} Andrew Meade,¹ Chris Venditti,¹ Simon J. Greenhill,² Mark Pagel^{1,3†}

Toward a likelihood model of semantic shift: Inferring polysemy with English as a meta-language

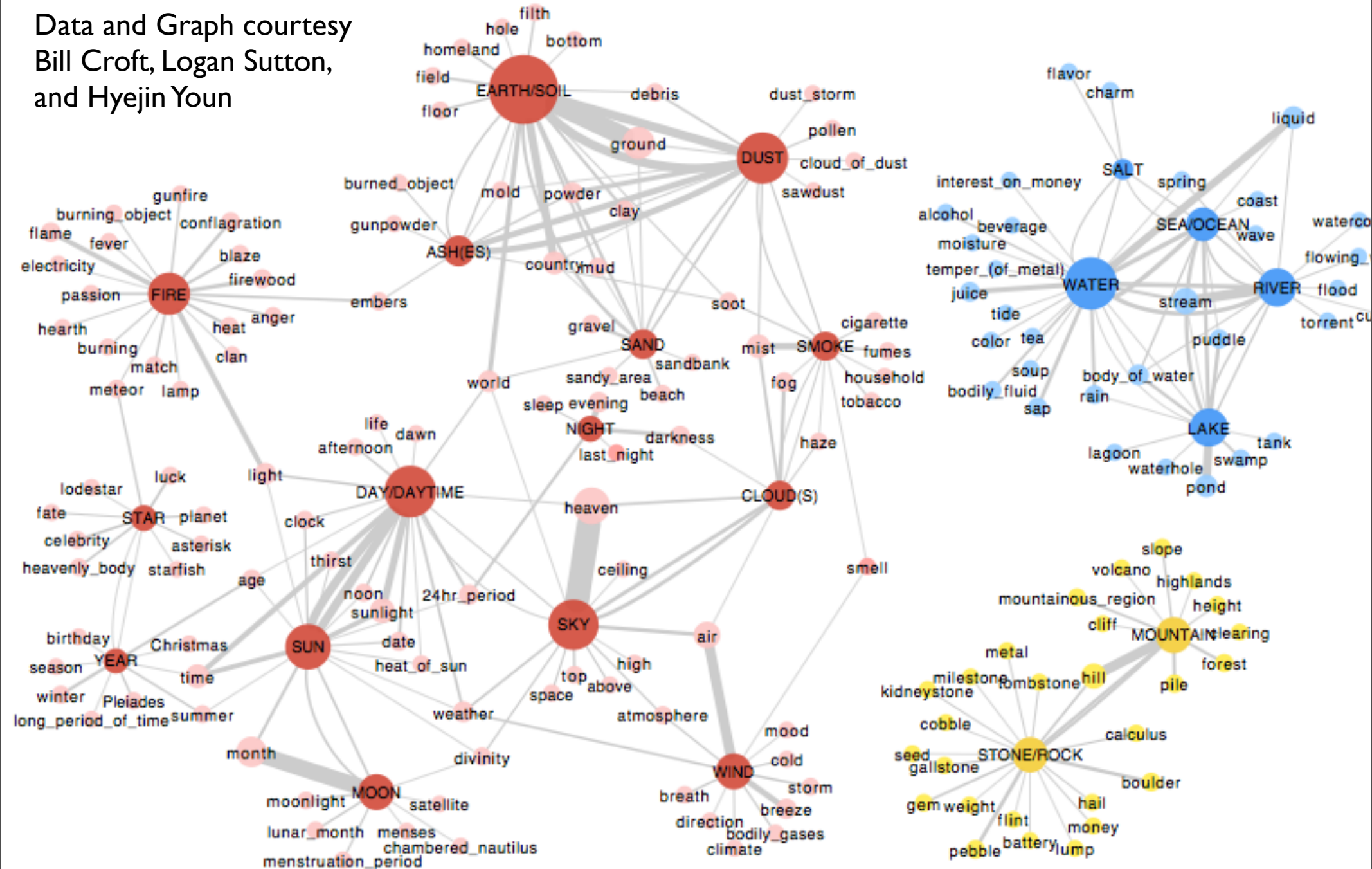


Sun
1
Day

Moon
2
Month

Network of polysemes in 81 diverse languages

Data and Graph courtesy
Bill Croft, Logan Sutton,
and Hyejin Youn



Summary comments

- Much linguistics traditionally modeled on logic;
Can we root historical linguistics in probability?
- Language evolution is *not* molecular evolution;
Same principles lead to different models
- New and refined quantitative signatures: Both methodological and conceptual opportunities