Machine Learning and Artificial Intelligence: Part 1

An introduction to core concepts

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What is machine learning?

- The science of building computer models that:
 - $\circ\,$ Learn from data how to perform a task
 - $\,\circ\,$ Self-tune their parameters to optimize performance
 - Generalize behavior to new/unseen data
- The primary goal of ML is to provide <u>solutions to practical</u> <u>real-world problems</u>:
 - $\circ\,$ Inspiration from biology is welcome but not required
 - $\,\circ\,$ Explaining nature is a plus but not a must

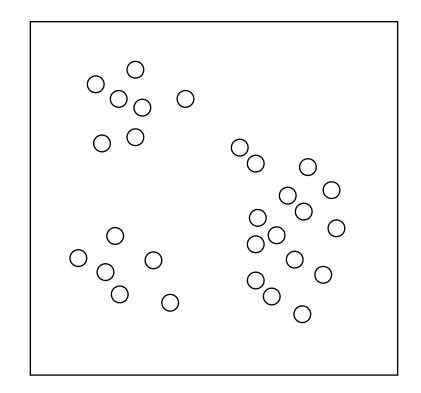
Types of learning

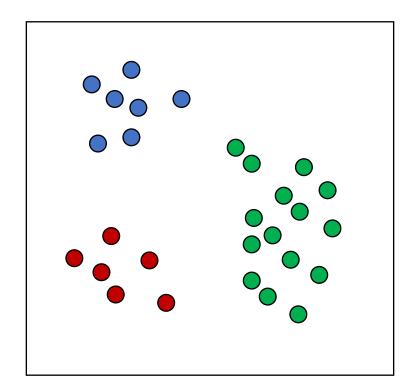
- <u>Unsupervised learning</u>:
 - Training data is unlabeled. The model searches for a compact representation of the inherent structure in the data.
- <u>Supervised learning</u>:
 - Training data is labeled. The goal is to create a compact mapping between the input features and the target.
- <u>Reinforcement learning</u>:
 - Interactive learning where training data (labeled and unlabeled) is obtained by interacting with an environment.

Types of machine learning problems

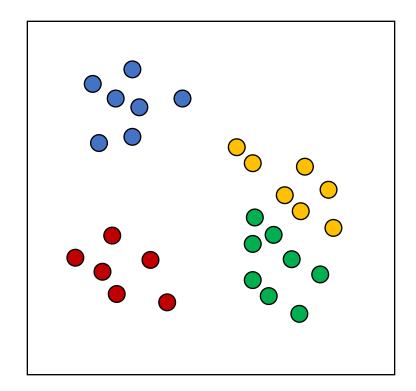
<u>Clustering</u>

- Finding inherent groups in the data (unsupervised)
- <u>Classification</u>
 - Predict the (discrete) class of each data point (supervised)
- <u>Regression</u>
 - Predict a continuous, real-valued variable (supervised)
- <u>Dimensionality reduction</u>
 - Represent the data using a reduced number of variables (unsupervised)

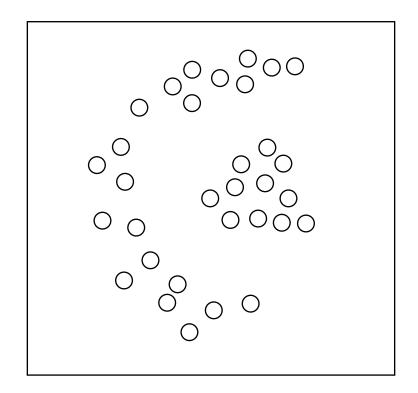




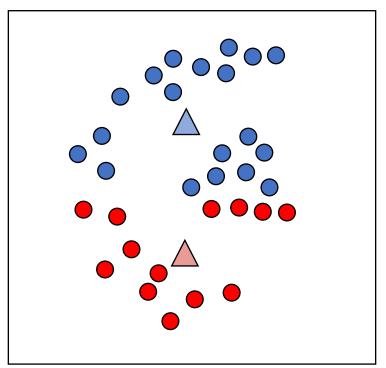
3 clusters



4 clusters

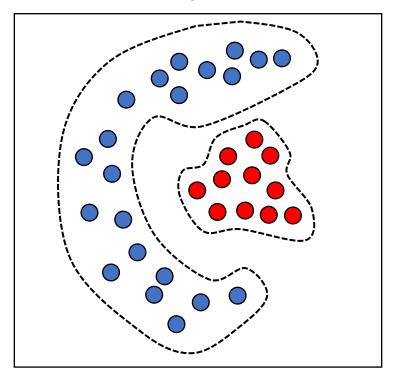


Centroid-based

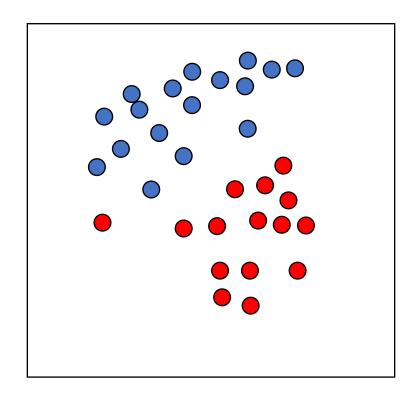


2 clusters

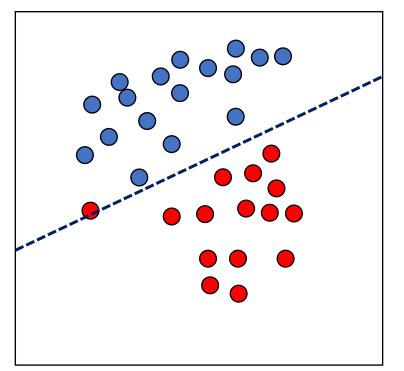
Density-based

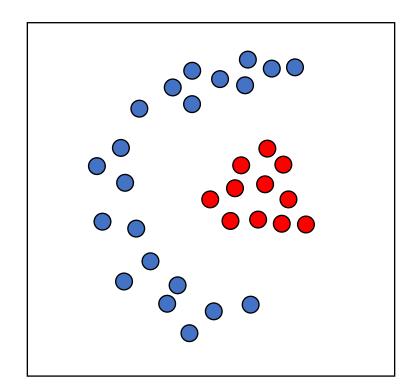


2 clusters

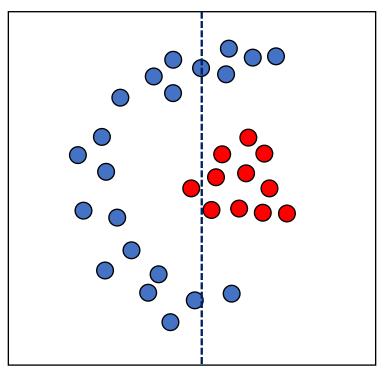


Linear classification

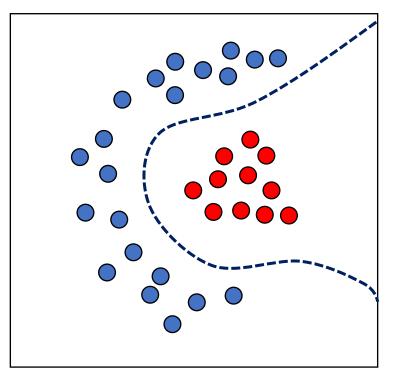


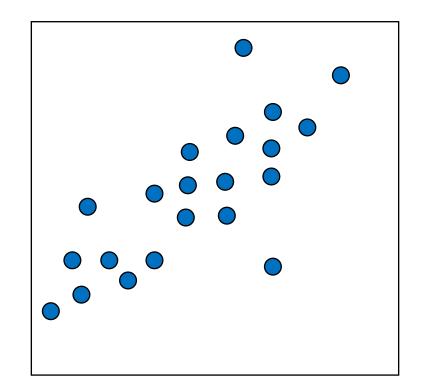


Linear classification

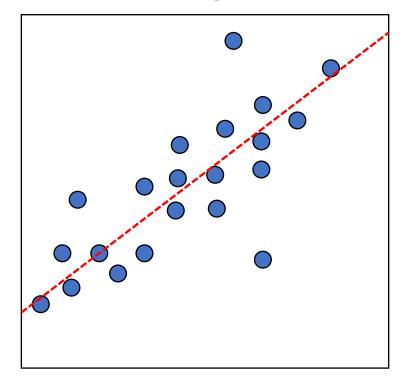


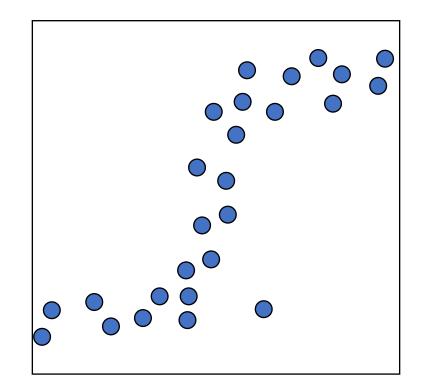
Non-linear classification



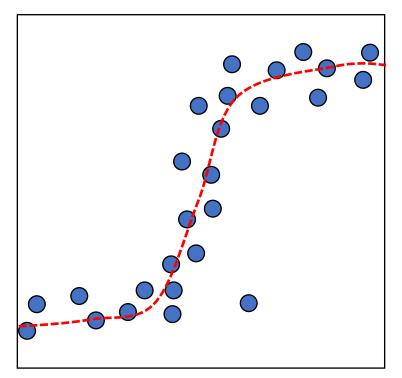


Linear regression

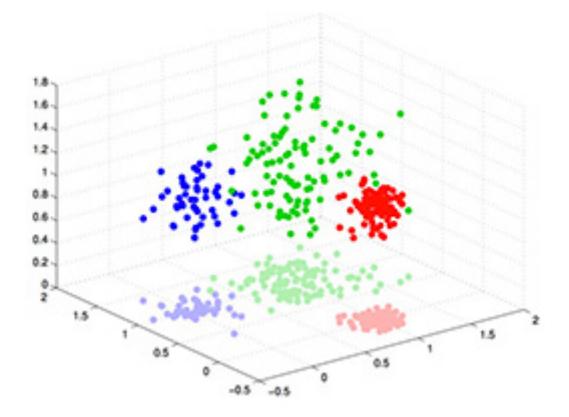




Non-linear regression

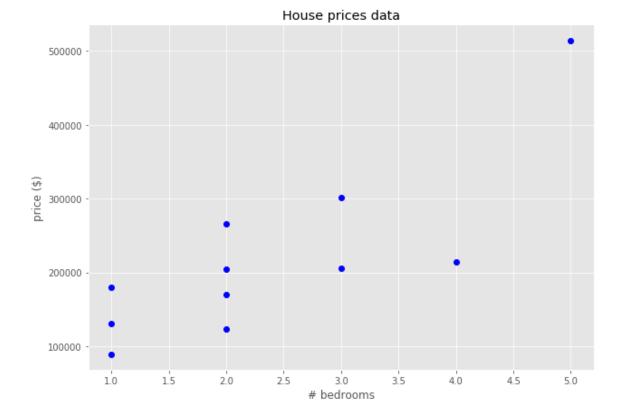


Dimensionality reduction



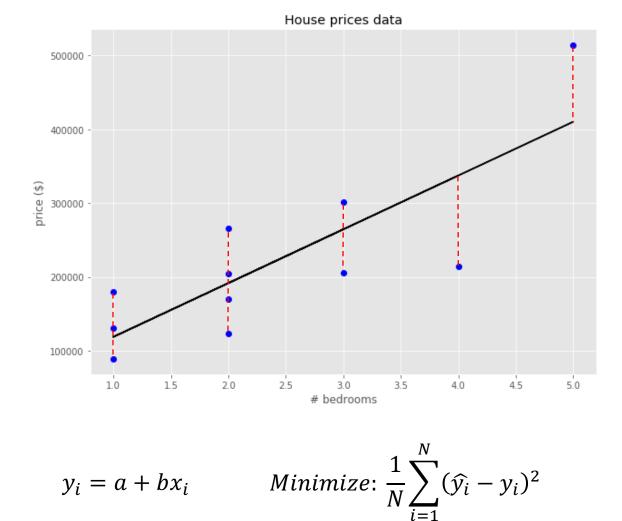
A simple model: Linear regression

# bdrs (x)	price (\hat{y})
1	130k
2	122k
1	89k
3	301k
2	204k
5	514k
2	169k
1	180k
4	213k
2	266k
3	205k

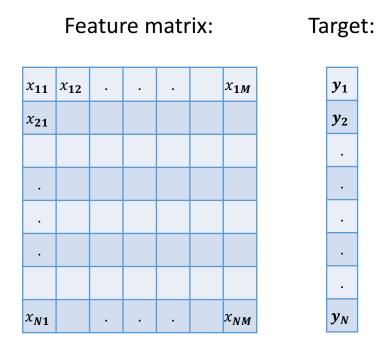


A simple model: Linear regression

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A simple model: Linear regression



M = Number of dimensions (features)N = Number of samples

Model Equation:

$$y_i = \sum_{j=0}^M w_j x_{ij}$$

Loss function (mean squared error):

$$Loss = \frac{1}{N} \sum_{i=1}^{N} (\widehat{y}_i - y_i)^2$$

Logistic regression (classification)

Log-odds transformation:

$$log\left(\frac{p}{1-p}\right) = \sum_{j=0}^{M} w_j x_j$$

Logistic regression (classification)

Log-odds transformation:

Logistic sigmoid

-2

-4

2

6

4

0

-6

Logistic regression (classification)

Log-odds transformation:

Logistic sigmoid

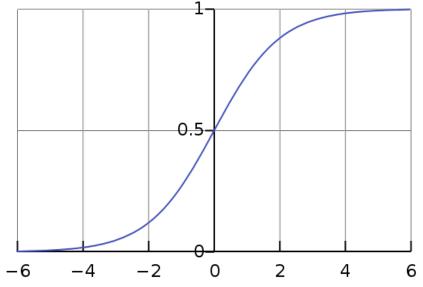
$$log\left(\frac{p}{1-p}\right) = \sum_{j=0}^{M} w_j x_j$$

$$p = \frac{1}{1 + e^{-\left(\sum_{j=0}^{M} w_j x_j\right)}}$$

1

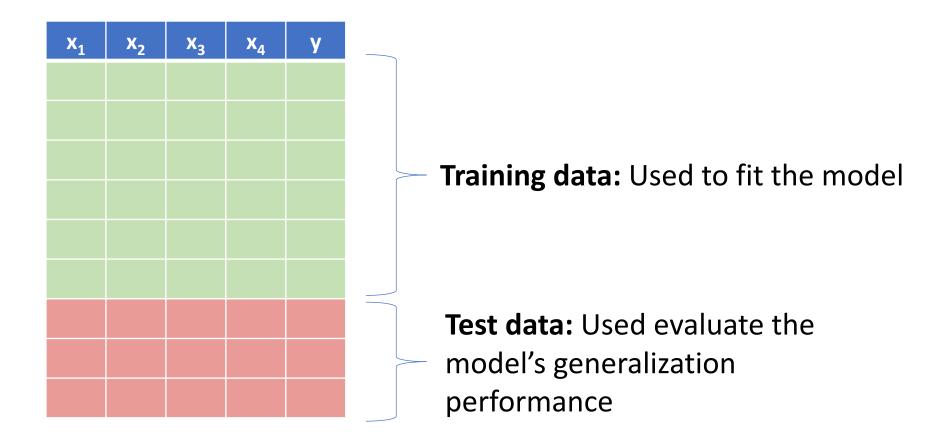
Binary cross-entropy (Log-loss):

$$Loss = -\sum_{i}^{N} \hat{y} \cdot \log p + (1 - \hat{y}) \log(1 - p)$$

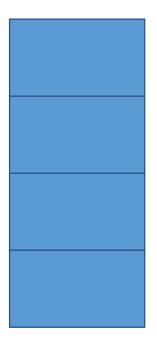


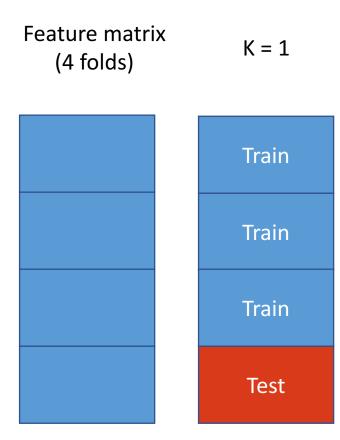
Model validation

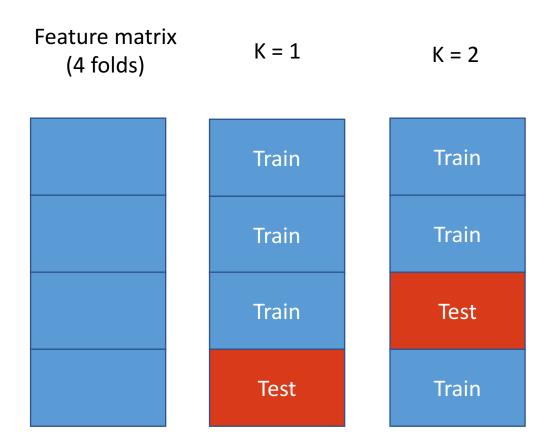
Splitting between training and test data

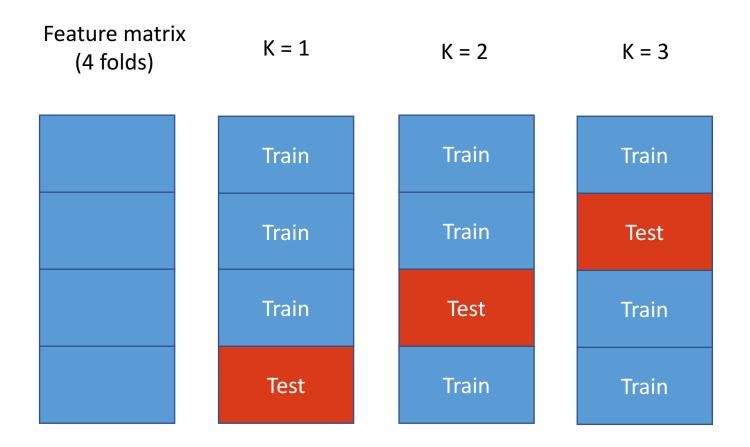


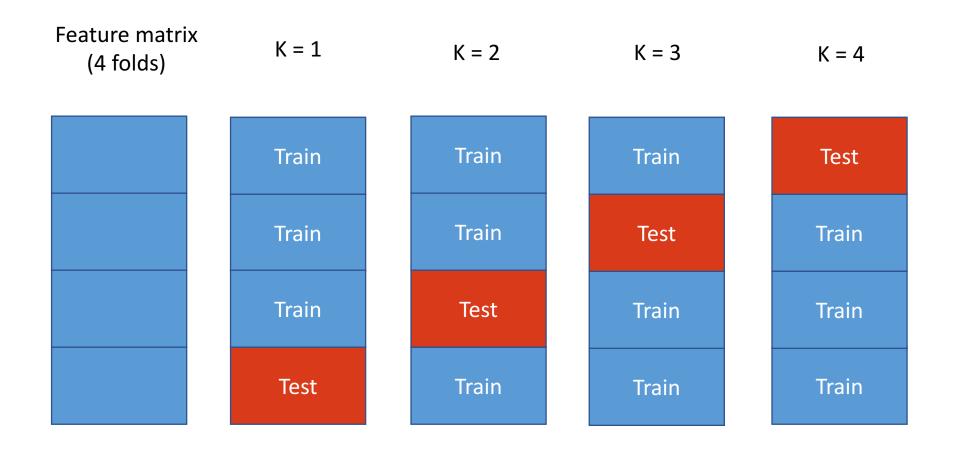
Feature matrix (4 folds)





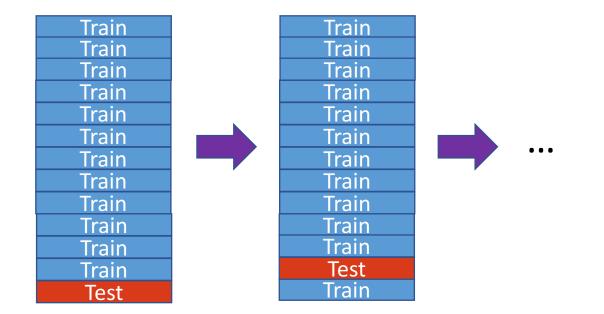






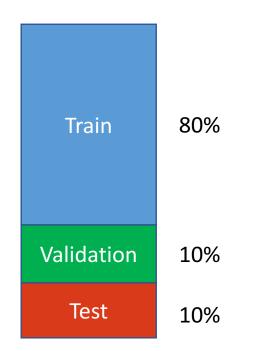
Leave-one-out cross-validation

- Useful when very little data is available
- K = N: Use a single data point for testing; train on the remaining samples in the data set

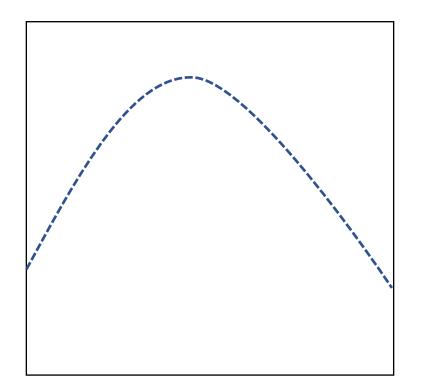


Train-validation-test split

- Sometimes your model takes too long to train or there is plenty of data available.
- Use a fixed split into train, validation, and test sets.

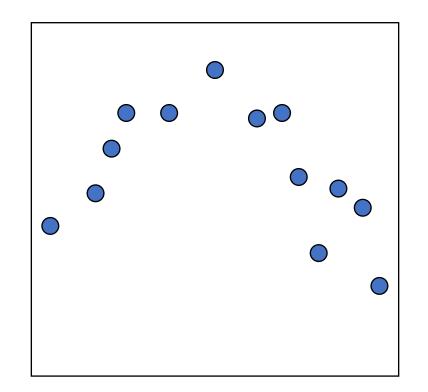


Model selection



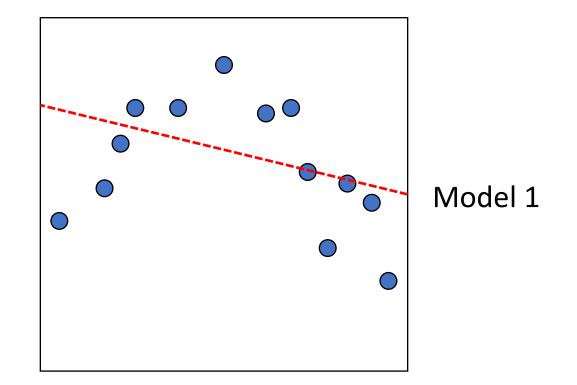
True function: y = f(x)

Model selection



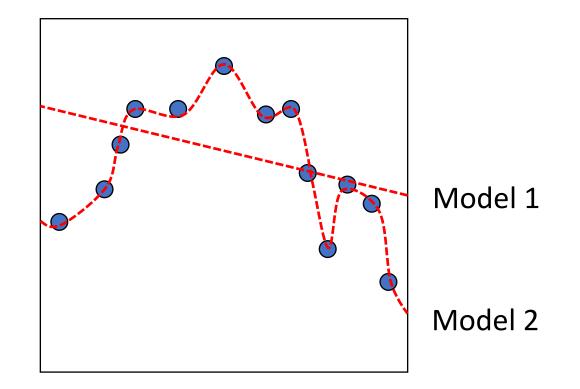
Sample of f(x) with Gaussian noise

Model selection



Linear model approximation of *f*(*x*)

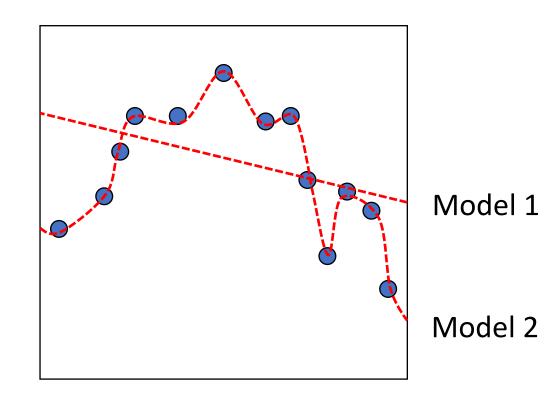
Model selection



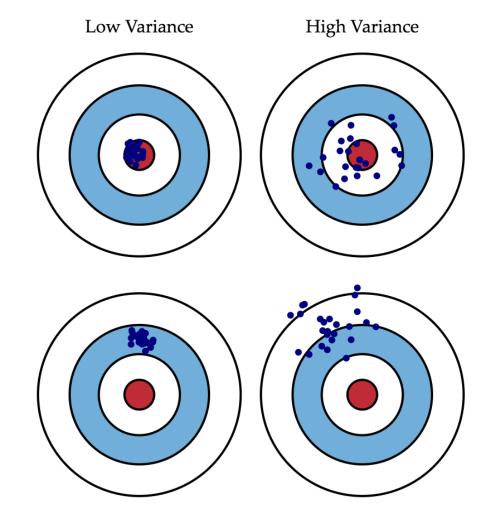
Non-linear model approximation of *f(x)*

Model selection

- Model 1 is overly simplistic. It underfits the data
- Model 2 is overly complex. It over-fits the data.
- Finding the right model is more than just reducing the error.



The bias-variance tradeoff



- Bias is how much the average model prediction differs from the desired value (mean test error).
- Variance is how much the model predictions change with each training data (variance of test error).

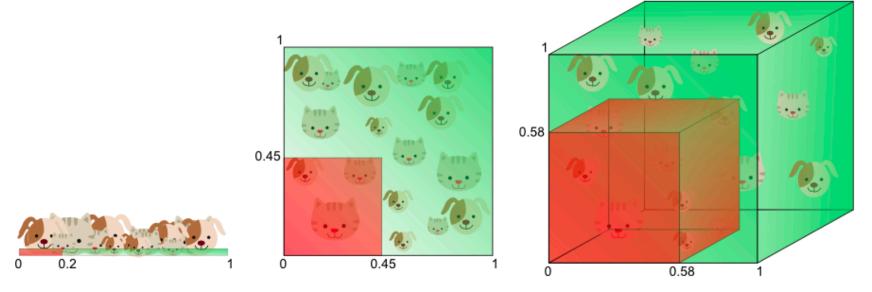
Low Bias

High Bias

⁽Image from "Understanding the Bias-Variance Tradeoff", by Scott Fortmann-Roe.)

The curse of dimensionality

- In order to maintain the same density, the number of data samples must grow exponentially with the number of dimensions in the feature space.
- When data is sparse, models tend to overfit.



(Image from http://www.visiondummy.com/2014/04/curse-dimensionality-affect-classification/)

Regularization

- Penalty to model complexity that reduces the model's flexibility and improves generalization.
- Complexity = Tunable variables in the model.

L1 and L2 norms

• L2 norm:
$$||w||_2 = \sum_{j}^{M} w_j^2$$

• Gaussian prior on the weight distribution

• L1 norm:
$$||w||_1 = \sum_{j}^{M} |w_j|_1$$

- Laplace prior on the weight distribution
- Generates sparse solutions
- Useful in supervised feature selection

Regularized linear regression

• Ridge regression (L2):

$$Loss = \frac{1}{N} \sum_{i=1}^{N} (\hat{y}_i - y_i)^2 + \gamma \sum_{j=1}^{M} w_j^2$$

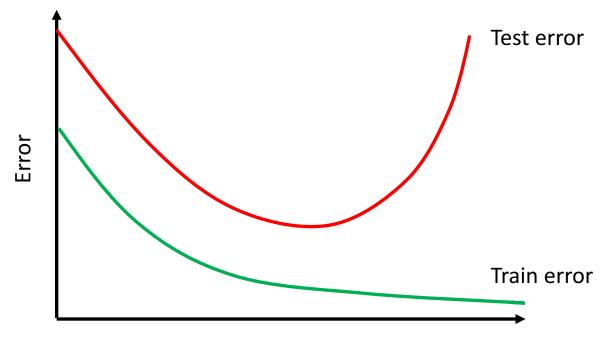
• Lasso regression (L1):

$$Loss = \frac{1}{N} \sum_{i=1}^{N} (\hat{y}_i - y_i)^2 + \lambda \sum_{j=1}^{M} |w_j|^2$$

• Elastic-net (L1 + L2):

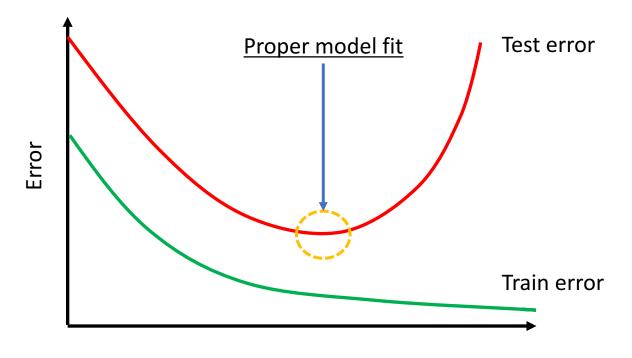
$$Loss = \frac{1}{N} \sum_{i=1}^{N} (\hat{y}_i - y_i)^2 + \lambda \sum_{j=1}^{M} |w_j| + \gamma \sum_{j=1}^{M} |w_j|^2$$

Hyper-parameter tuning



Model complexity

Hyper-parameter tuning



Model complexity

Model complexity

Statistical distributions

Hypothesis testing

Linear regression

Logistic regression

Decision trees

K-means clustering

Random forests

Performance



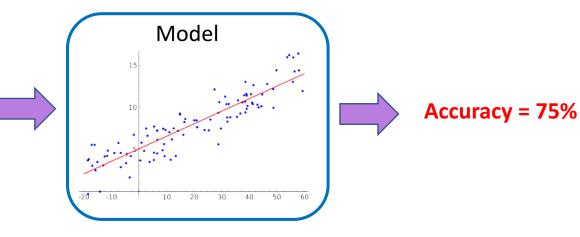
Etolainability

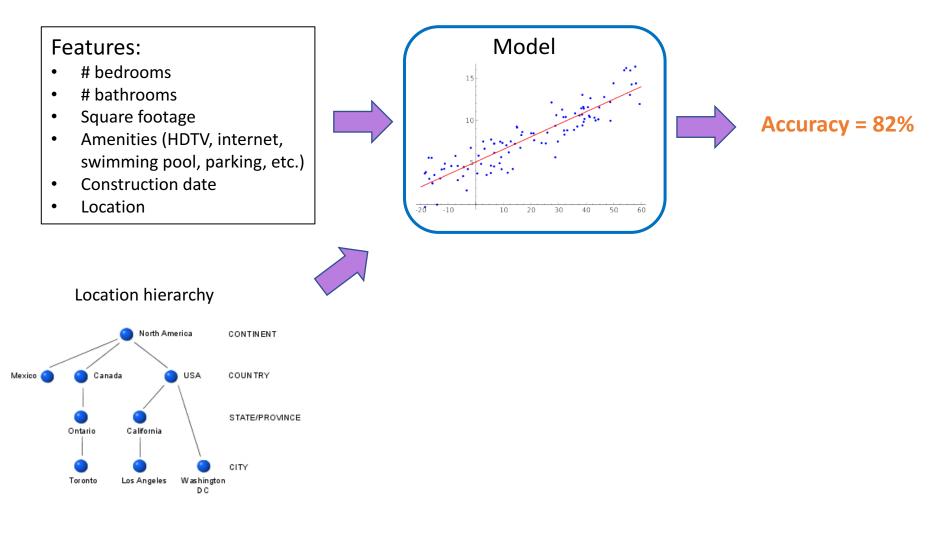
Gradient boosting (XGBoost)

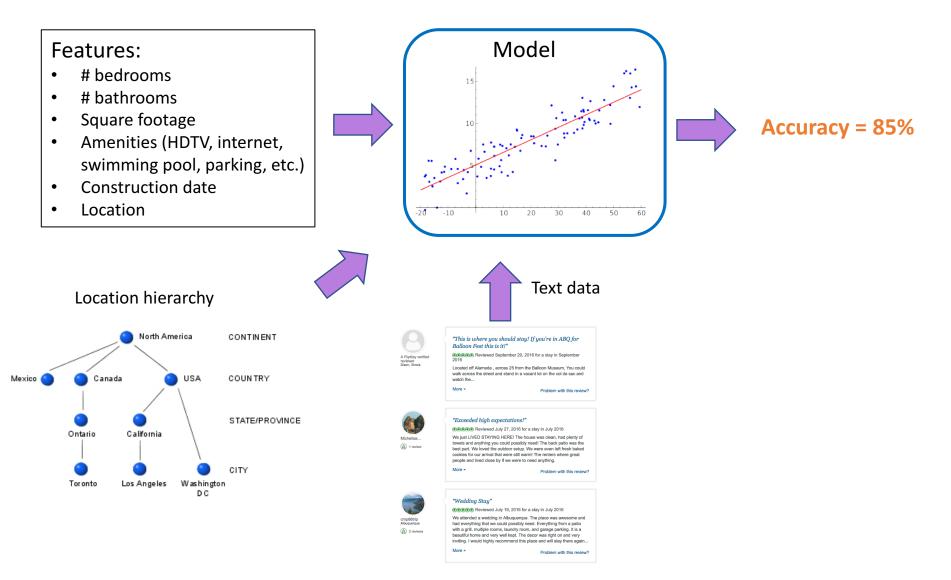
Neural networks (deep learning)

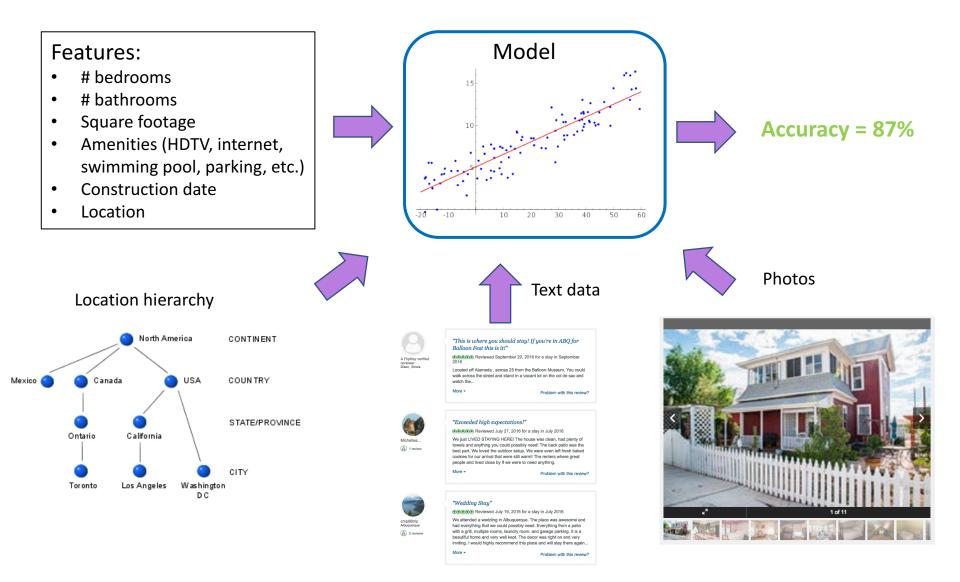
Features:

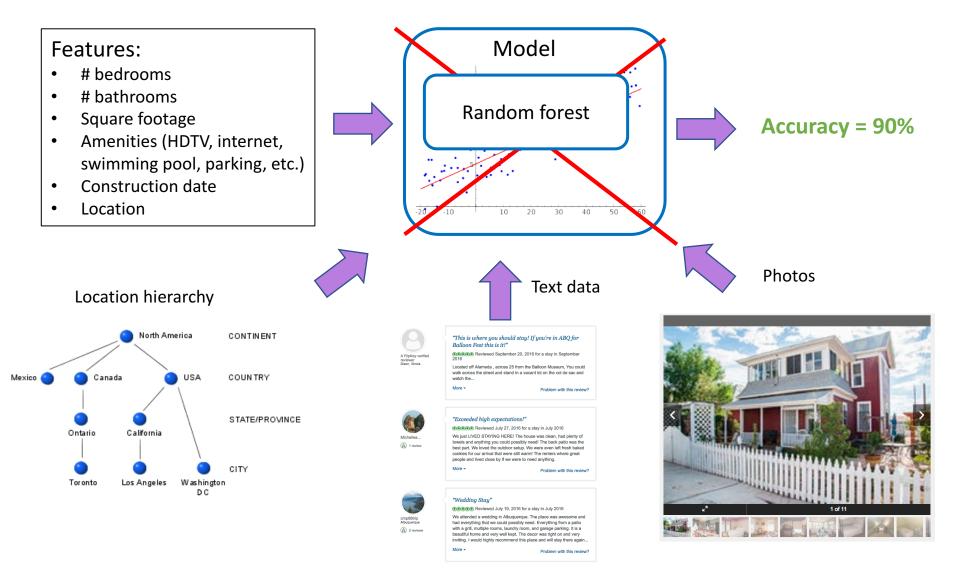
- # bedrooms
- # bathrooms
- Square footage
- Amenities (HDTV, internet, swimming pool, parking, etc.)
- Construction date
- Location

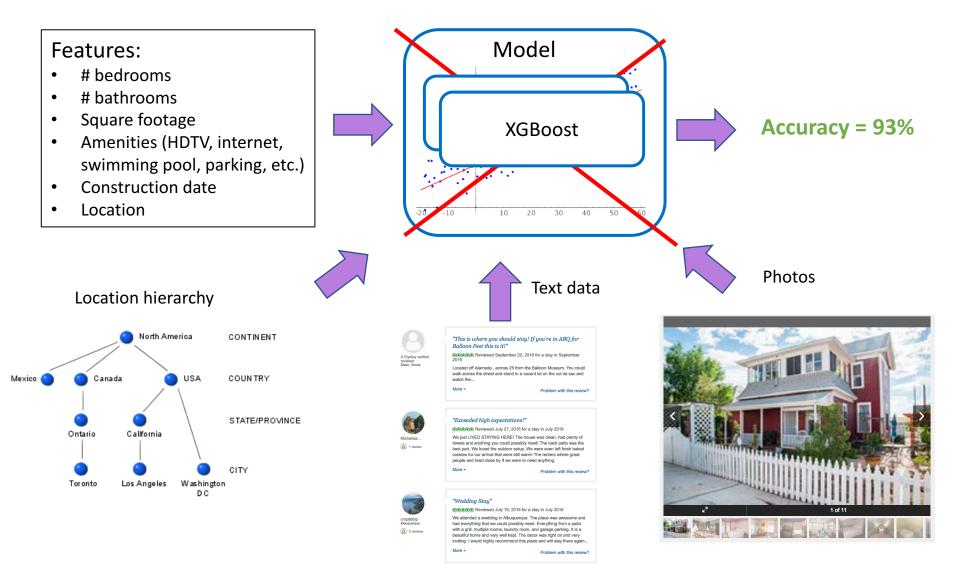


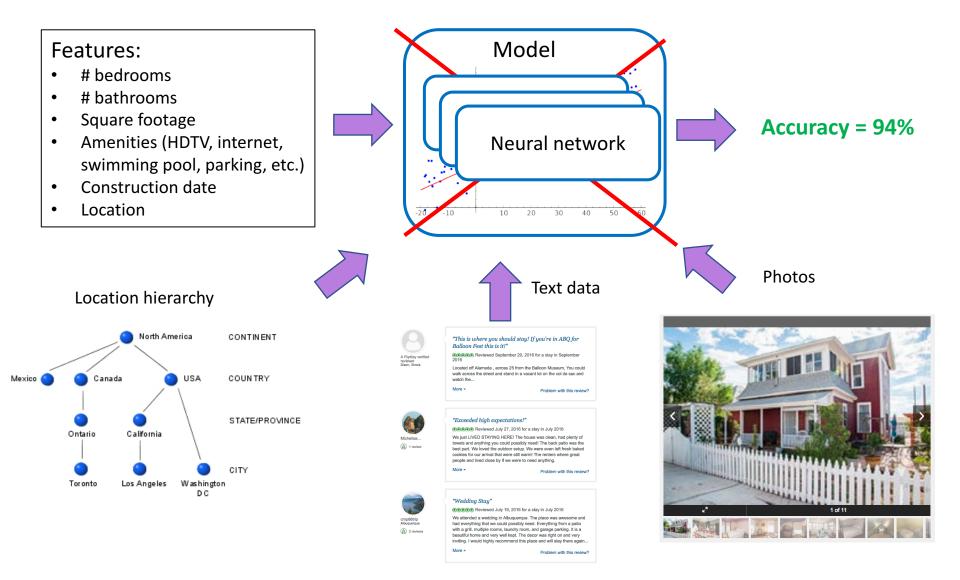








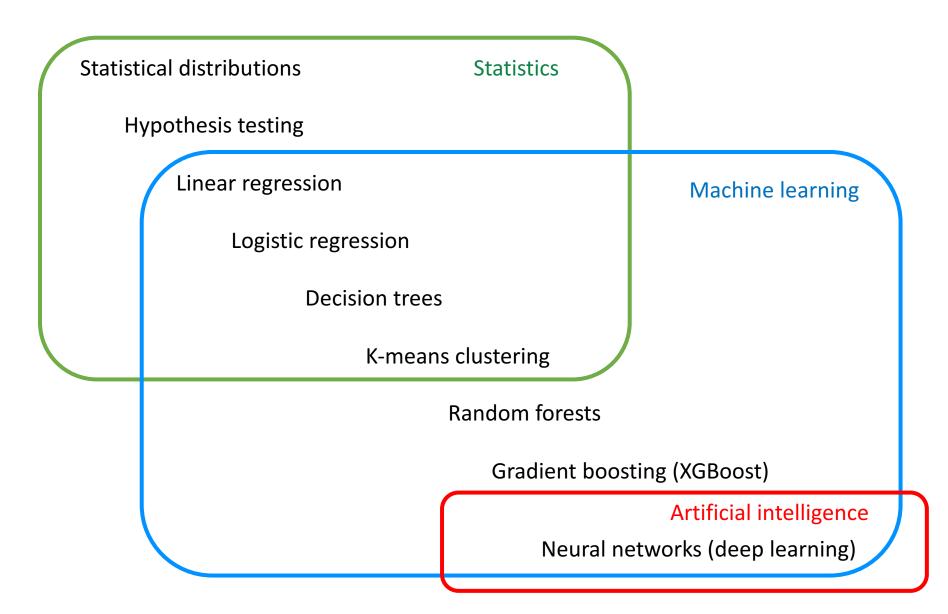




Recap (Part 1)

- Most problems in machine learning can be reduced to only 4 types: Clustering, regression, classification, and dimensionality reduction.
- The goal of a model is **not** to reduce error/increase accuracy but to generalize to unseen data.
- Model complexity increases flexibility, but requires more training data and reduces interpretability.
- Regularization techniques constrain model complexity and improve generalization.
- Model validation techniques can be used to properly tune hyperparameters and achieve the right bias-variance trade-off.

Statistics x ML x Al



What is machine learning?

- The science of building computer models that:
 - $\,\circ\,$ Learn from data how to perform a task
 - Self-tune their parameters to optimize performance
 - $\,\circ\,$ Generalize behavior to new/unseen data