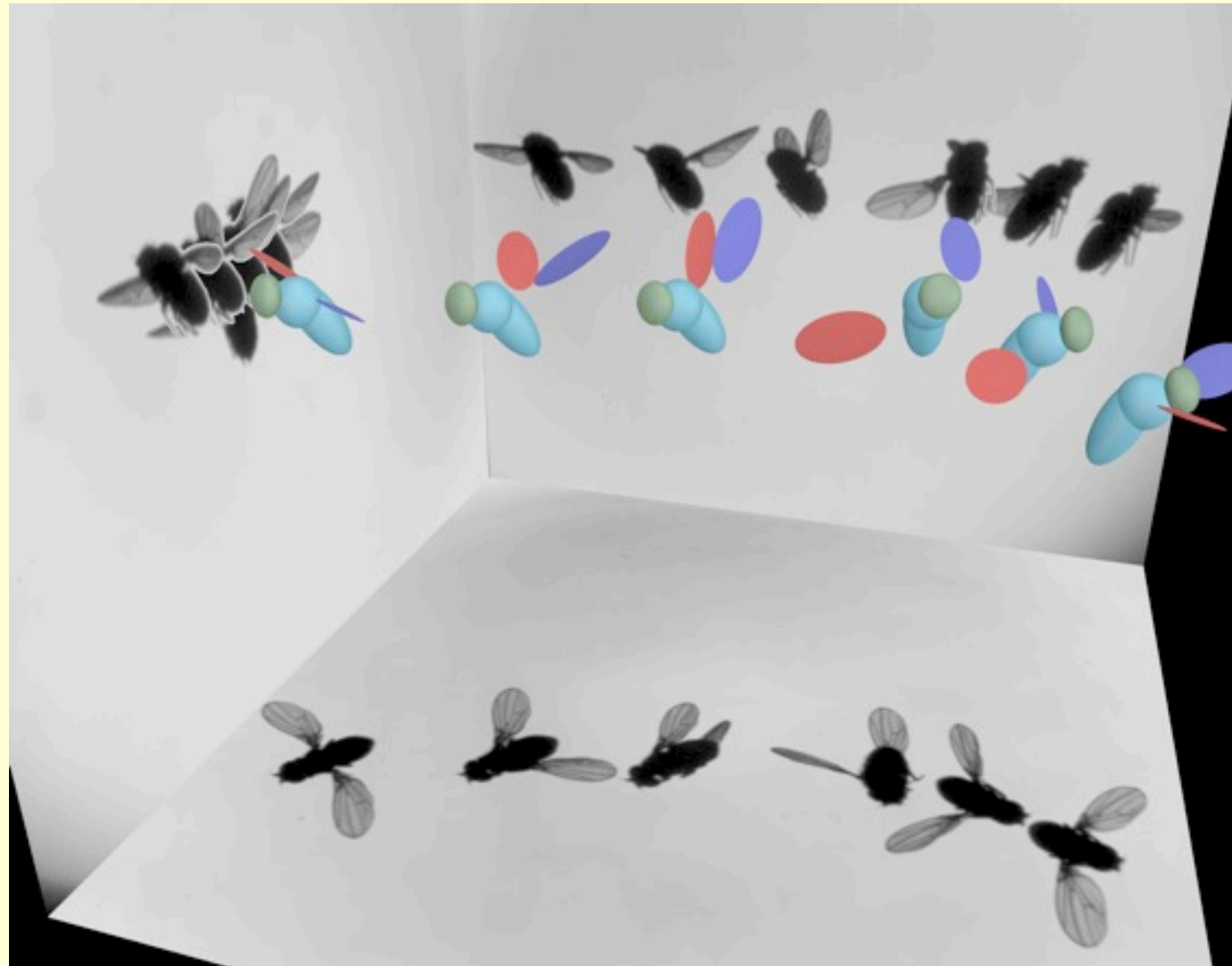


# Insect Flight

movement and thoughts



Jane Wang  
Cornell University

## Students/Collaborators:

### Aerodynamics of Dragonfly Flight/ Falling Paper

David Russell, Anders Andersen, Umberto Pesavento

### Computational Fluid Dynamics:

Sheng Xu

### Flight Dynamics of Fruit flies:

Leif Ristroph, Attila Bergou, Gordon Berman  
Itai Cohen, John Guckenheimer

### Stability Analysis of Insects in Free Flight:

Song Chang

## Papers:

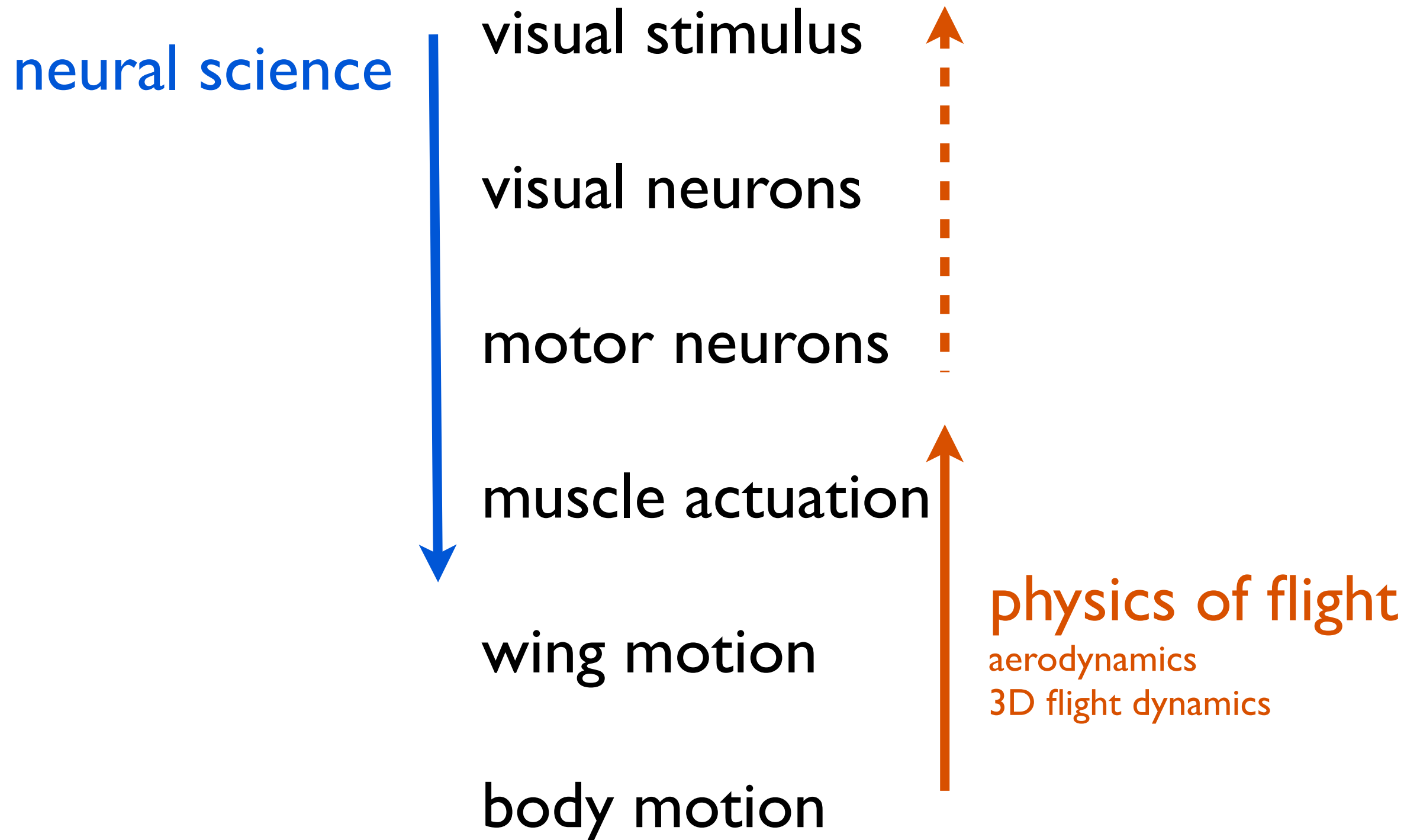
<http://dragonfly.tam.cornell.edu>

## Support:

NSF, AFOSR, ONR, Packard Foundation

# Quantitative Study of Organismal Behavior

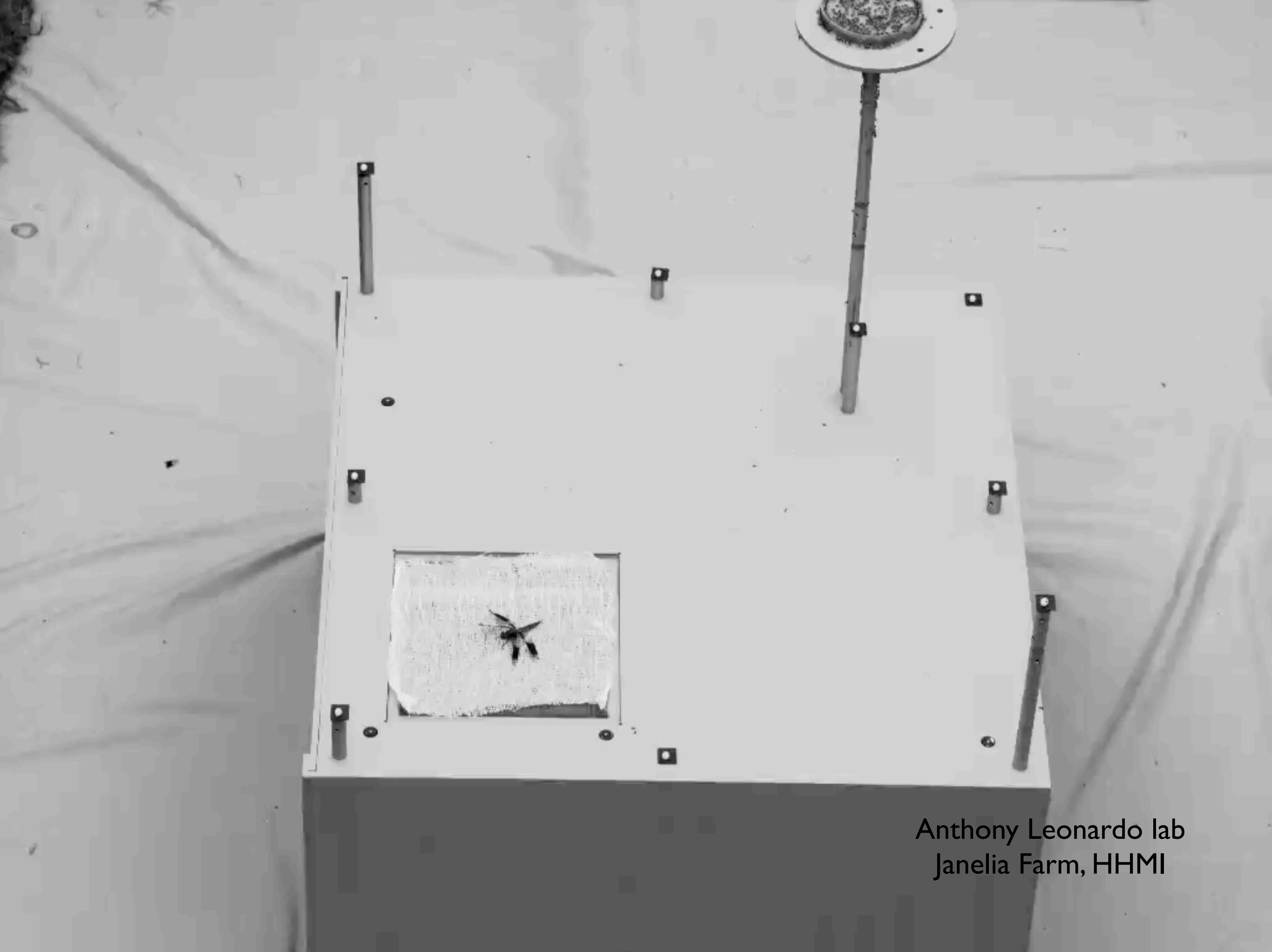
from flight dynamics to neural dynamics



# Why Do Organisms Move the Way They Do?







Anthony Leonardo lab  
Janelia Farm, HHMI

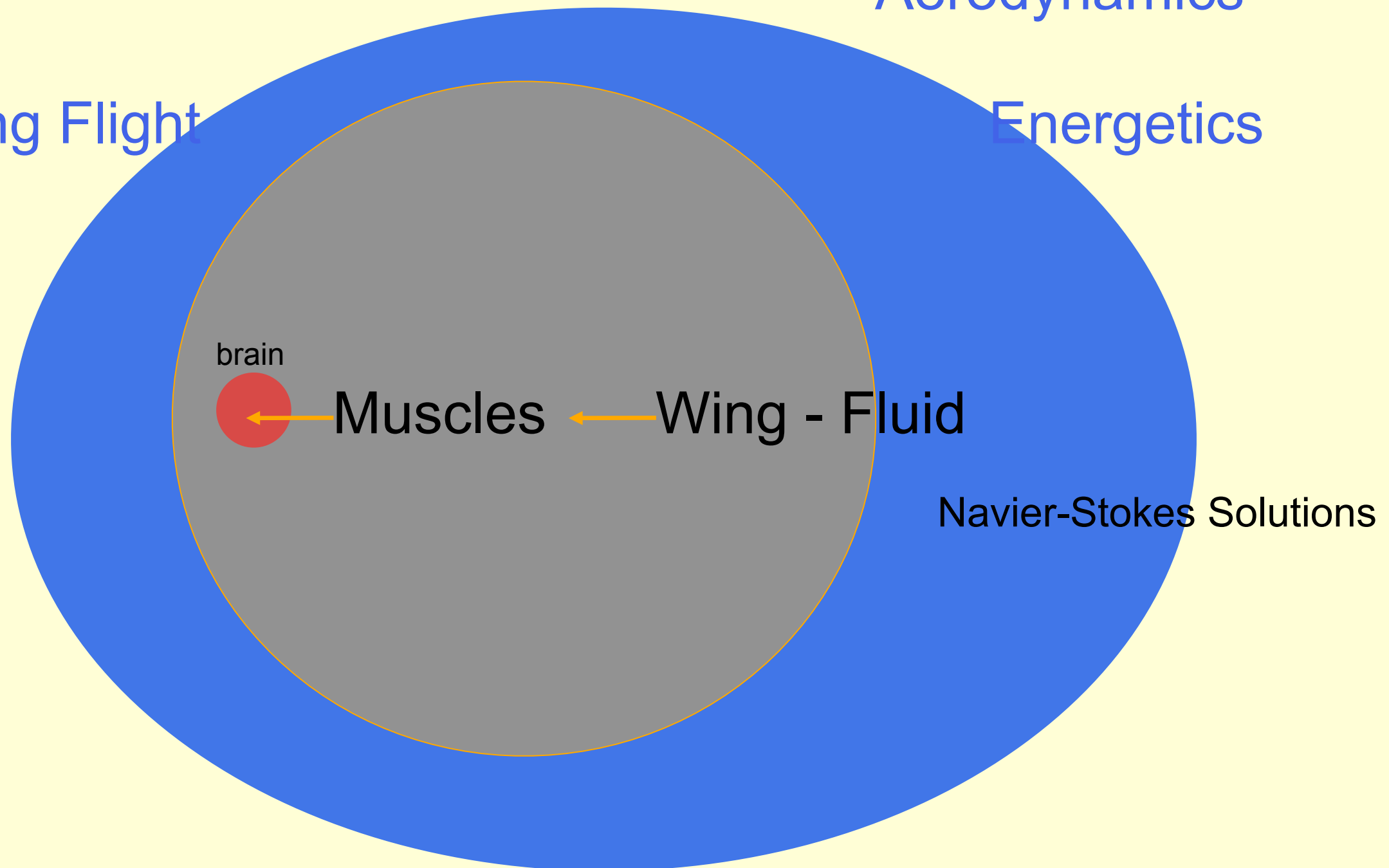
# Dissecting Insect Flight

Dynamics

Aerodynamics

Maneuvering Flight

Energetics



# Taking It Apart

- I. Kinematics
- II. Aerodynamics and Computational Methods
- III. Energetics and Optimization
- IV. Dynamics and Control
- V. Stability and Control



Le vol d'un pélican vu de profil.

## MAREY ET LE VOL DES OISEAUX

Les premières études scientifiques des mouvements des êtres vivants sont l'œuvre d'Etienne-Jules Marey. Le rôle de Marey dans les recherches concernant le vol des oiseaux a été considérable.

Entre 1860 et 1880, il a essayé nombre d'appareils de mesure, la plupart basés sur son « tambour » pneumatique transformant les mouvements à un style inscripteur. Les expériences de Marey ont porté également à cette époque sur la subtilité des mouve-



Etienne-Jules Marey, membre de l'Institut (1830-1904).

Chronophotographie avec images successives  
par l'emploi d'un miroir tournant (1880).

appareils, en 1881, Marey obtint simultanément sur fond noir trois vues : de profil, de dessus et de trois quarts.

Marey créait en 1882 le fusil photographique à plaque circulaire mobile, puis, en 1888, il remplaçait la plaque fixe du chronophotographe par une bande de papier sensible située au foyer et se déplaçant de façon intermittente régulière avec arrêts aux passages des trous du disque obturateur. En 1889 et 1890, Marey perfectionnait cet appareil par l'introduction de bandes sensibles en celluloïd, puis transparentes, et,



Vol d'un canard (1881).



Prise du coup d'aile d'un goéland.

ments des ailes. En 1881, reprenant une idée de Pinaud, Marey fut le premier à réussir, grâce à l'appareil chronophotographique à plaque fixe avec disque obturateur, des images successives d'oiseaux en vol, rapprochées jusqu'à cinquante par seconde ou espacées et dissociées grâce à un miroir tournant. Combinant trois

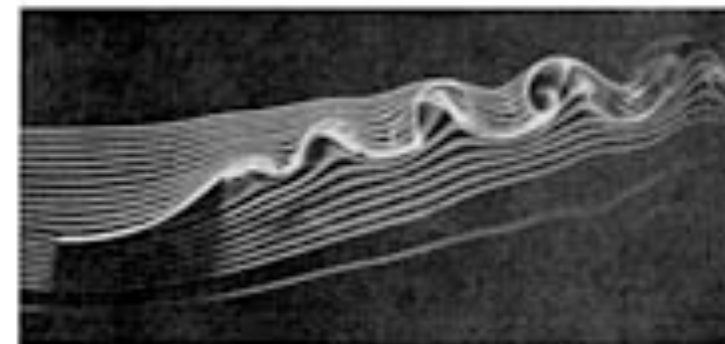
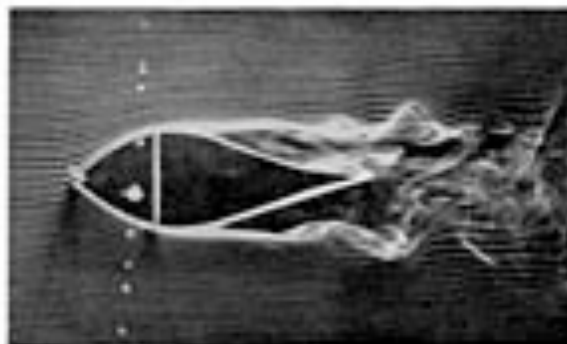


Essai d'un goéland.

en 1892, il projetait sur un écran les séries d'images obtenues.

Les travaux chronophotographiques de Marey forment la base de l'invention de la cinématographie.

A la fin de sa carrière, Marey étudia au moyen de fumées les remous produits par différents corps ou placés dans un courant d'air.



Déformations des filets d'un courant d'air, marqués par de la fumée d'amadou, au contact d'un corps fuselé et d'une surface courbe (1900-1901).

E. J. Marey  
1830-1904



difference, that an insect allowed to take flight after a string is tied to its leg can remain in the air without difficulty, while a bird similarly treated will fall to the ground as soon as the string is stretched. The apparatus of Professor Marey, as improved by him, is sufficient to determine, with the greatest precision, the number of beats of the wing per minute, as well as the particular curve of flight; and, among other observations, he informs us that, while the sparrow makes thirteen movements of the wing in a second, and the wild duck nine, the buzzard (*Buteo vulgaris*) beats its wings only three times in the same interval. As a general rule, he finds that the time occupied in depressing the wing is always decidedly longer than that of elevation, excepting in birds of a small wing area, in which case the two periods are almost equal. At starting the bird appears to make fewer strokes, but with a greater amplitude of stretch than subsequently. The rapidity of the stroke, on the other hand, appears to diminish anew when the bird has obtained a high degree of velocity.

The comparison of the two modes of flight may be summed up by saying, that in the bird the extremity of the wing describes a simple helix, while in the insect a series of lemniscates is traced. The difference in the two curves will be appreciable by an examination of the diagrams.



FLIGHT OF A BIRD.



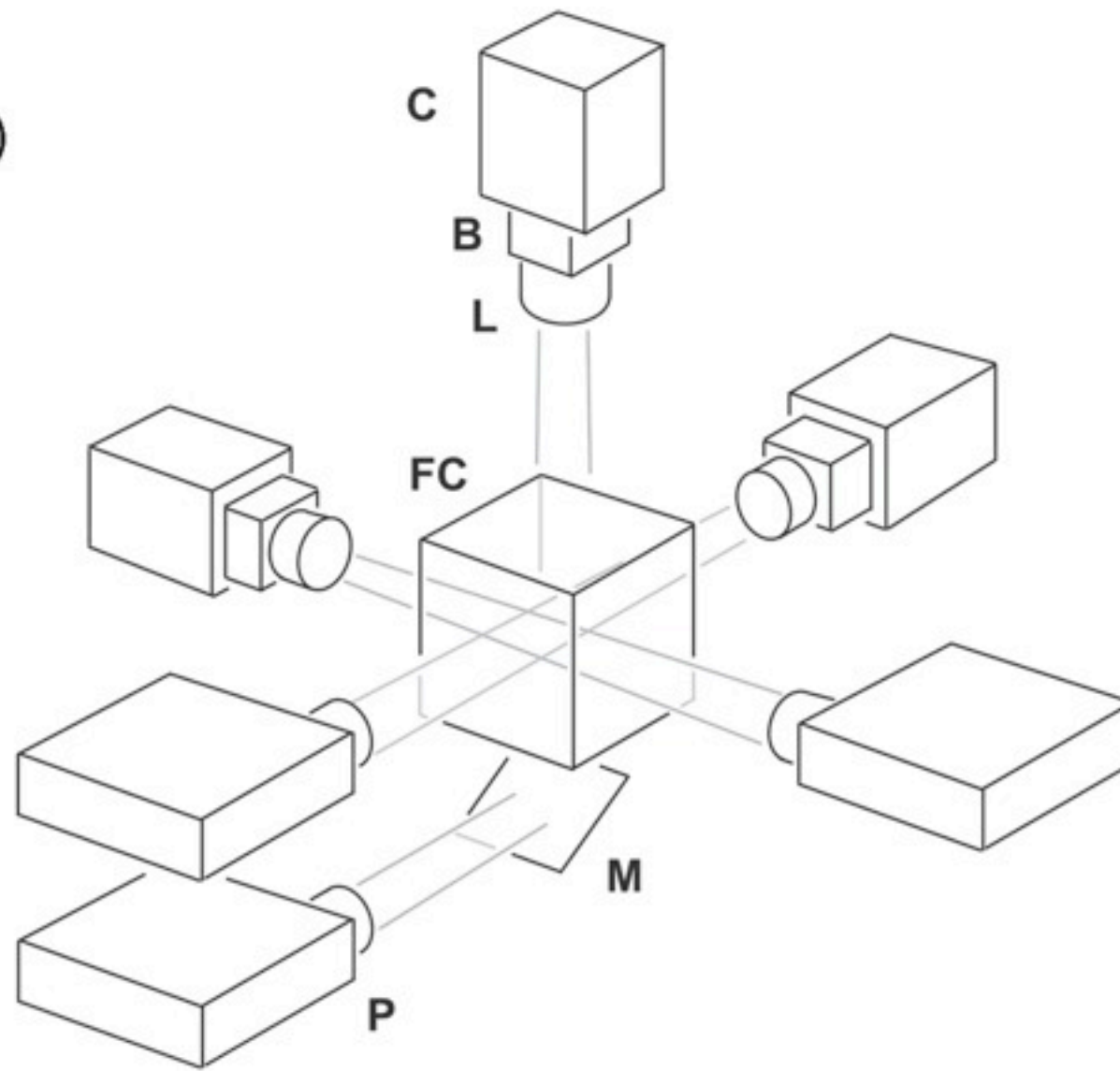
FLIGHT OF AN INSECT.

Harper Magazine  
1870

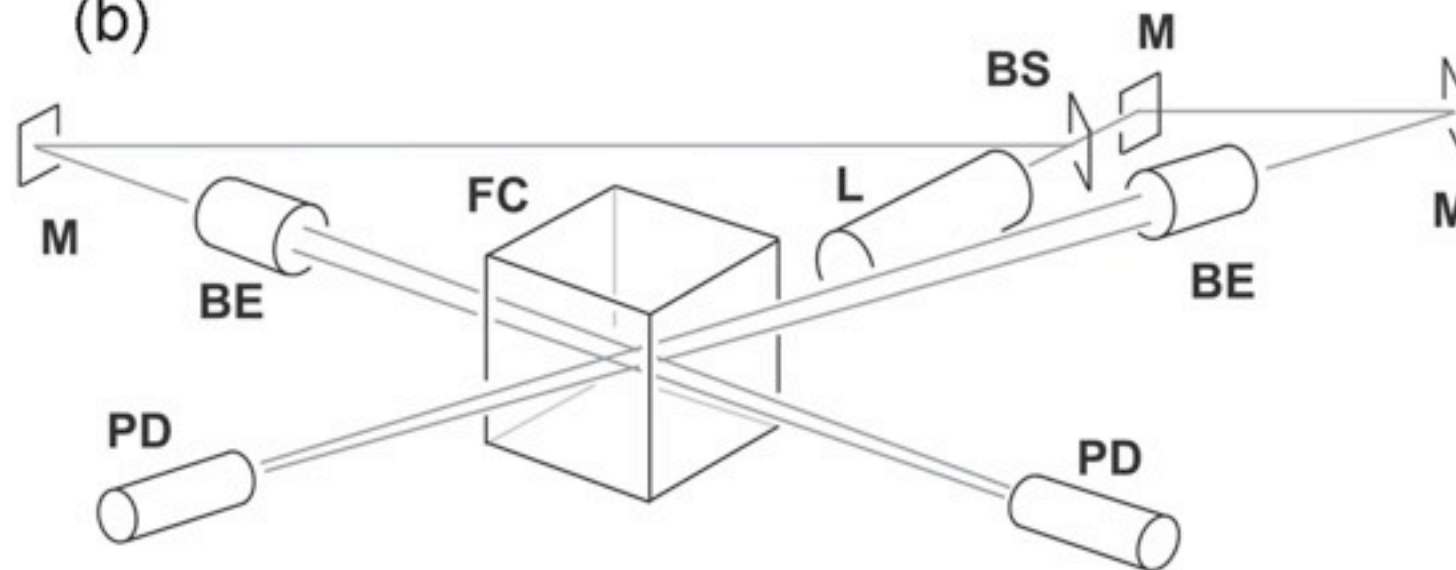
Fig. 9. — Zootrope dans lequel sont disposées 10 images en relief d'un goéland dans les attitudes successives du vol.

Other previous work:  
Weis-Fogh and Jensen (1956)  
Ellington (1984)  
Fry, Sane, Dickinson (2003)

(a)



(b)

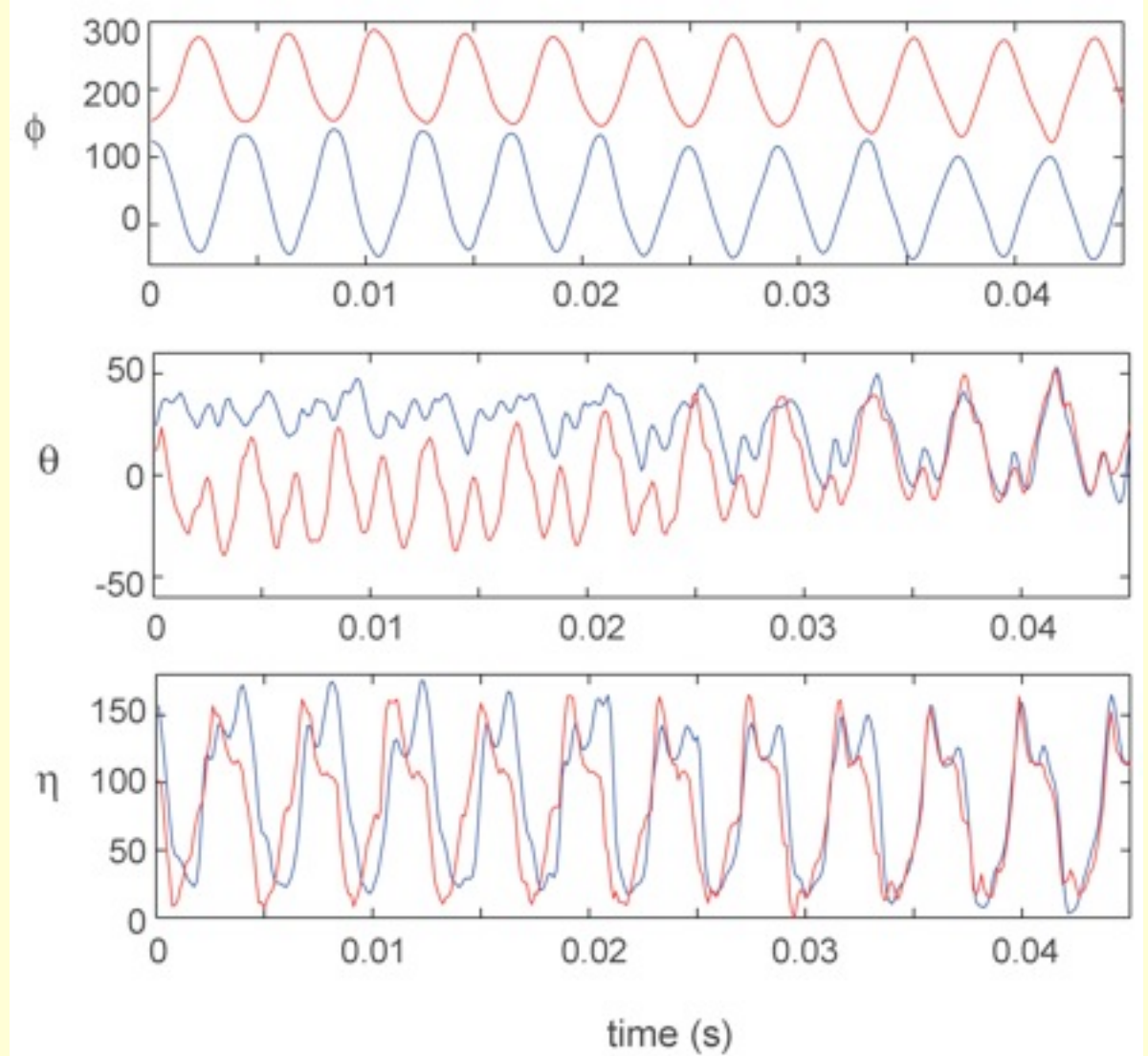
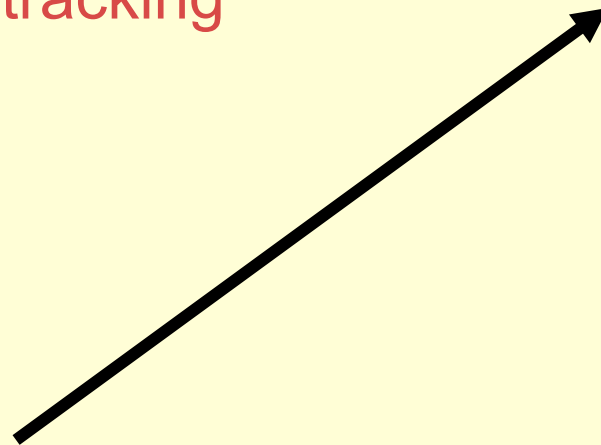


Leif Ristroph and Itai Cohen

Subtle change of wing kinematics

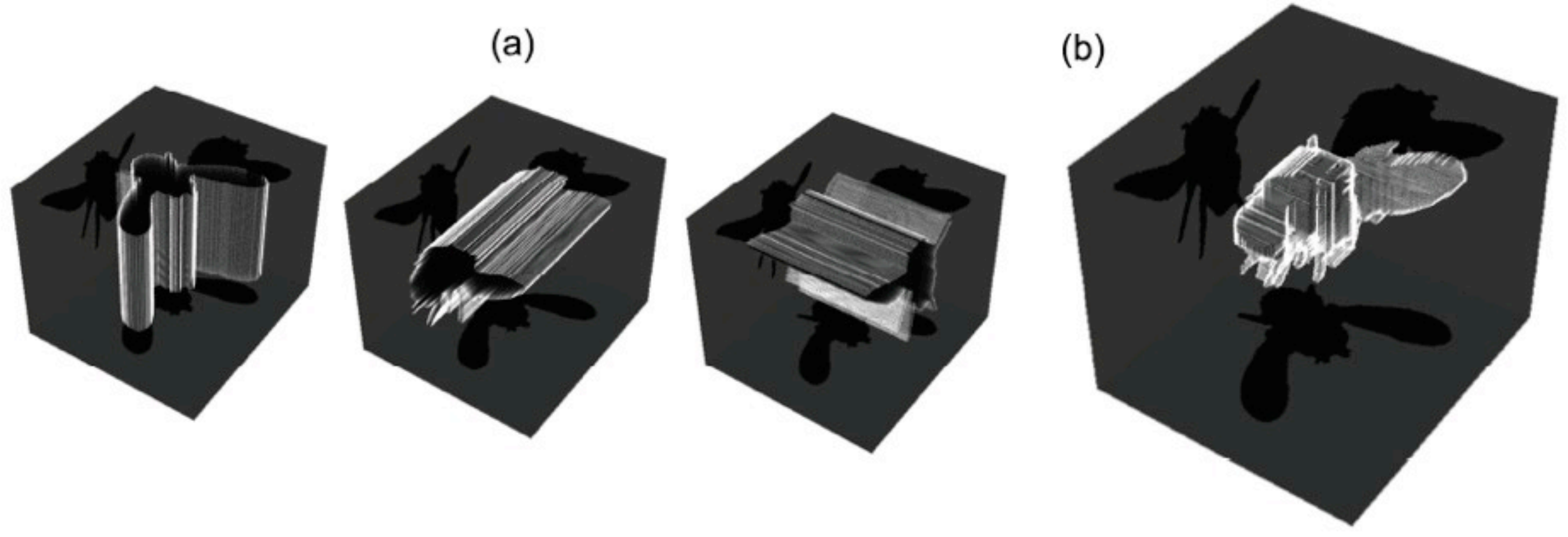
Lots of data

--> high accuracy & statistics  
in tracking





# Automatic Tracking of Wing and Body Motions (without using markers)



Ristroph, Berman, Bergou, Wang, Cohen, J. Exp. Biol.(2009)



# Automatic Tracking of Wing and Body Motions

---

1. Visual hull (maximal volume encompassing the fly)
2. Clustering Algorithm (separate body and wings)
3. Centroid (position)
4. Principal axes (orientation)

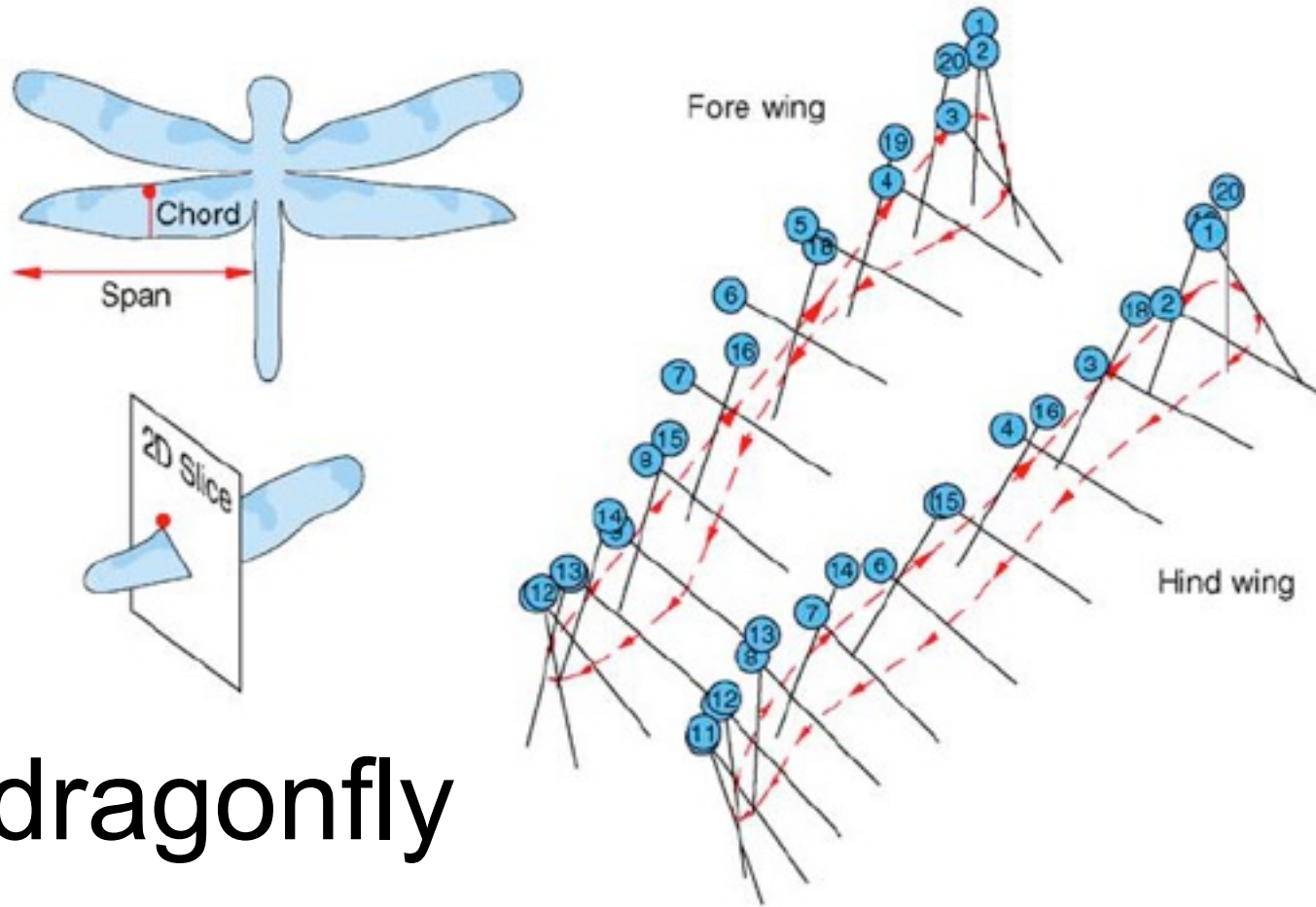
+ camera calibration and etc....

---

hours

reduced to

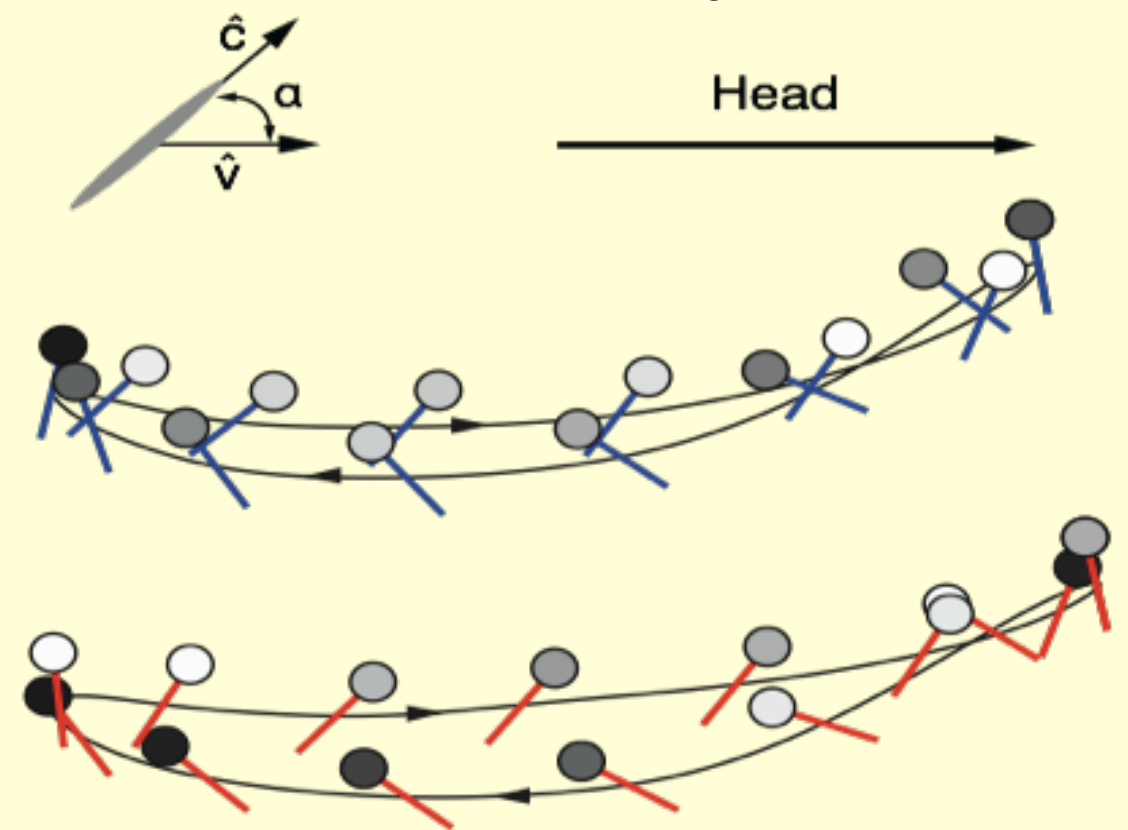
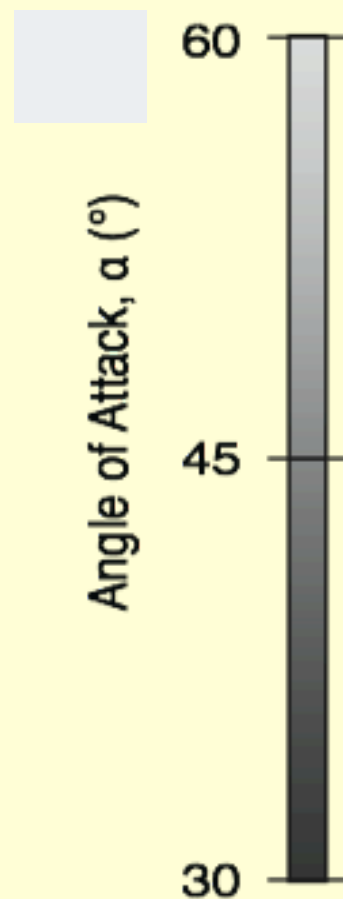
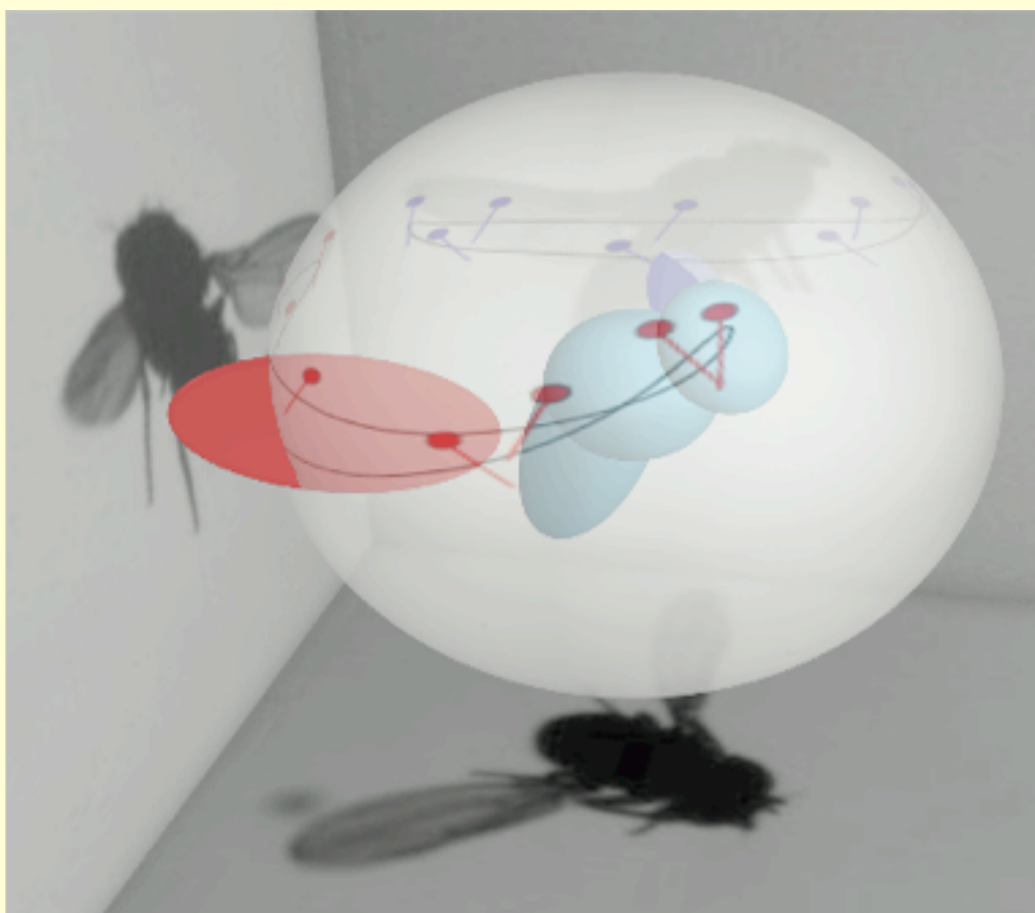
minutes



dragonfly

# Why the Observed Motions?

fruitfly



# Taking It Apart

I. Kinematics

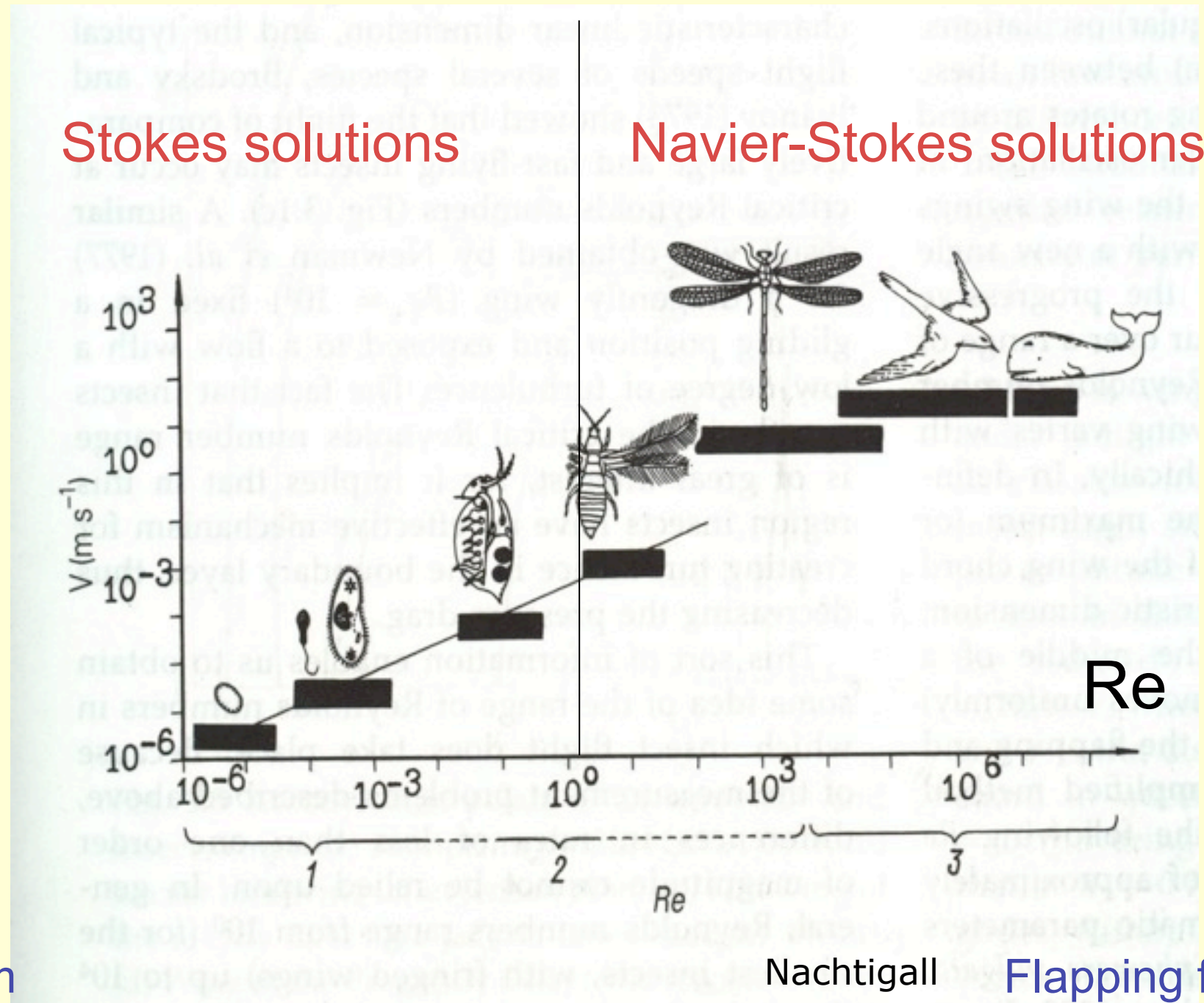
II. Aerodynamics and Computational Methods

III. Energetics and Optimization

IV. Dynamics and Control

V. Stability and Control

# Life in Fluids



Scallop theorem  
 Flagellar/Cilia swimming  
 Rotating helix/Helical wave/undulatory motion

Flapping flight/swimming  
 Gliding  
 Airplanes

G.I. Taylor, 1951, 1952 Swimming Micro-organisms  
 Purcell, 1977 Life at Low Reynolds numbers  
 Lauga and Powers 2009

Lighthill, 1975  
 Childress, 1981  
 Ellington 1984, Dickinson 1999  
 Wang 2005



# Governing Equations

Navier-Stokes equations for incompressible flows:

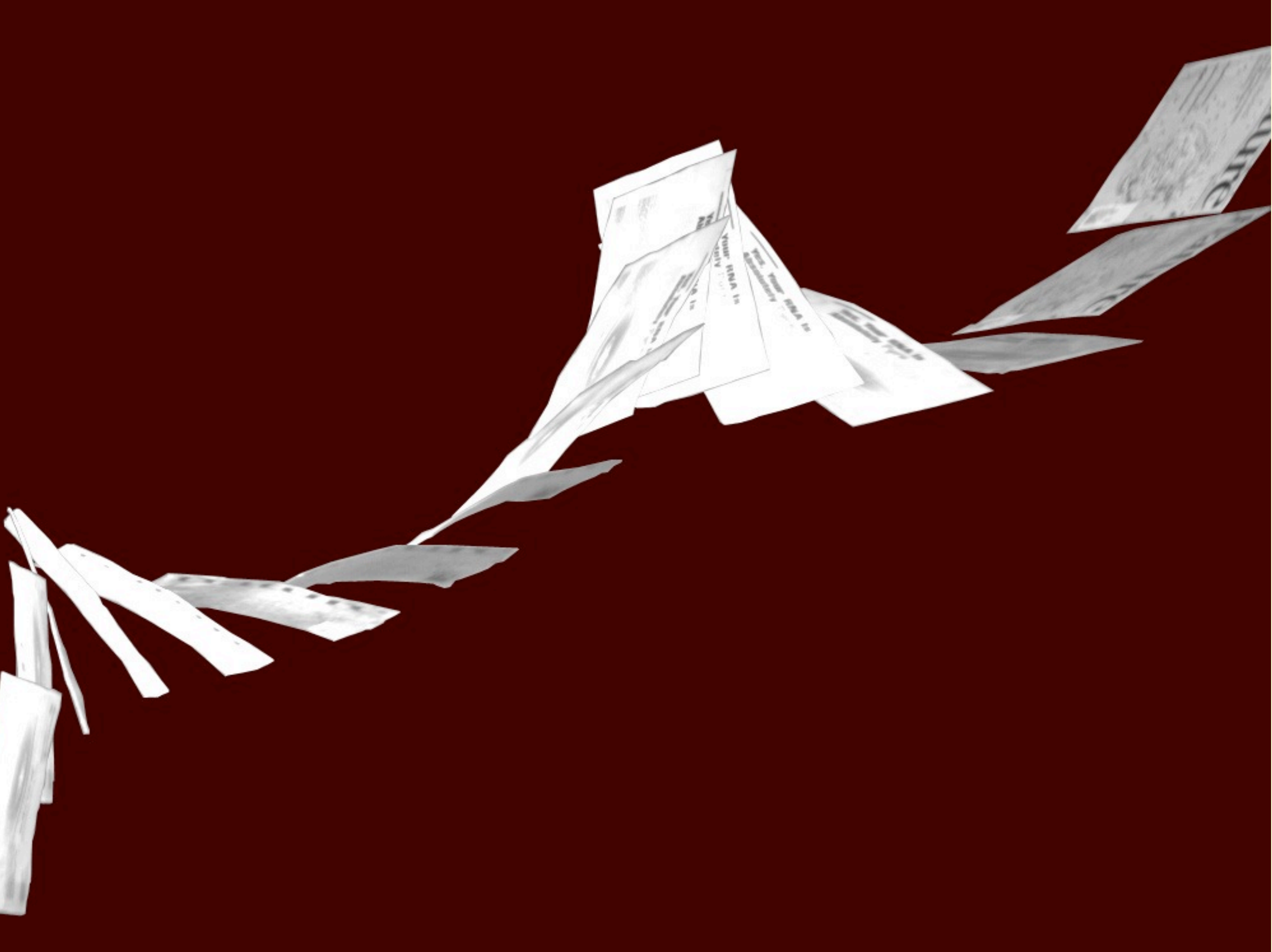
$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \frac{1}{\text{Re}} \nabla^2 \mathbf{u}$$
$$\nabla \bullet \mathbf{u} = 0$$

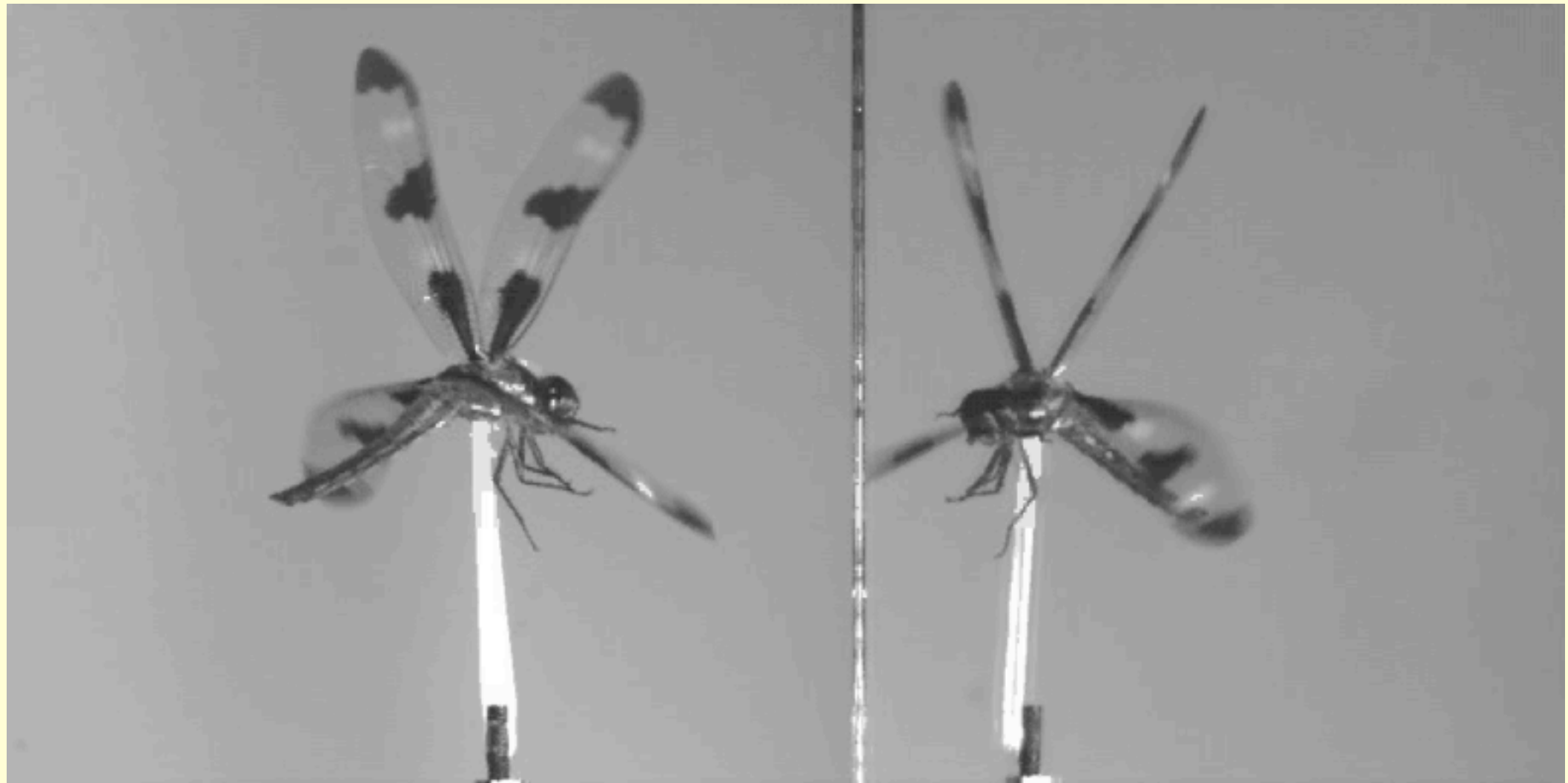
Boundary condition (no-slip) (wing kinematics):

$$\mathbf{u}_b = \mathbf{v}_b$$

Dynamics of the wing coupled to the fluid:

$$m \frac{d\mathbf{v}_b}{dt} = \mathbf{F}_{fluid} + \mathbf{F}_{ext}$$

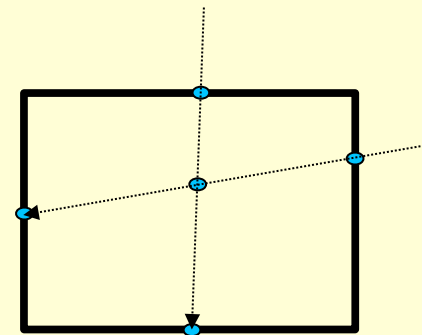
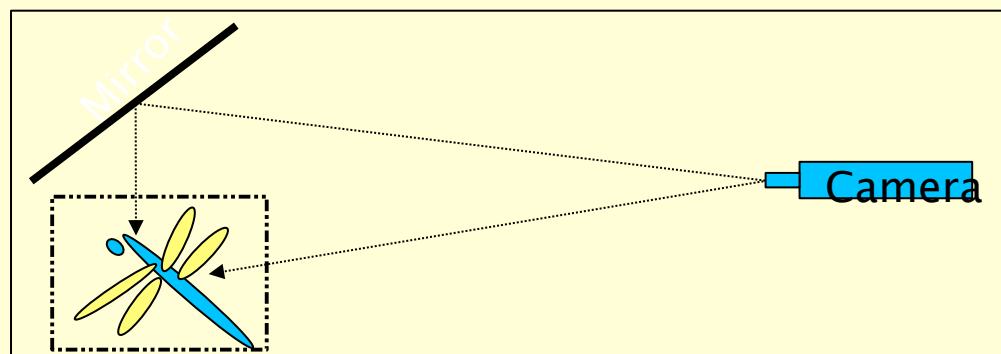




marker based tracking

1600fps, 1024x1024

mirror

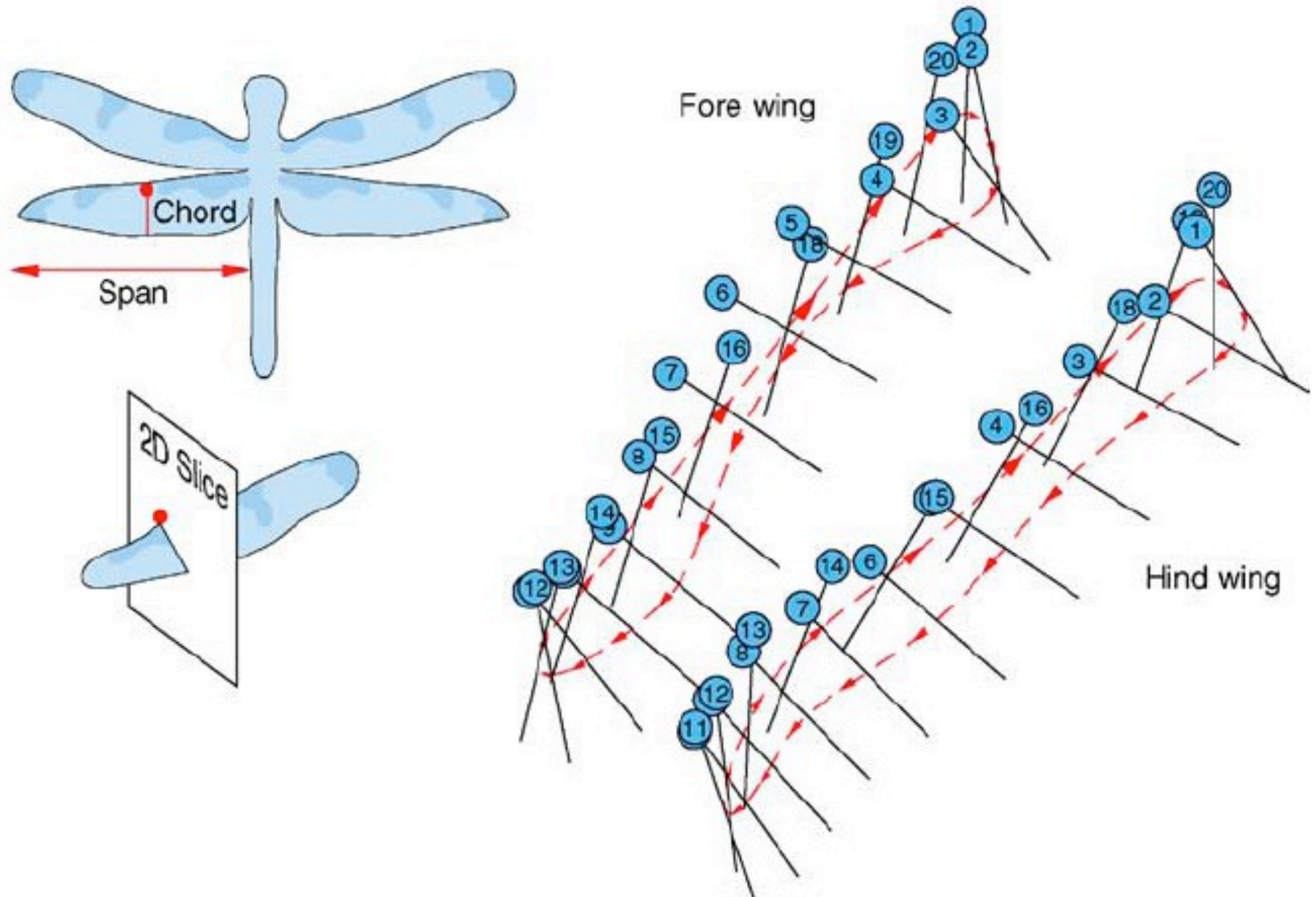


$L \sim 1\text{cm}$

Freq  $\sim 40\text{Hz}$

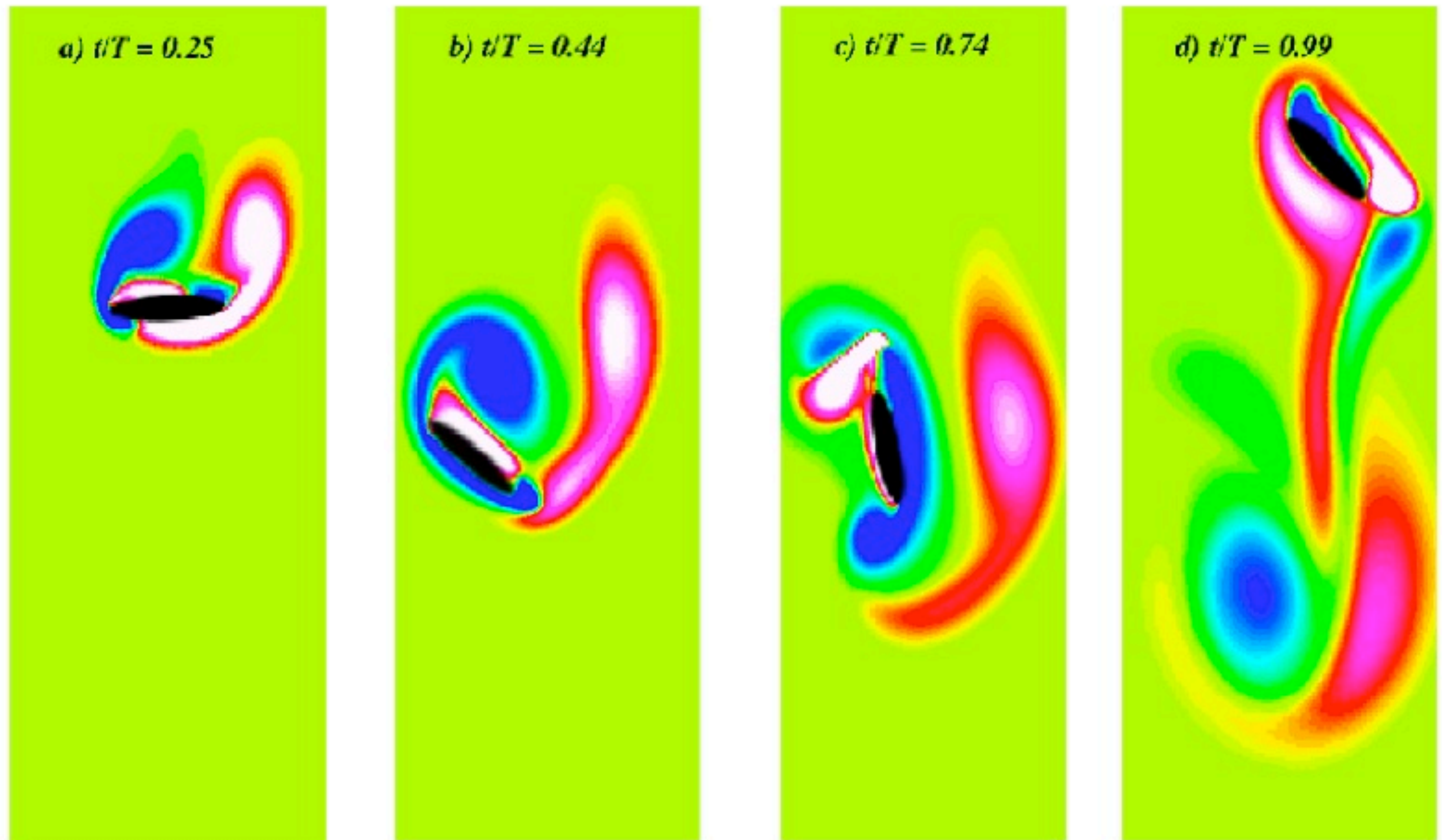
$Re = UL/\nu \sim 3000$

# Wing Kinematics



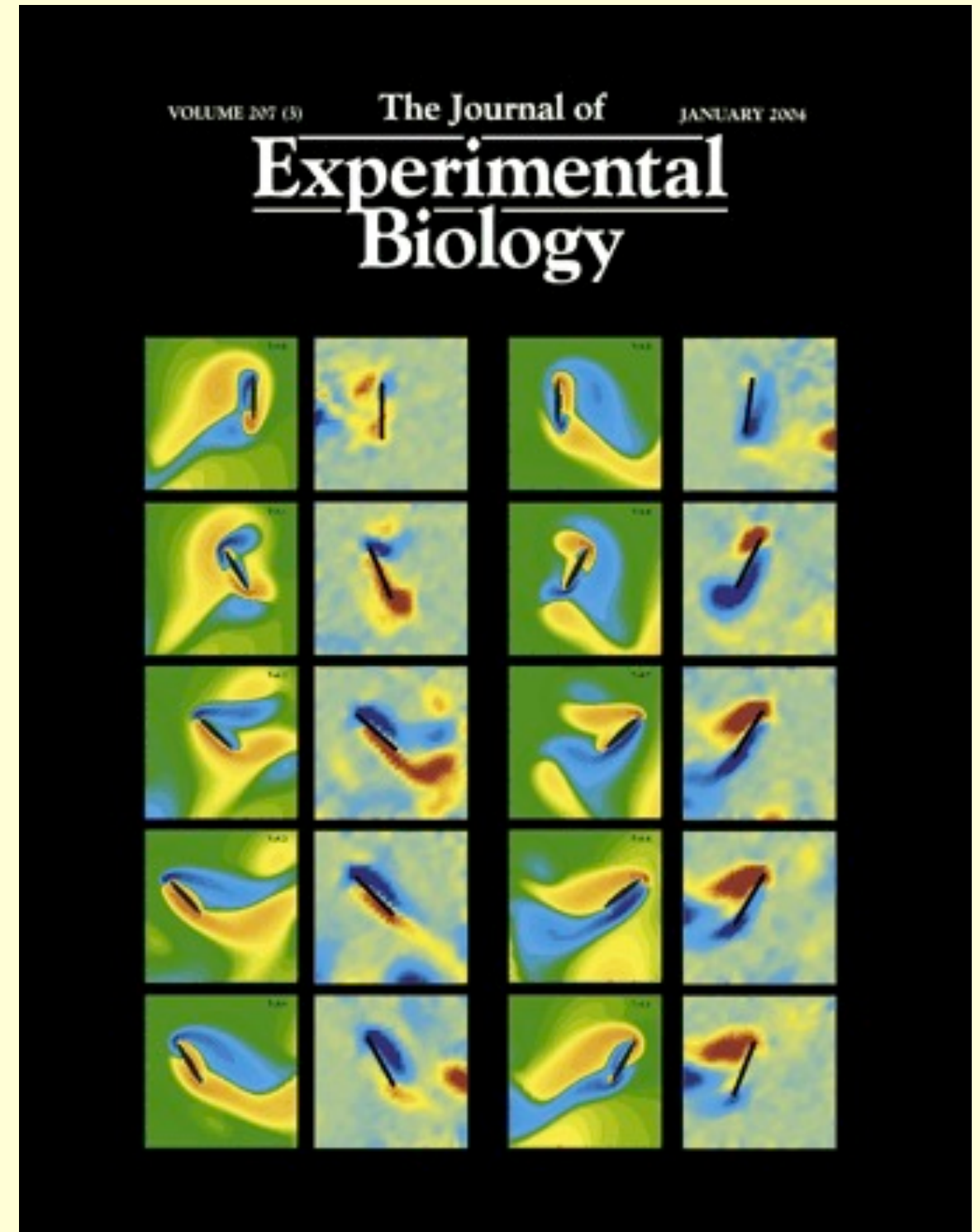
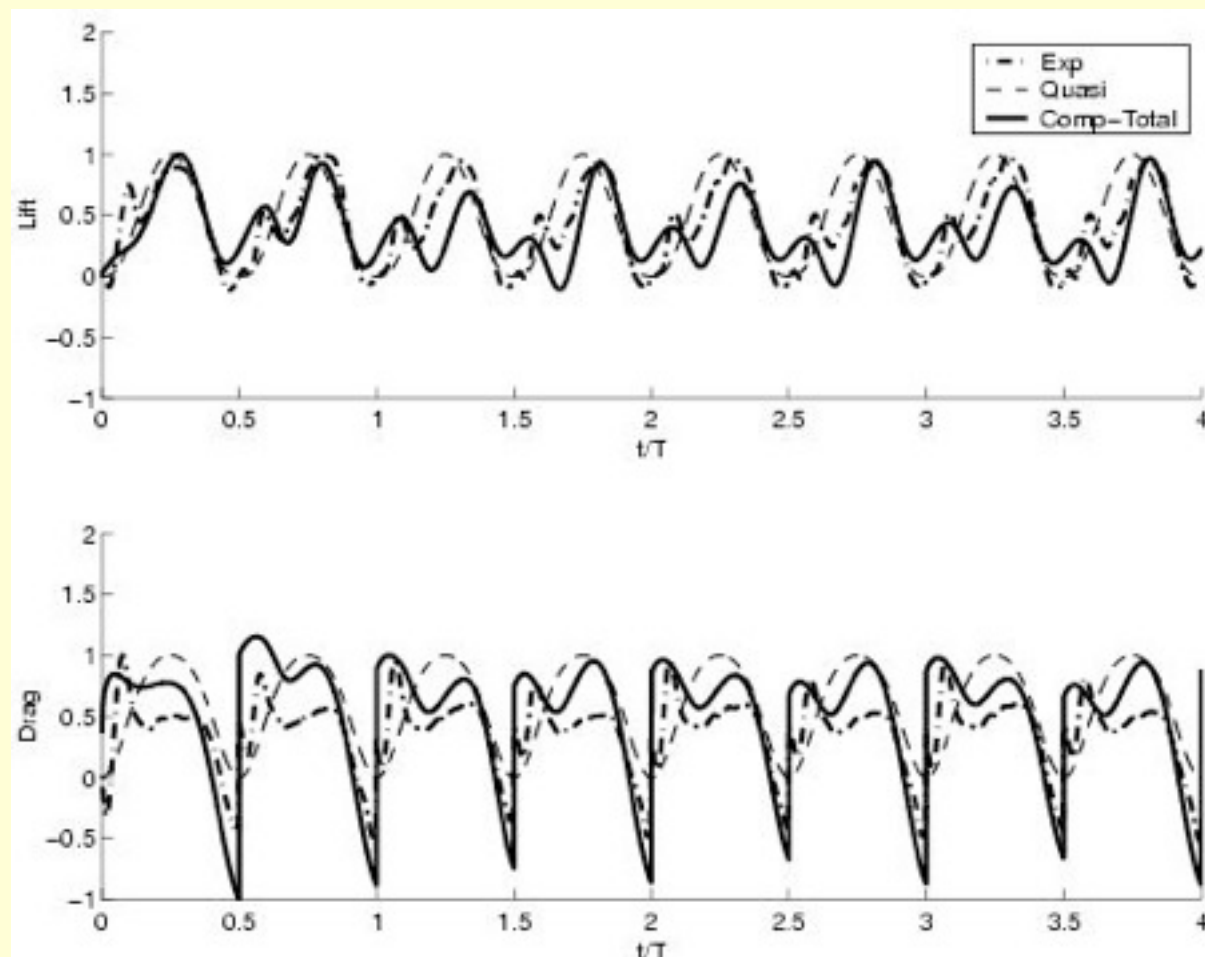
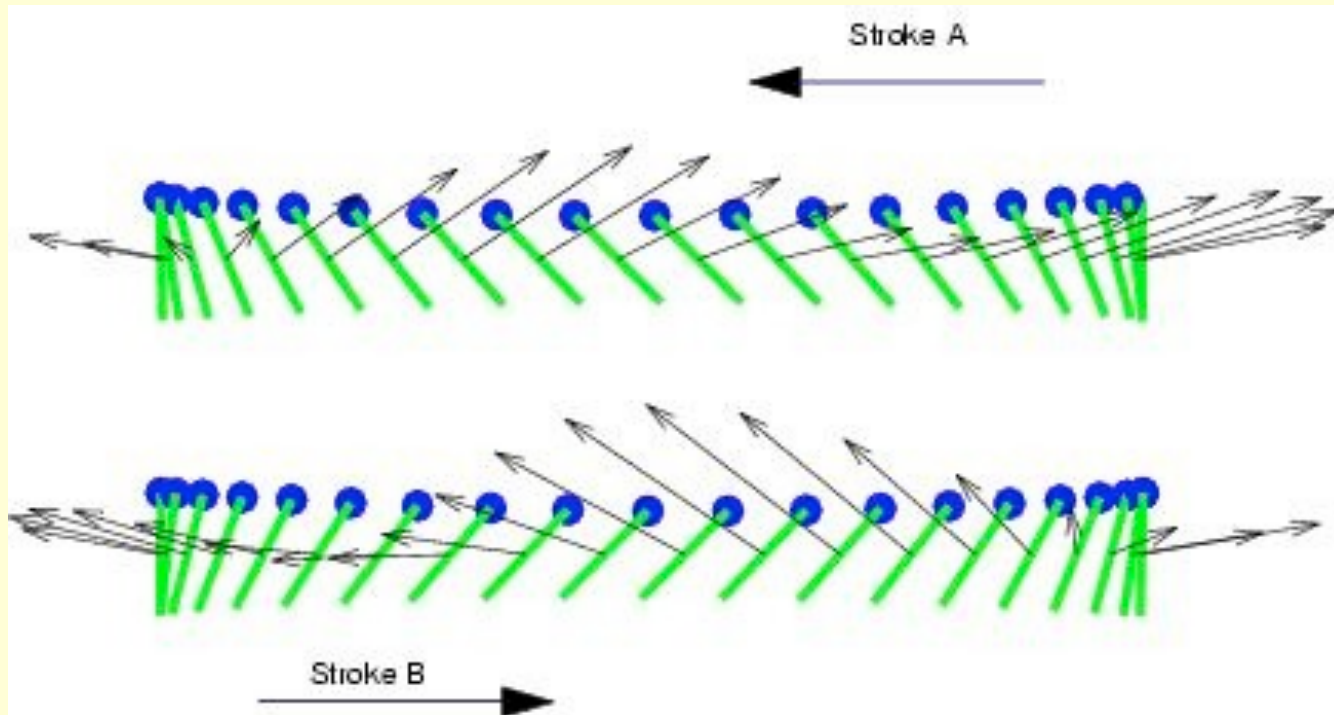


How does an insect flap its wings  
to generate enough forces to hover?



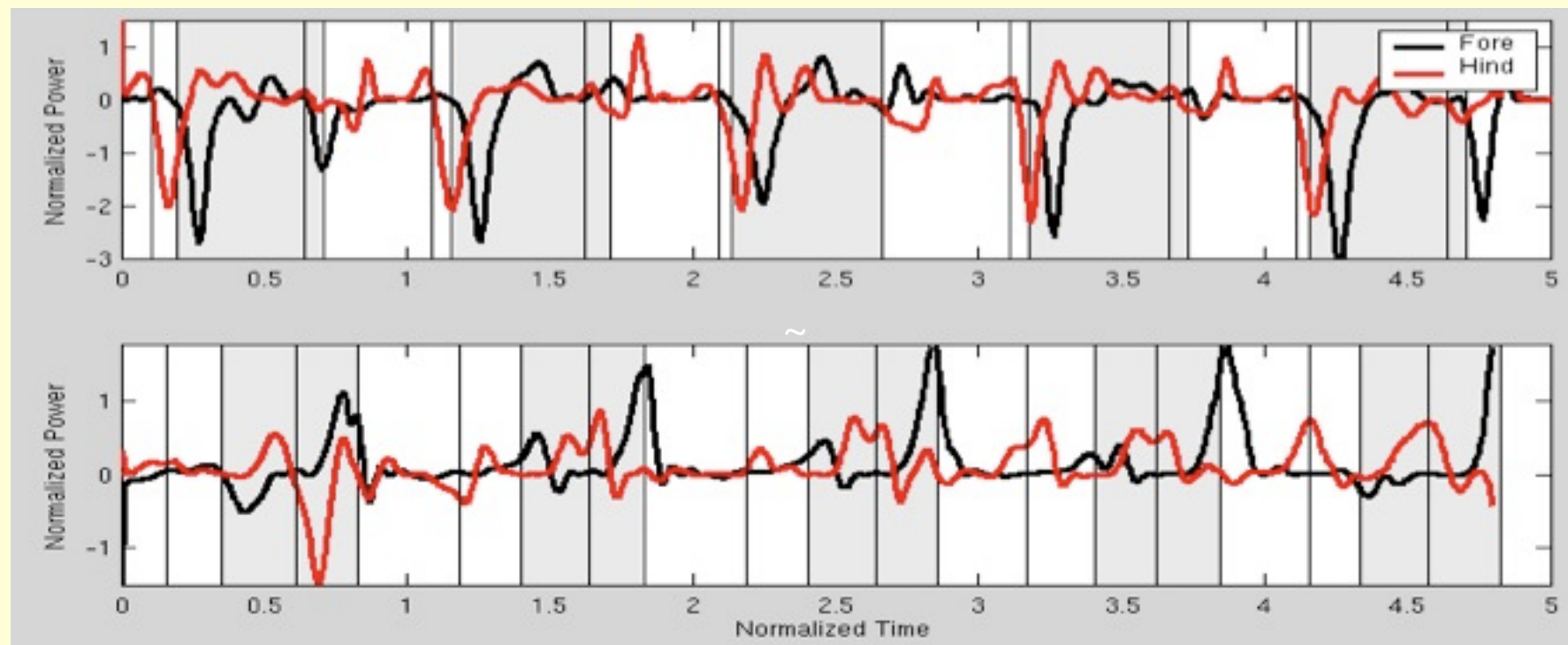
Wang, Phys. Rev. Lett. 2000

# Comparing Against Experiments



Wang, Birch, and Dickinson, JEB (2004)

# Passive Wing Pitching



Bergou, Xu, Wang, J. Fluid Mech., 2007



# Computing the Navier-Stokes Equation

## Which Method for Which Problem

Sharp Edges:

By conformal mapping:

$$x + iy = \cosh(\mu + i\theta)$$

$$S(\mu, \theta) = \cosh^2 \mu - \cos^2 \theta$$

2D NS equation (Vorticity–Stream Function Formulation) in elliptic coordinates

$$\frac{\partial(S\omega)}{\partial t} + (\sqrt{S}u \cdot \nabla)\omega = \frac{1}{\text{Re}} \nabla^2 \omega$$

$$S\omega = \nabla^2 \Psi$$

$$\sqrt{S}u = -\nabla \times \Psi$$

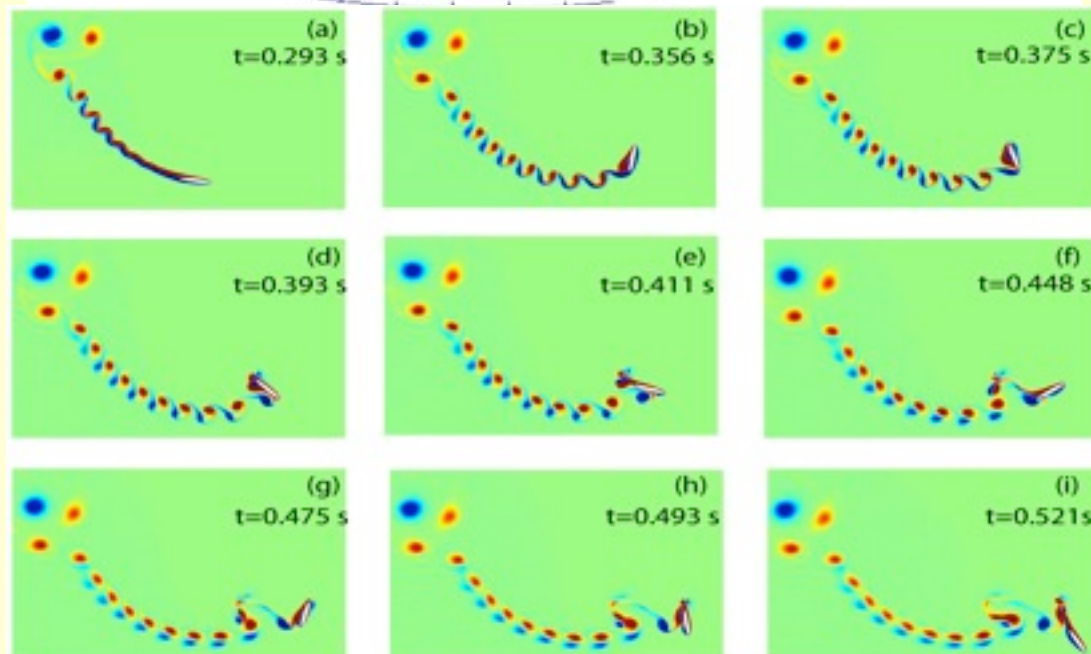
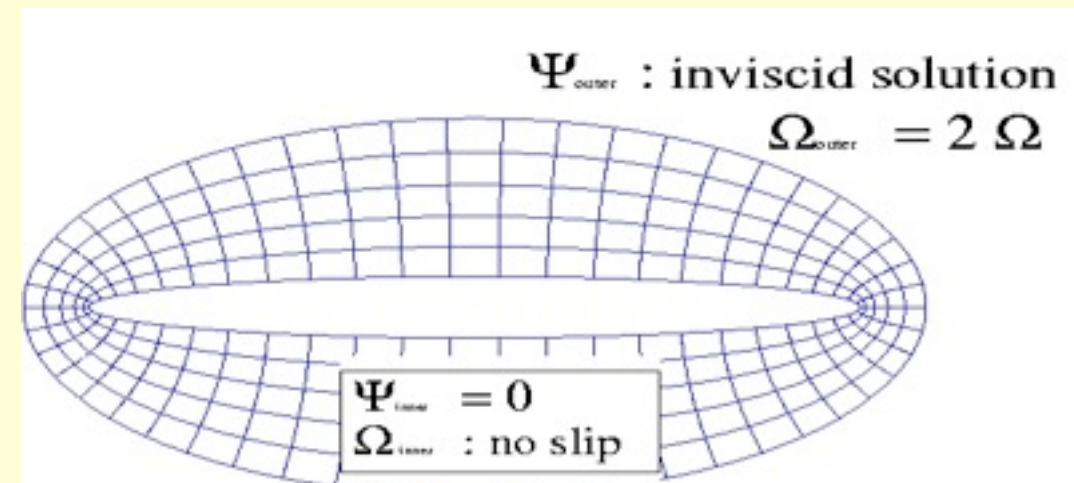
4th order in time (RK)

4th order in space (implicit scheme)

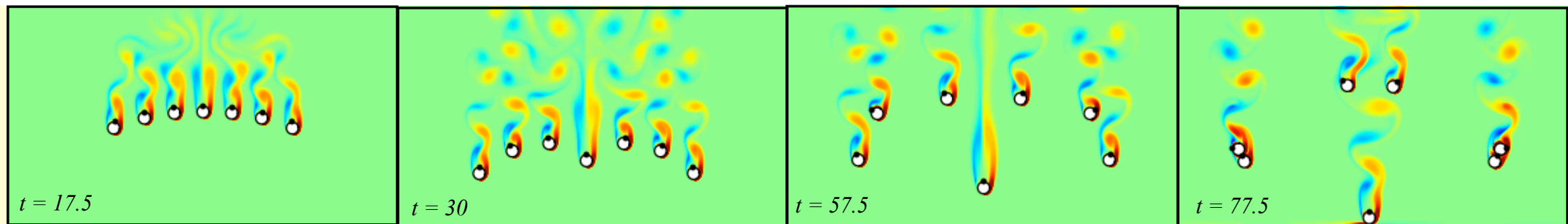
Explicit method (E & Liu 1996)

Solved in noninertial body frame in elliptic coord with far field boundary conditions

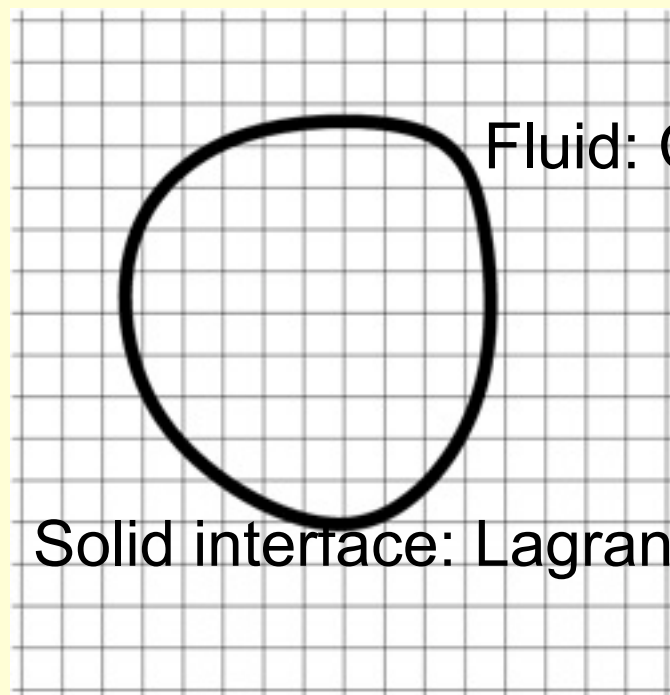
Dynamic coupling, PDE optimization  
wang (2000) , pesavento & wang 2004, 2009



# An immersed interface method for solving multiple moving objects in 2D and 3D (hydrodynamic interactions, collective behavior, flexibility)



$$\frac{\partial \vec{v}}{\partial t} + \vec{v} \cdot \nabla \vec{v} = -\nabla p + \frac{1}{Re} \nabla^2 \vec{v} + \int_{\Gamma} \vec{f}(\alpha, t) \delta(\vec{x} - \vec{X}(\alpha, t)) d\alpha$$



Fluid: Cartesian

$$\nabla \cdot \vec{v} = 0$$

Solid interface: Lagrangian

$$\begin{aligned} m_s \ddot{\vec{x}}_c &= \vec{F}_b + \vec{F}_{fl} \\ I \ddot{\theta} &= \vec{\tau}_{fl} + \vec{\tau}_b \end{aligned}$$

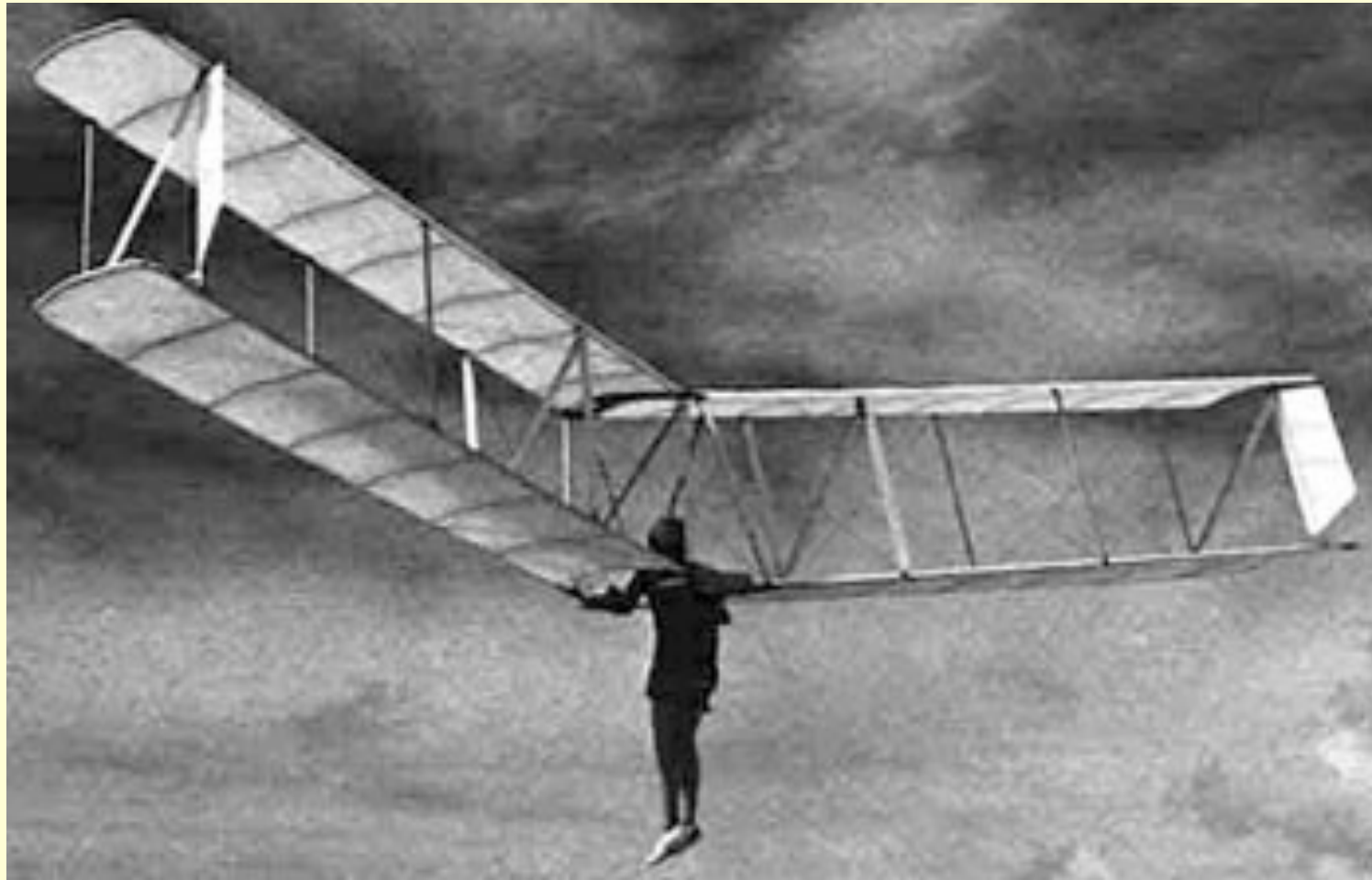
$$\begin{aligned} f_{\tau} &= -\frac{1}{Re} \left( \vec{\tau} \cdot \frac{\partial \vec{v}}{\partial n} \Big|_{\Gamma^+} - \frac{d\theta}{dt} \right) = -\frac{1}{Re} \left( \omega|_{\Gamma^+} - 2 \frac{d\theta}{dt} \right) \\ f_n &= \int \left( \frac{1}{Re} \left[ \frac{\partial \omega}{\partial n} \right] + [b_{\tau}] \right) J d\alpha \end{aligned}$$

Xu and Wang, SIAM J. Num. Analysis (2006), J. Comp. Phys. (2006), Comp. Meth. Appl. Mech. and Eng. (2008)

# ‘Birds vs. Plane’

Which is more efficient?

What do we mean by ‘efficient?’

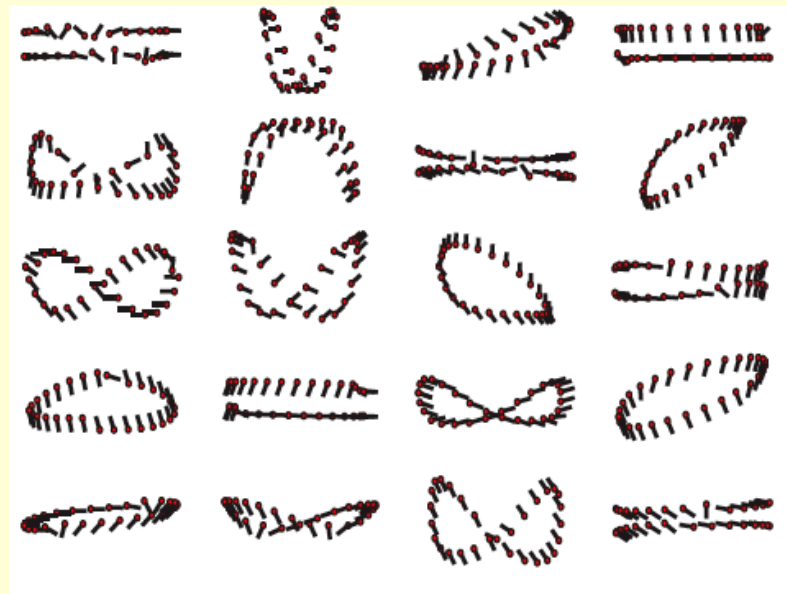
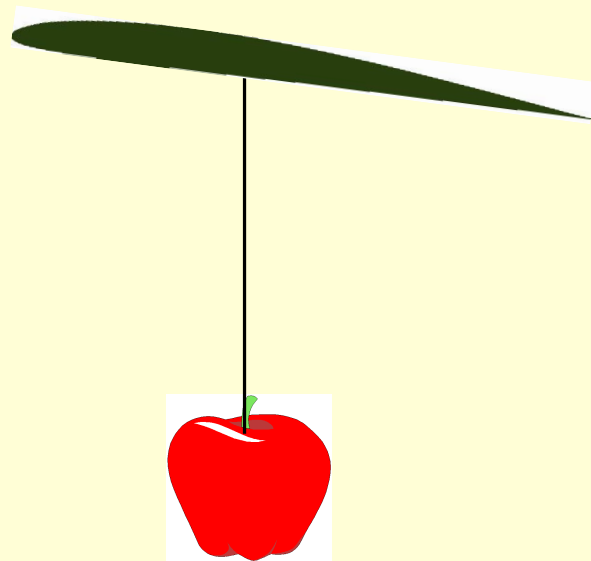


# Energy Minimizing Hovering Wing Motion

Problem:

Given a wing and a weight,

find wing motions

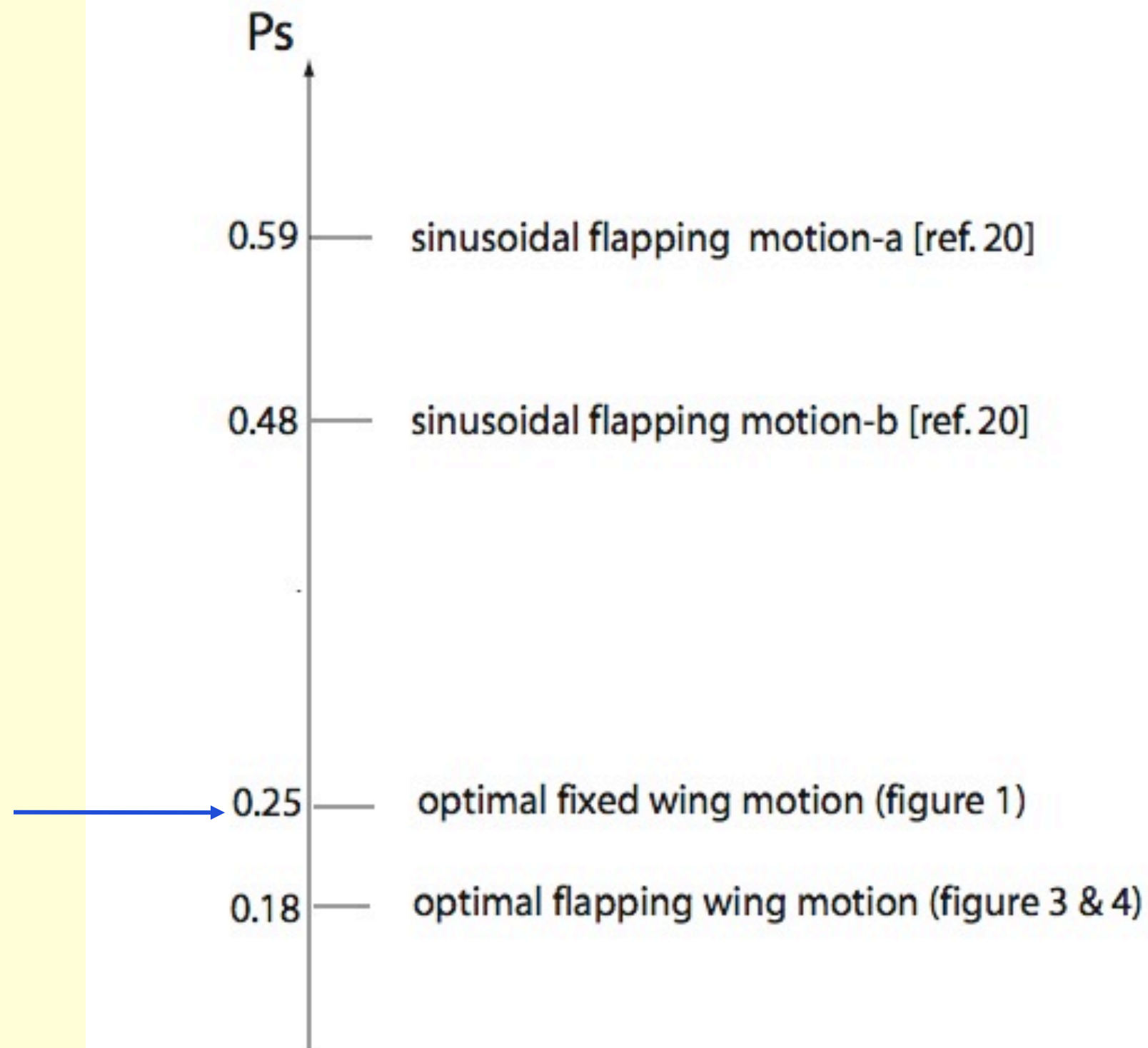


that minimize the aerodynamic power to support the weight

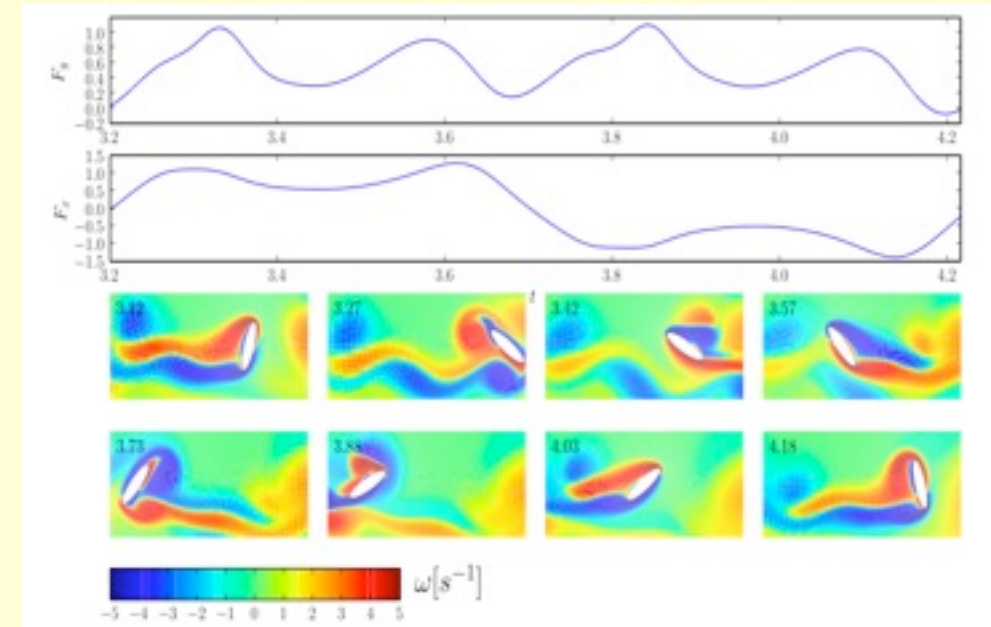
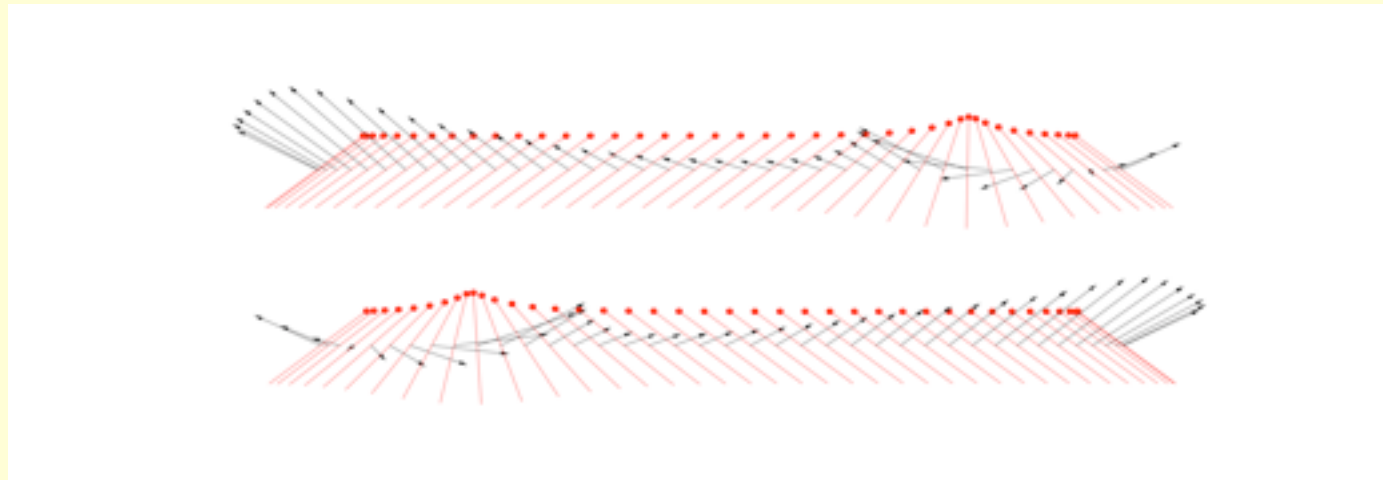
Constrained PDE/ODE optimization



# Specific Power

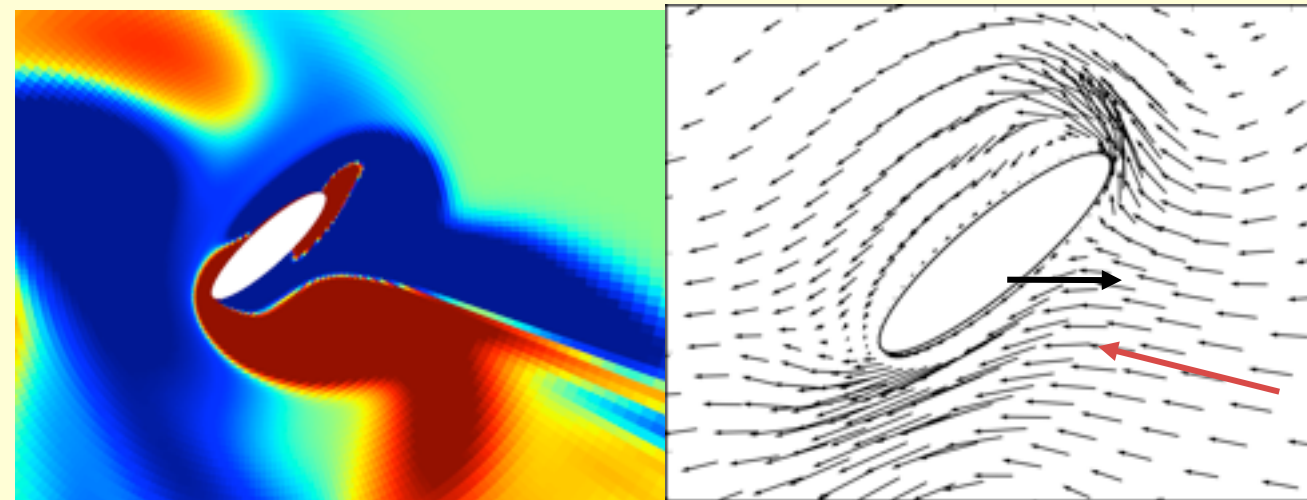


# Optimal Flapping Motion

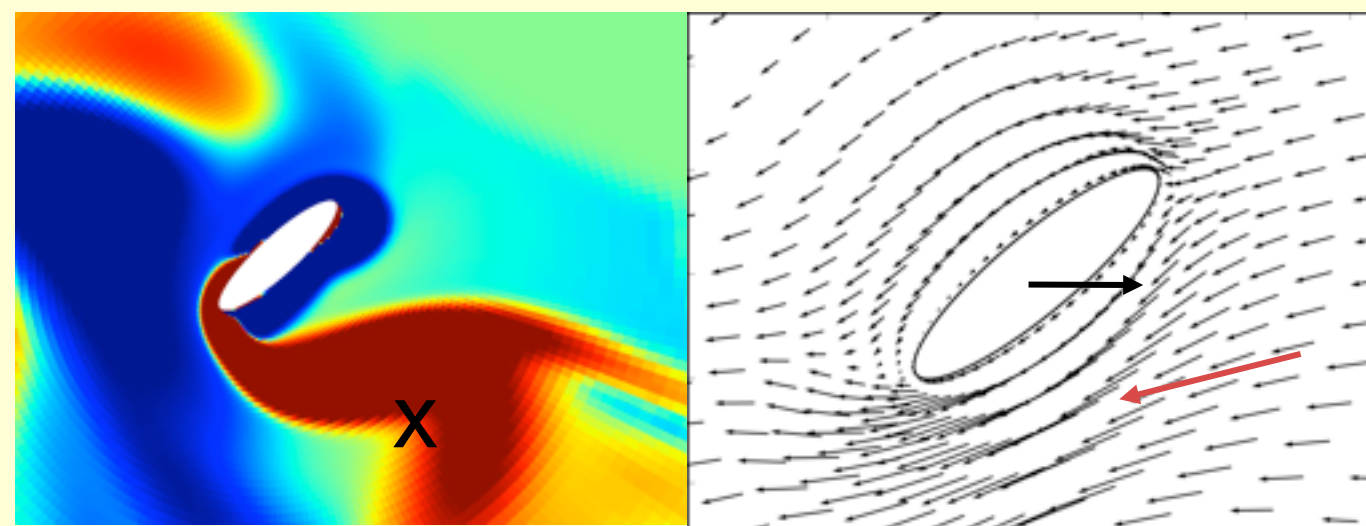


Near  
wing reversal:

Unperturbed case:



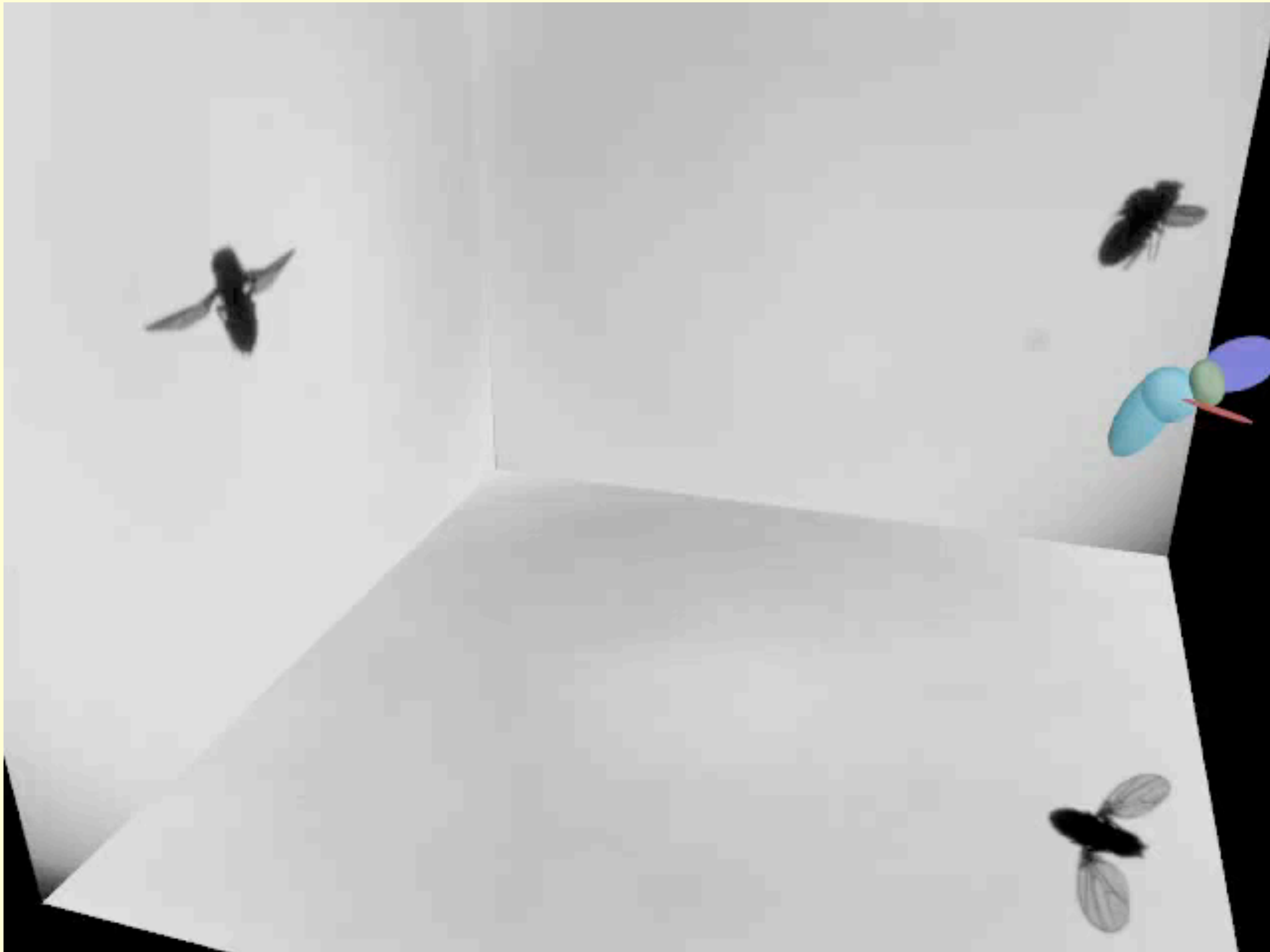
Remove the leading edge vortex in previous half-stroke:



# Taking It Apart

- I. Kinematics
- II. Aerodynamics and Computational Methods
- III. Energetics and Optimization
- IV. Dynamics and Control
- V. Stability and Control

# How do fruit flies control their wings to Turn?





# sensory feedback loops

mechanical

visual

...

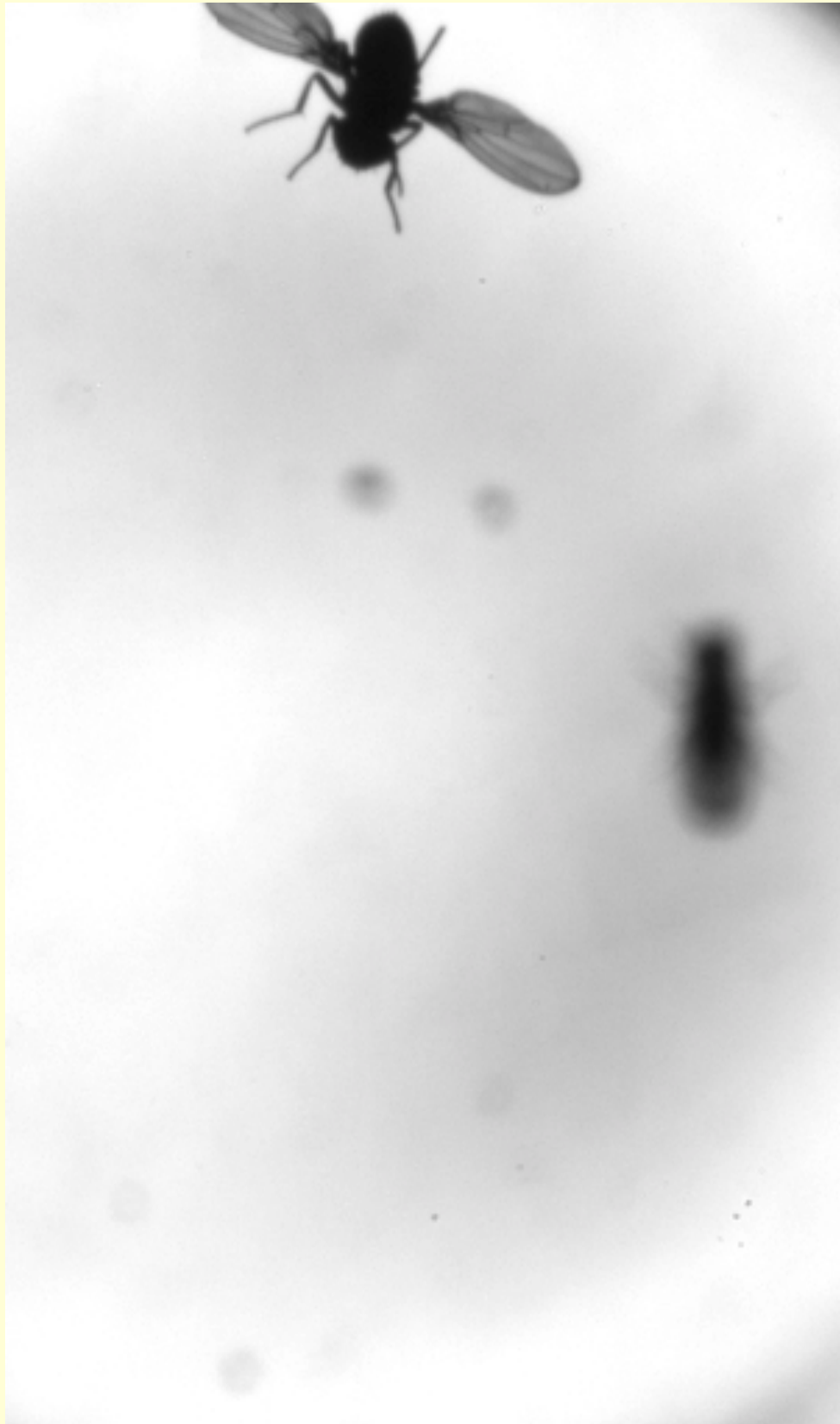
## time scales

fast compared to ?

slow

# Perturbed by Magnetic Field

top view



Start

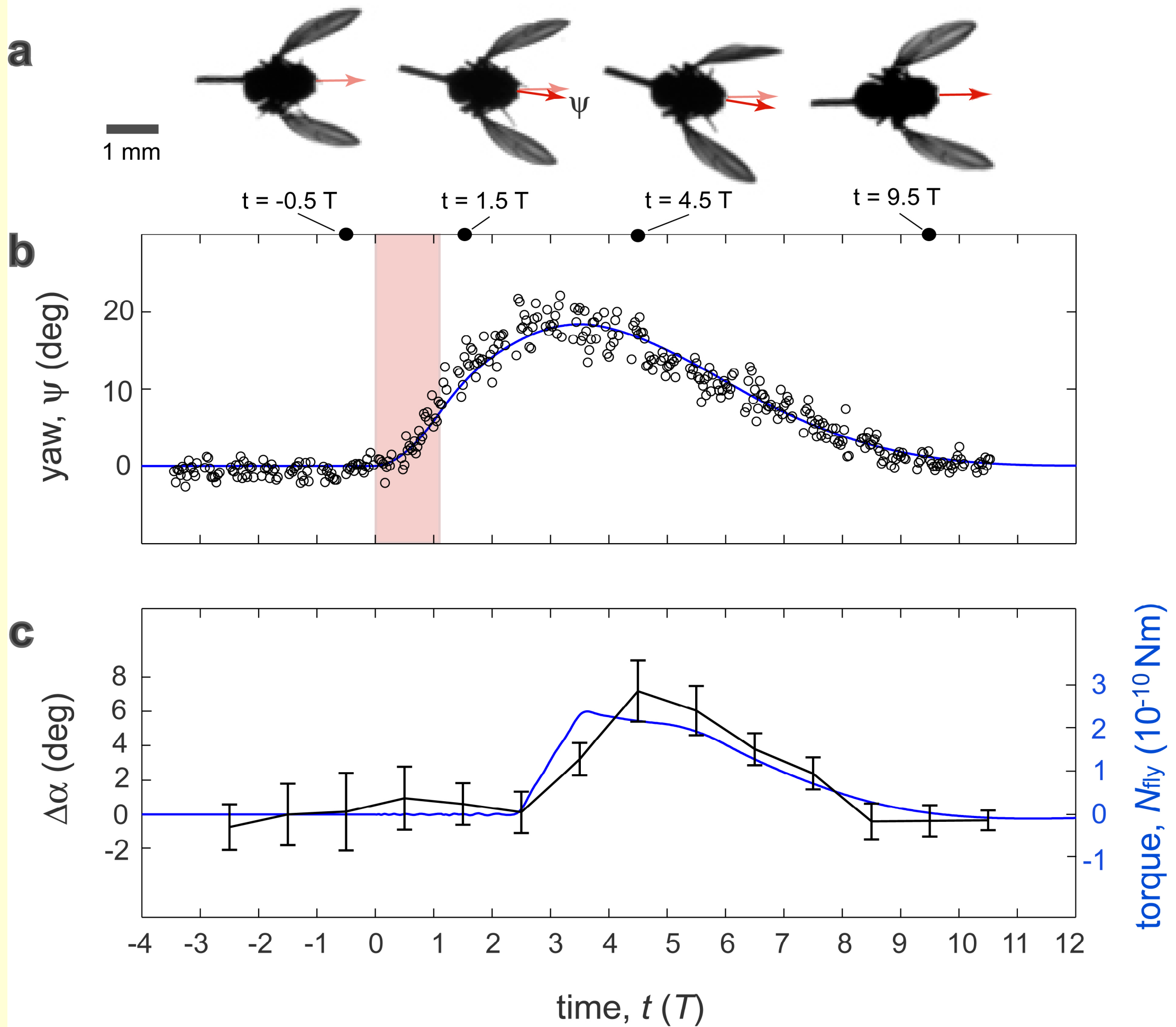


finish



Reset  
orientation

Ristroph et al, PNAS (2010)



# Recovering from an Aerial Stumble

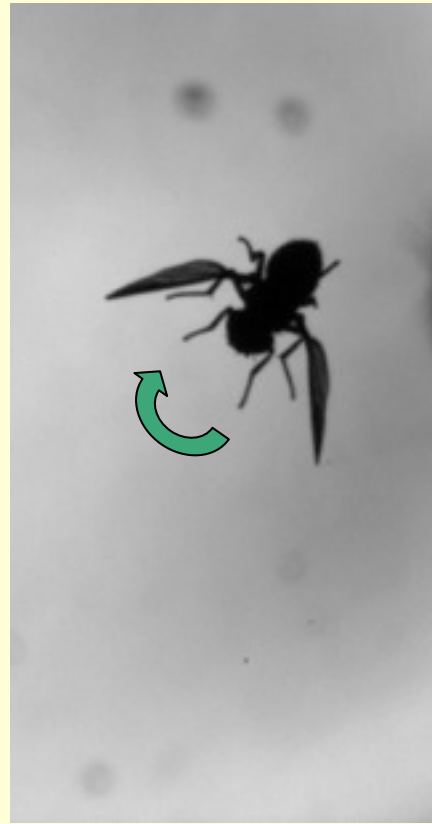
top view



Before  
perturbation

Symmetric  
wing motion

~ 4 wing beats

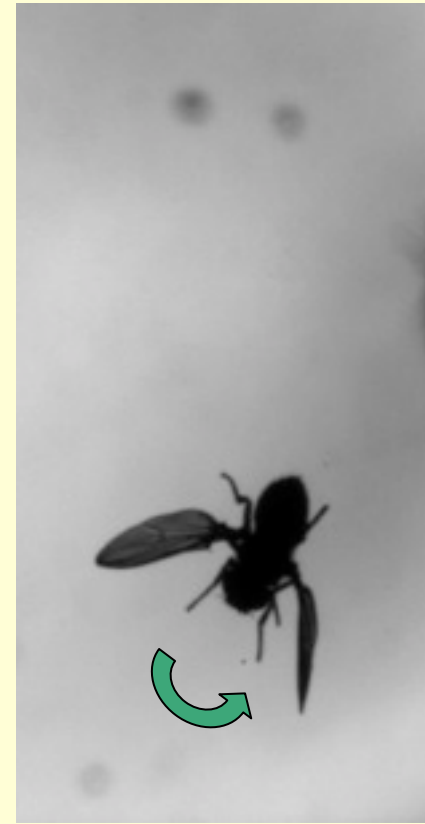


Passive  
damping

①

Symmetric

~ 4 wing beats



Active  
recovery

②

Asymmetric

~ 2 wing beats



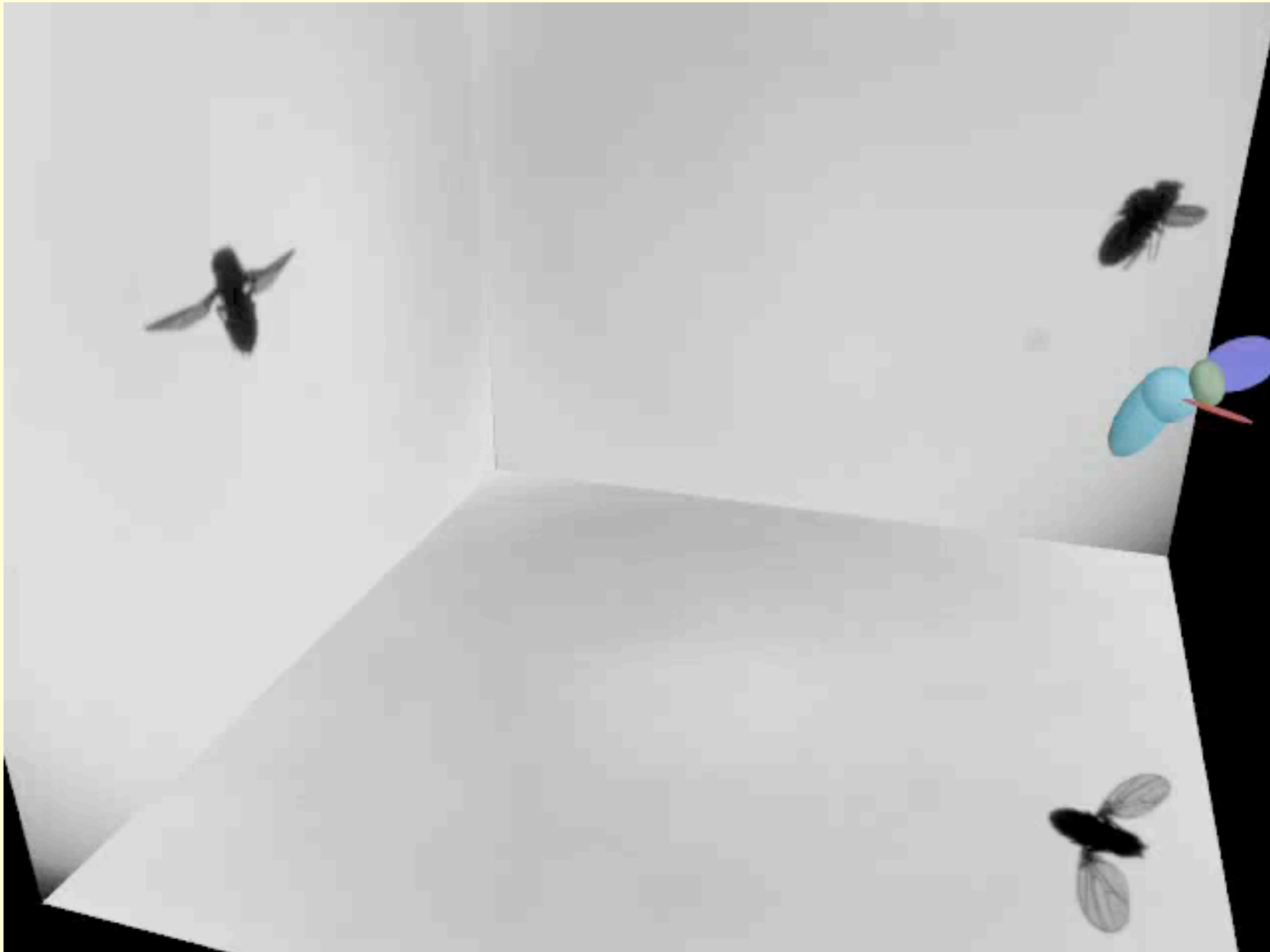
Passive  
recovery

③

Symmetric



# How do fruit flies control their wing to Turn?



# How does the insect control its wings to create these asymmetries?



Back and forth motion:

Driven by large indirect muscles

Pitching:

Controlled by steering muscles

However,  
the insect cannot adjust the wing stroke  
every wing beat (4ms)

# Inferring (Pitching) Torque

**Measure** wing kinematics  
wing mass, shape, axis of rotation

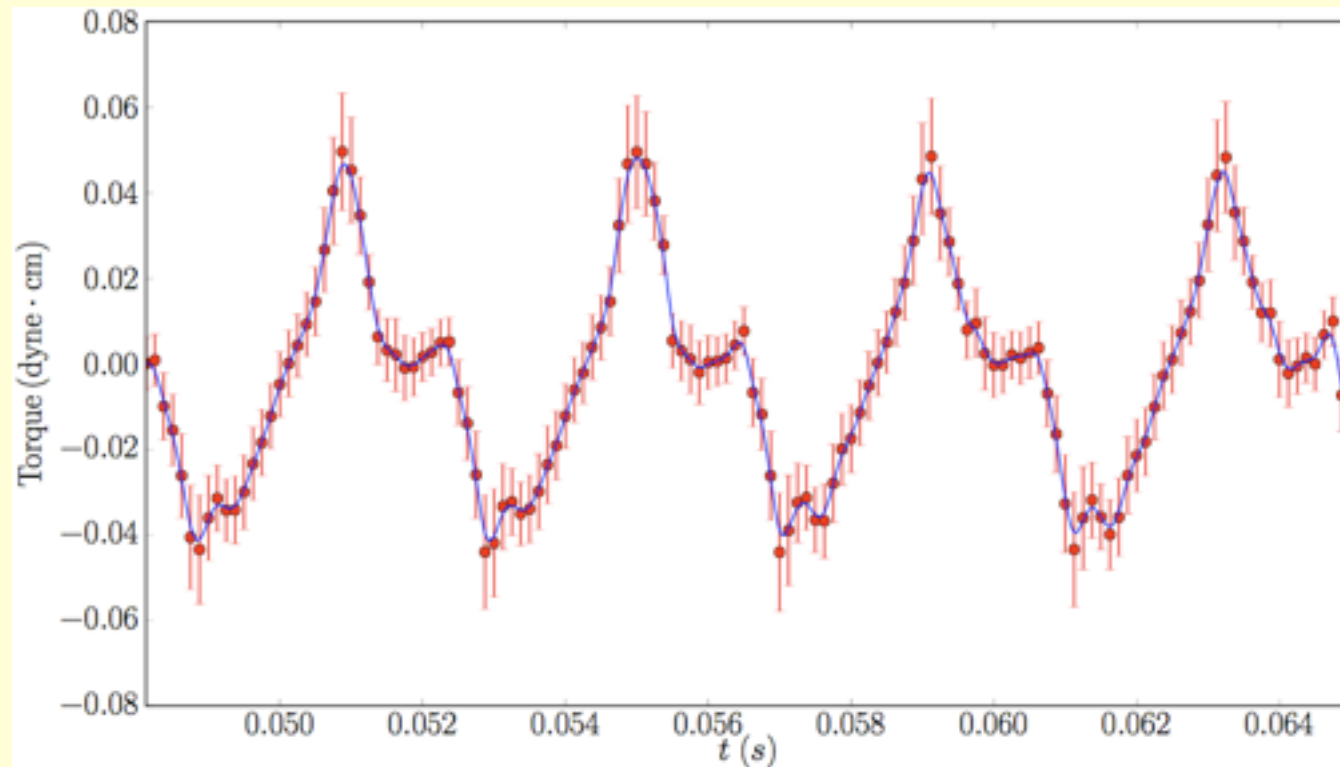
**Calculate** aerodynamic torque  
wing inertia

**Deduce** torque at the wing base

$$\vec{\tau}^{\text{fly}} = \mathbf{I}_{\text{cm}} \cdot \dot{\vec{\omega}} - \vec{r}_{\text{b}} \times m_{\text{w}} \vec{a}_{\text{cm}} + (\vec{r}_{\text{b}} - \vec{r}_{\text{c}}) \times \vec{F}^{\text{aero}} - \vec{\tau}^{\text{aero}}$$

# Torsional Spring at the Wing Base

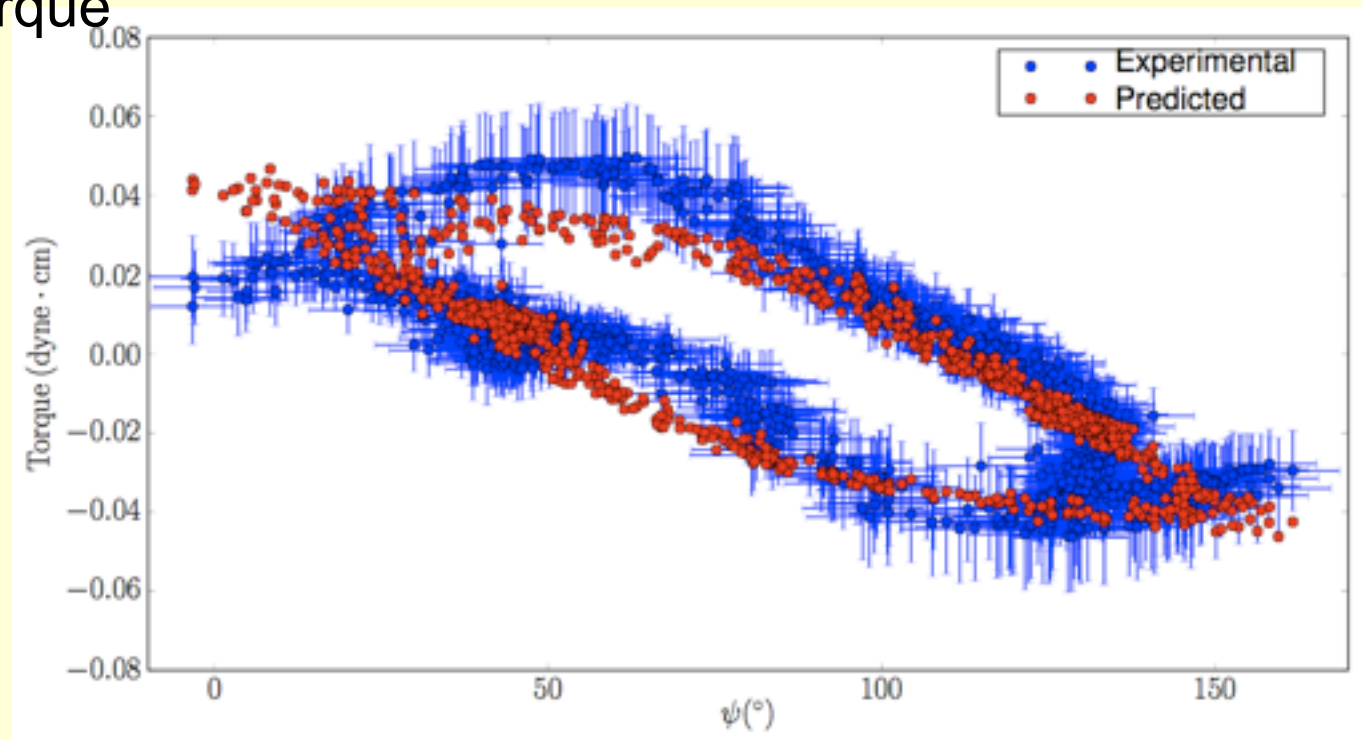
torque



time

$$\vec{\tau}^{\text{fly}} = -\kappa(\psi - \psi_0) - C\dot{\psi}$$

torque

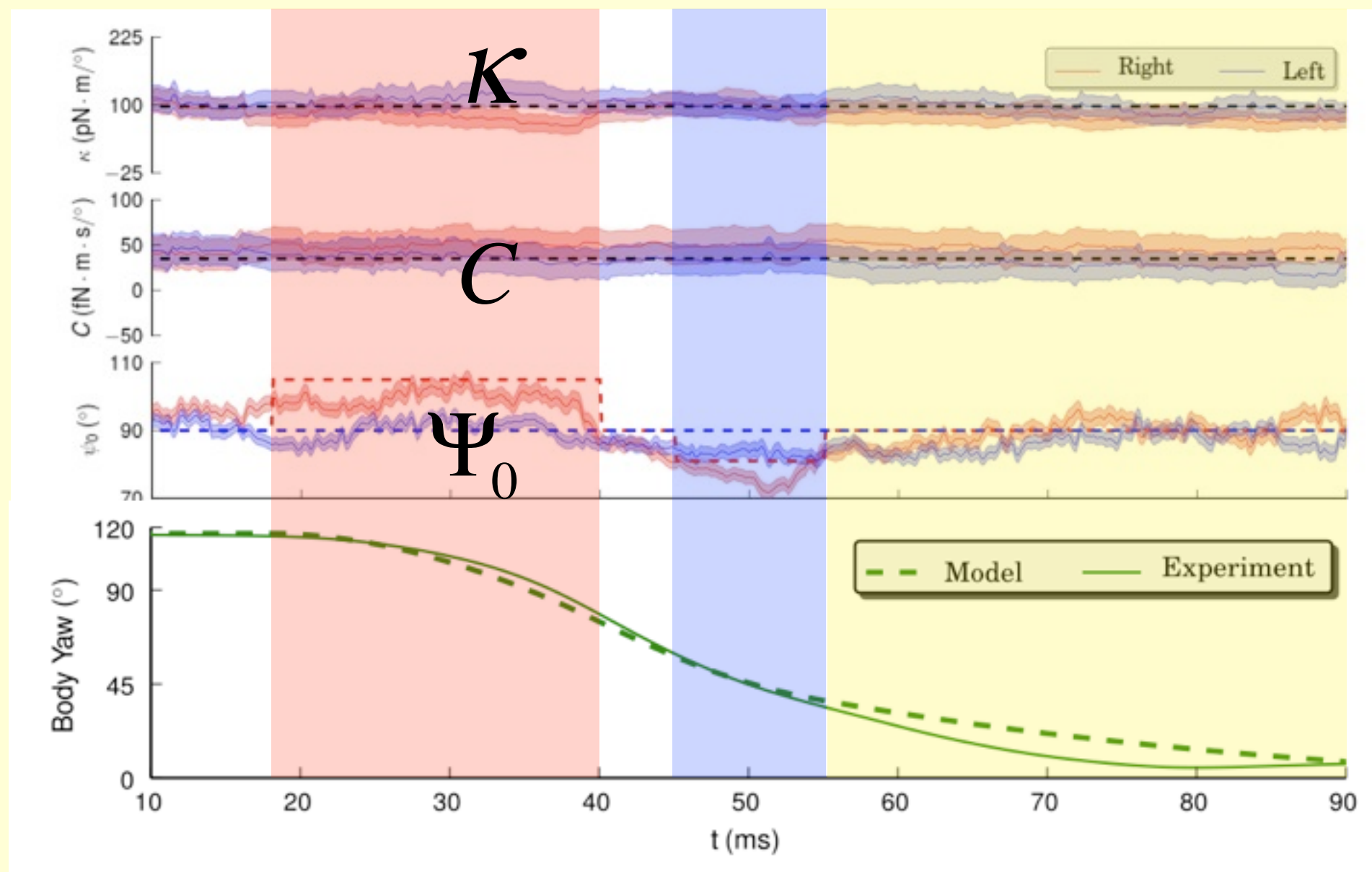


pitching angle

$$\kappa \sim 3 \text{ to } 5 \cdot 10^{-2} \text{ dyne cm/rad}$$

# Determining $\kappa, \Psi_0, C$ from experimental data

$$\vec{\tau}^{\text{fly}} = -\kappa(\psi - \psi_0) - C\dot{\psi}$$



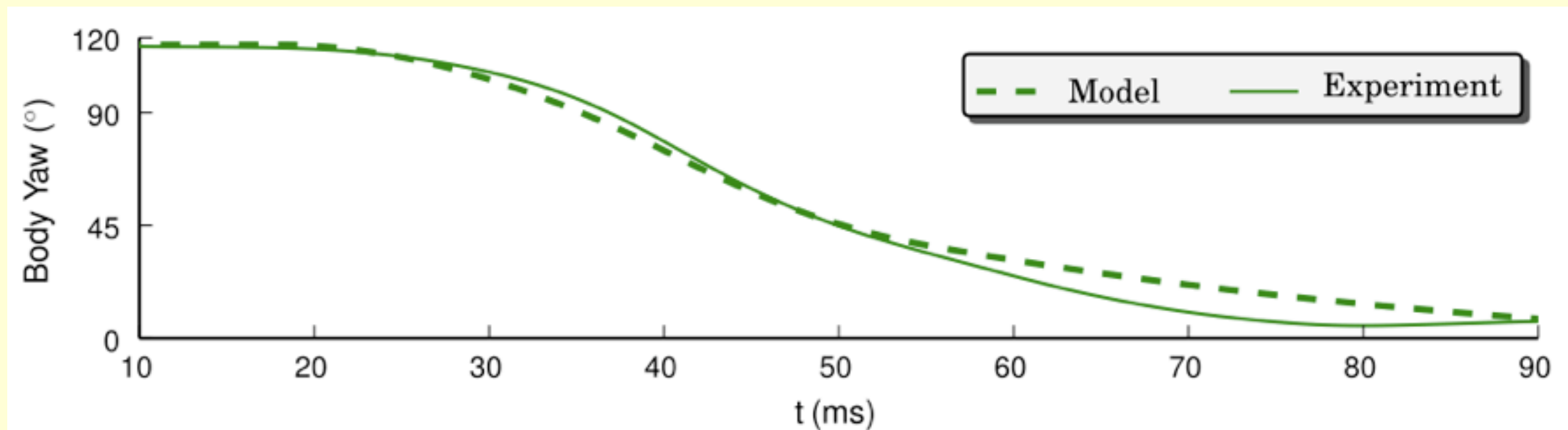
$\Psi_0$   
changes  
over a times  
scale of  
~20ms



# Predicts Body Trajectory

Back and forth motion: prescribed

Wing pitch: passive with one control variable



$$I_b \ddot{\phi}_b + \underbrace{2C_\tau \bar{\omega}}_{\text{damping}} \dot{\phi}_b = \underbrace{2C_\tau \bar{\omega}^2 \Delta\psi}_{\text{driving}}$$

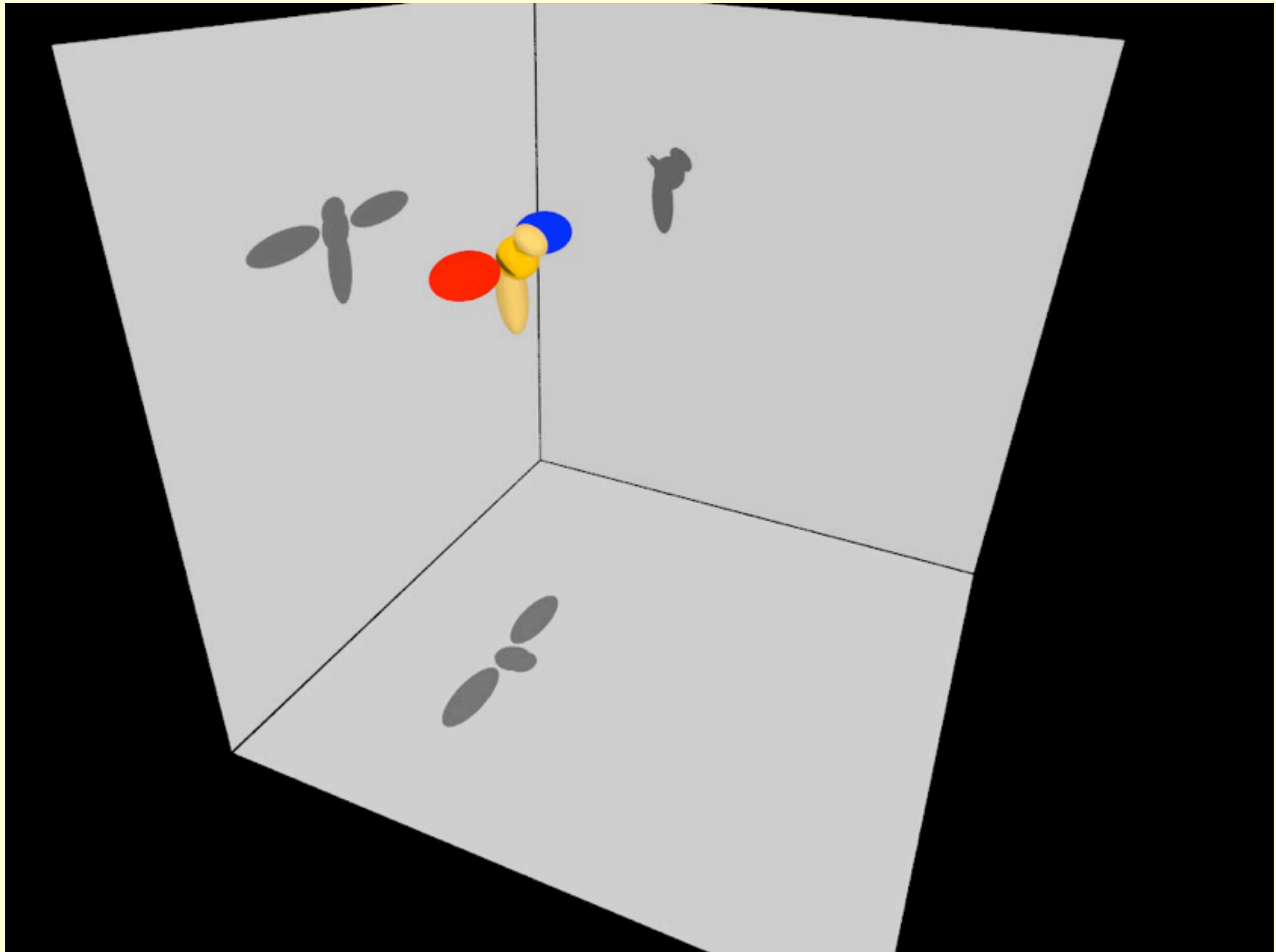
damping

driving

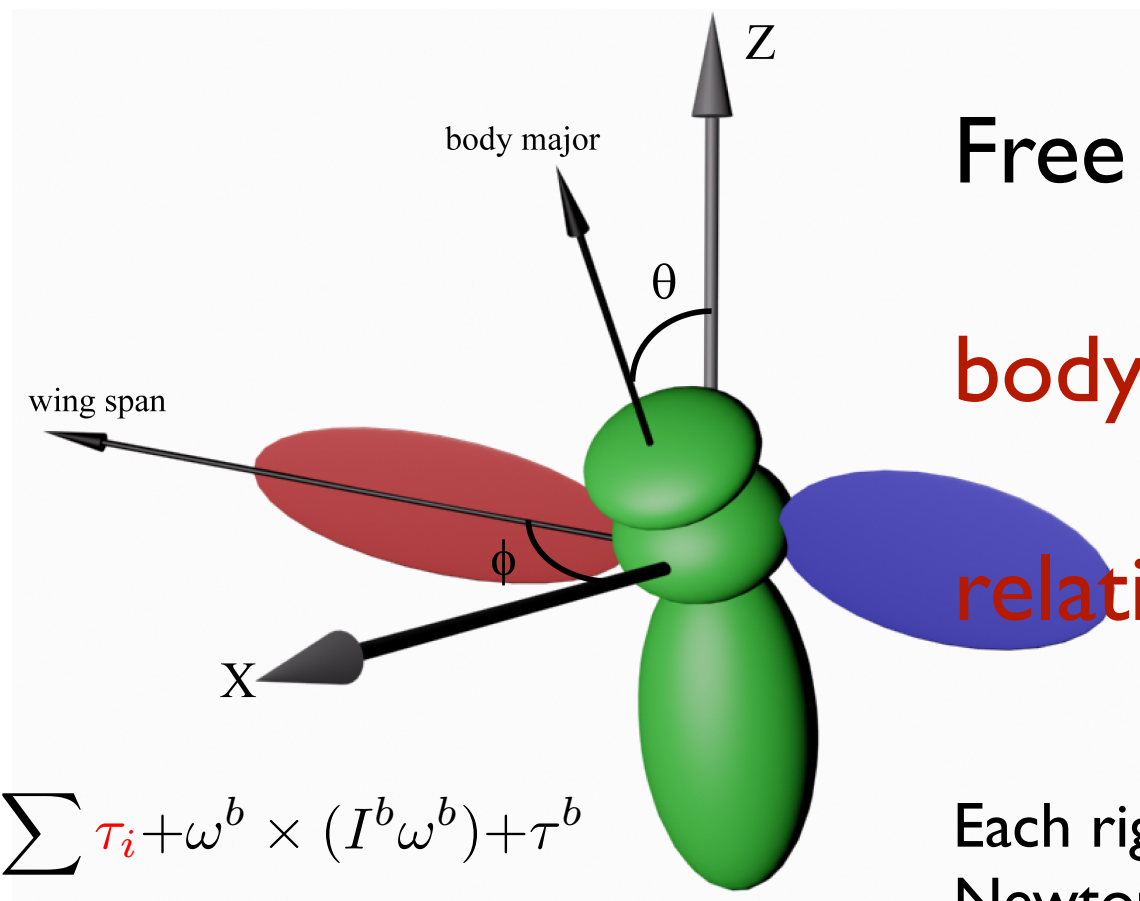
Bergou, Ristroph, Guckenheimer, Cohen, Wang, Phys. Rev. Lett. 2010

# Balancing in Air

# Flapping Flight is almost always unstable



# Dynamic Stability Analysis of Free Flight



Free Flight Simulation

body-wing coupling

relatively fast simulations

$$I^b \dot{\beta}^b = \sum \tau_i + \omega^b \times (I^b \omega^b) + \tau^b$$

$$I_i^w \dot{\beta}_i^w = (-\tau_i) + \omega_i^w \times (I_i^w \omega_i^w) + \tau_i^b$$

$$\beta_i^w - \beta^b = \beta^{\text{pre}}$$

$$m^b \dot{a}^b = (\sum f_i) + m^b g + F^b$$

$$m_i^w \dot{a}_i^w = (-f_i) + m_i^w g + F_i^w$$

$$r^b + r_i^b = r^w + r_i^w$$

Each rigid body satisfies the Newton-Euler Equation.

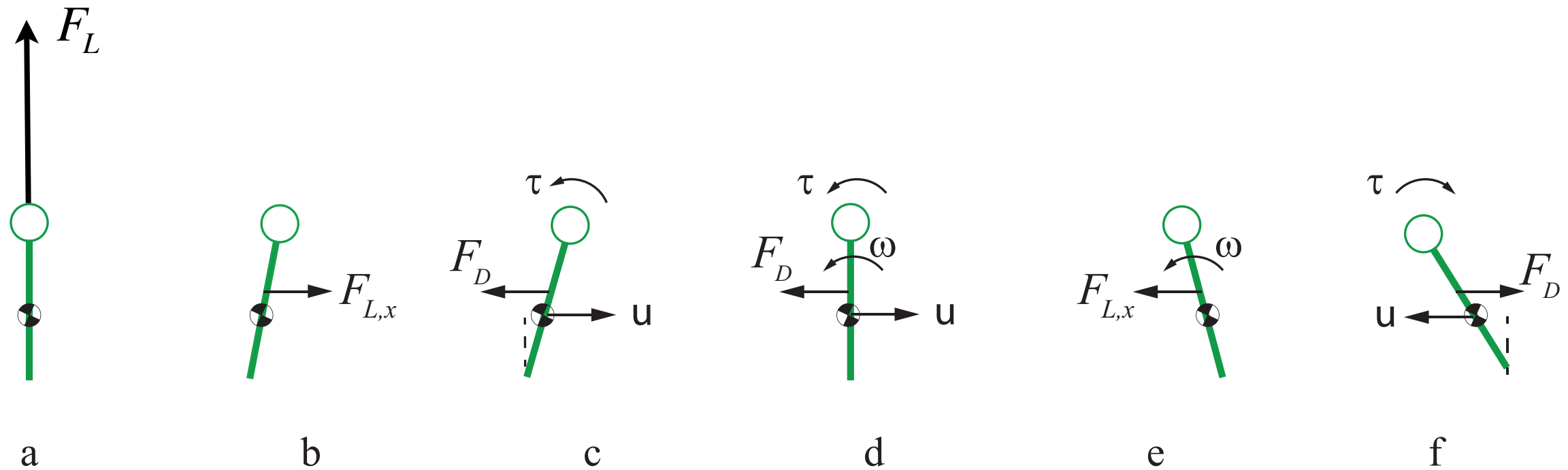
The coupling is enforced through the dynamic constraints at the joints.

Morphological parameters based on insects

The aerodynamics are approximated by a quasi-steady model.

# Pitching Instability

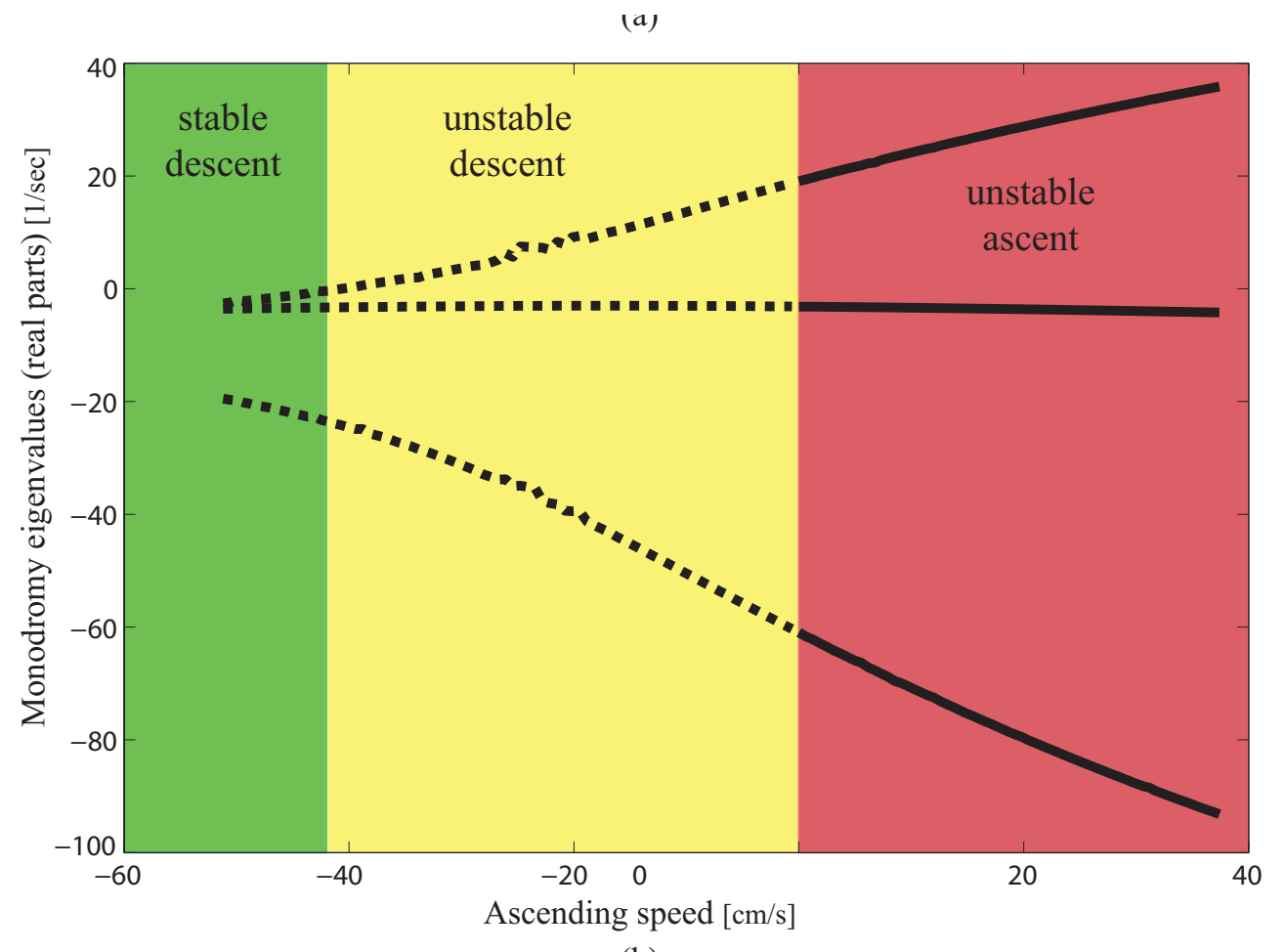
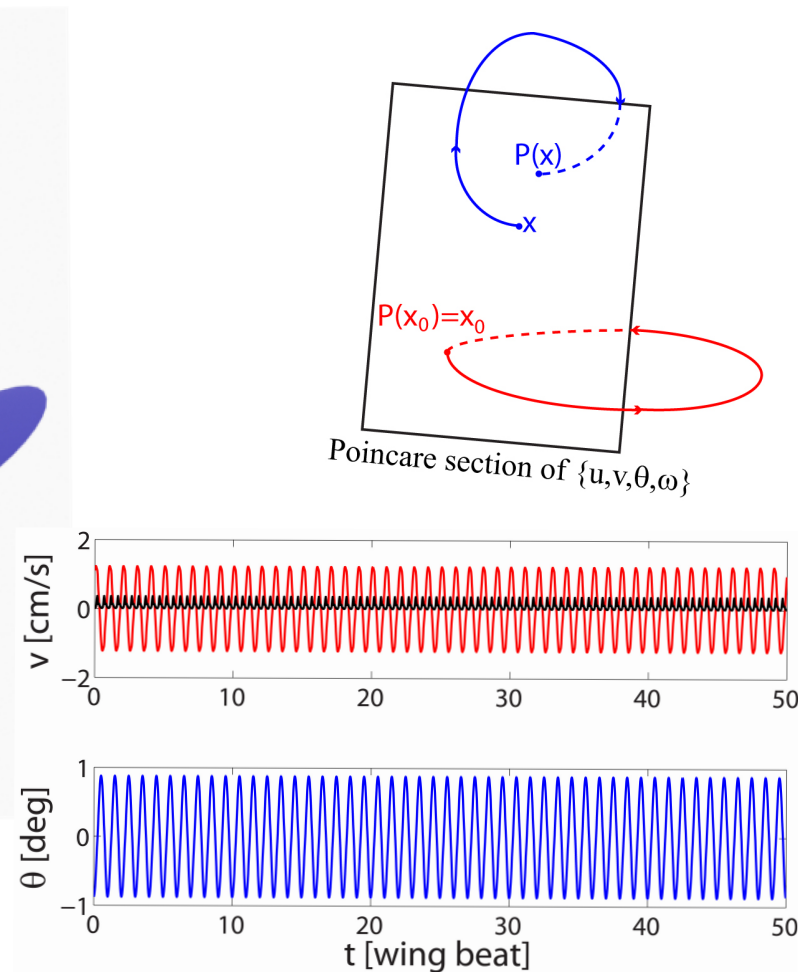
due to coupling between forward and pitching motion





# The Stability of the Periodic States

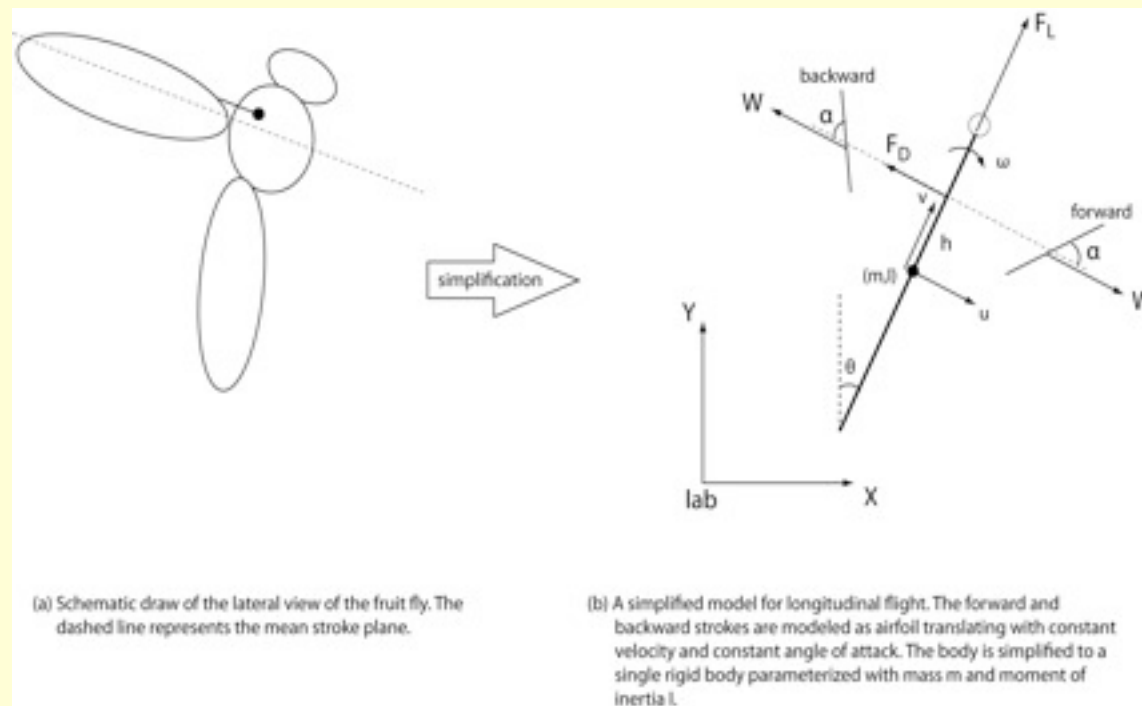
## Eigenvalues based on Poincare Map



Always unstable, unless in fast descent.

In contrast, ascending model excluding the pitching motion, the flight is stable

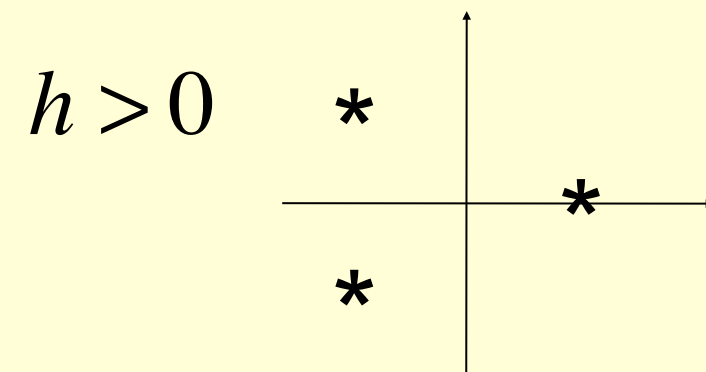
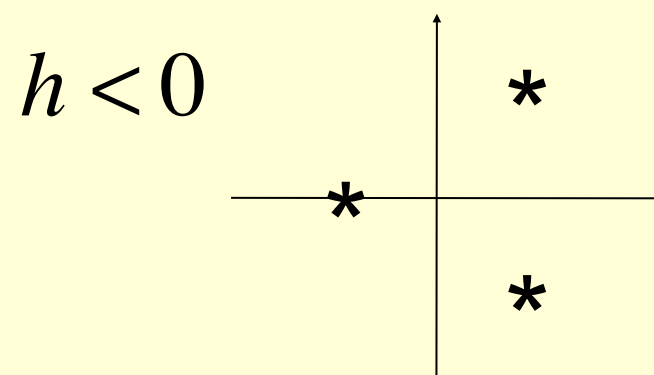
# Linear Stability Analysis of the Longitudinal Flight $(\theta, \dot{\theta}, u)$



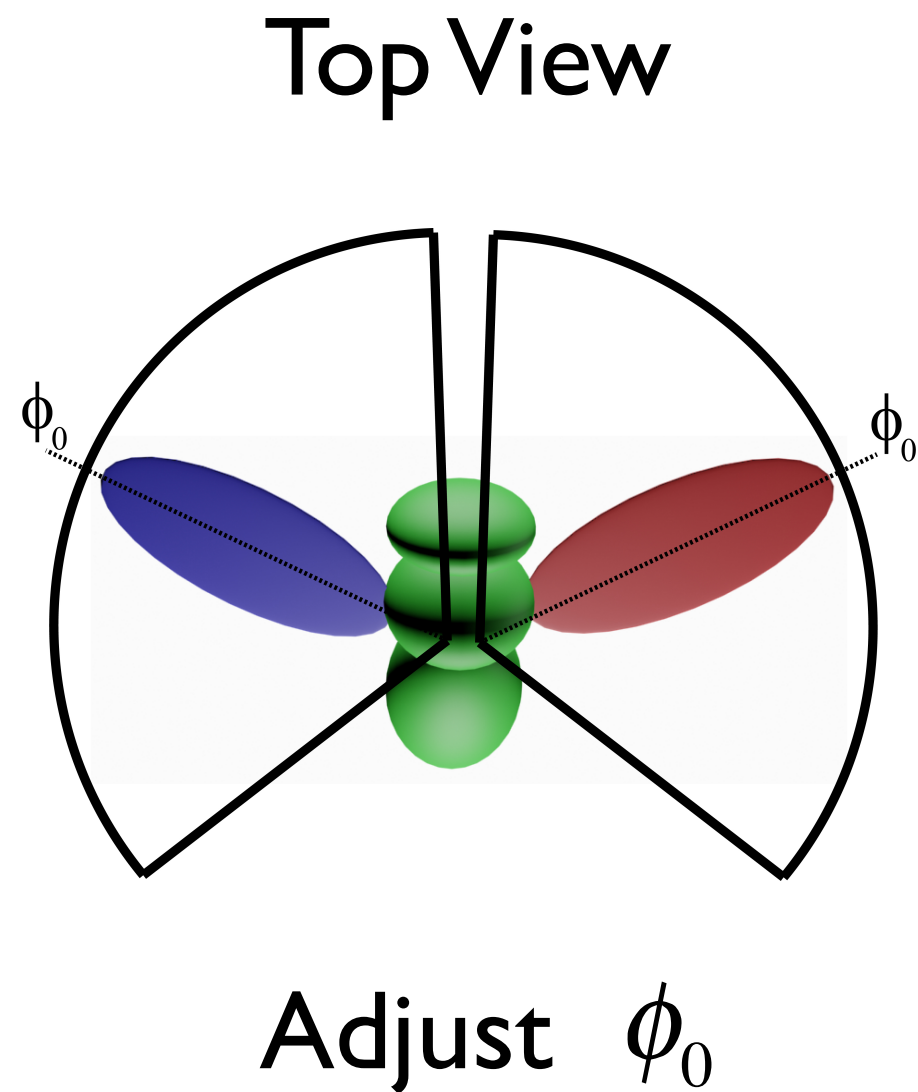
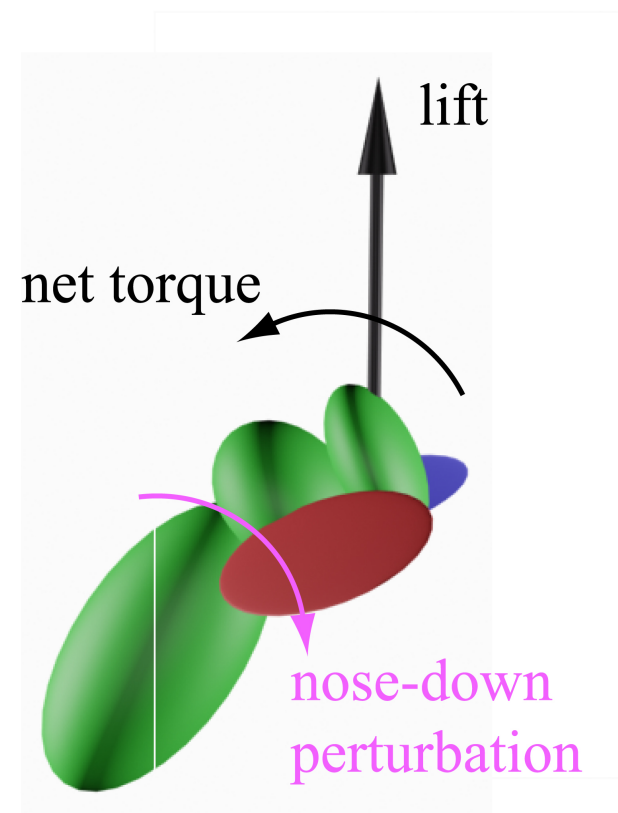
$$\begin{aligned}\dot{u} &= \omega v + \frac{1}{m} F_\xi + g \sin \theta \\ \dot{v} &= -\omega u + \frac{1}{m} F_\zeta - g \cos \theta \\ \dot{\theta} &= \omega \\ \dot{\omega} &= \frac{h}{I} F_\xi\end{aligned}$$

$$\lambda^3 + 2a\lambda^2 + 2ah/L = 0$$

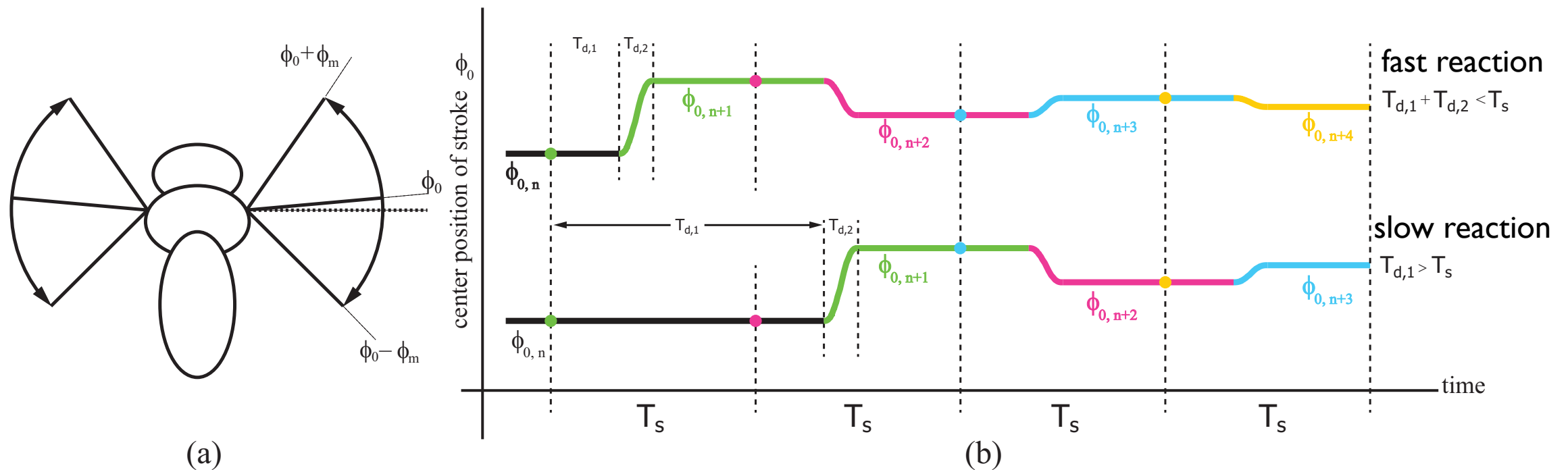
Eigenvalues:



The pitch instability can be controlled by adjusting the center of the stroke  $\phi_0$



# Designing a linear controller

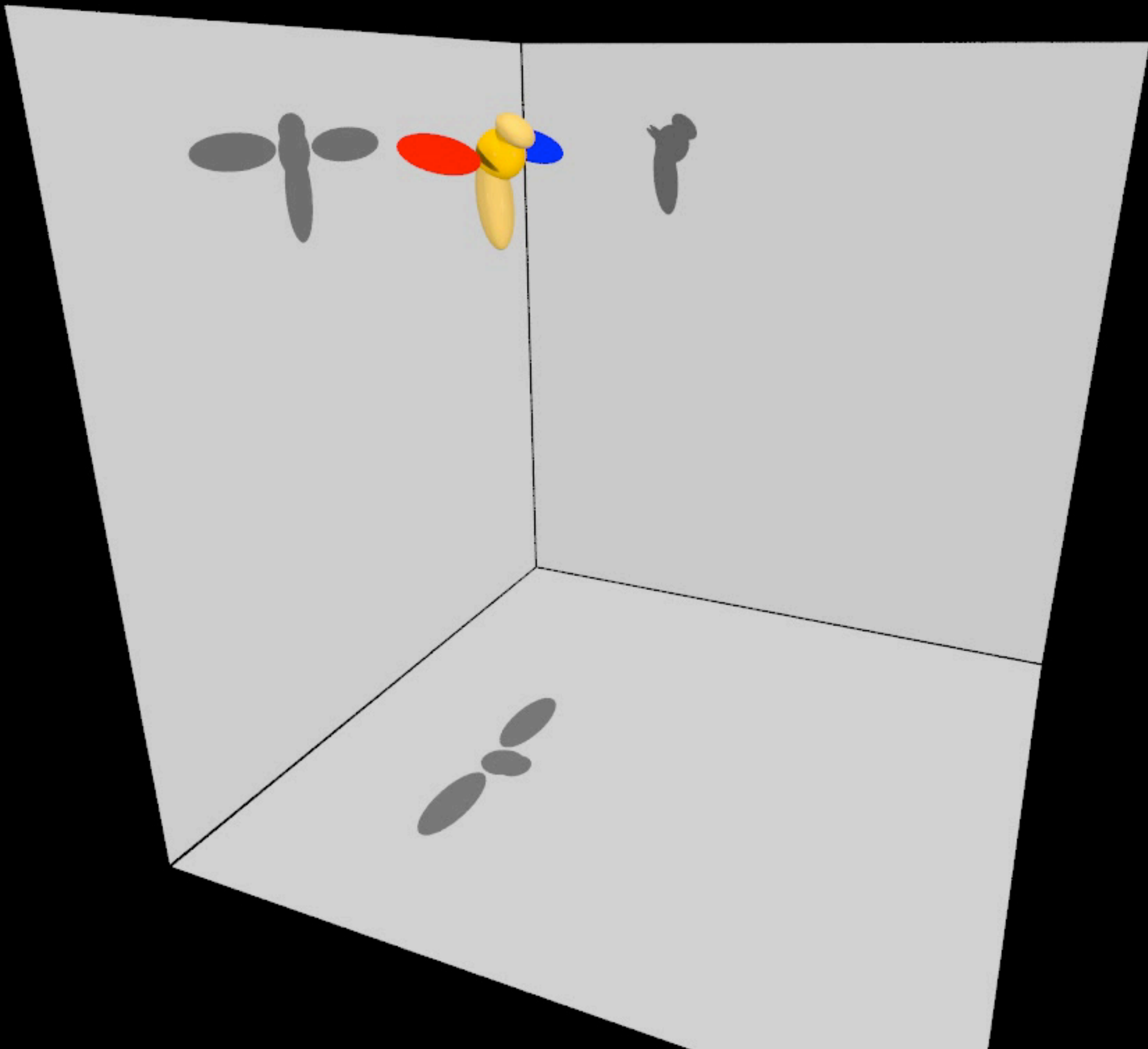


I. time-delay (due to sensing and actuation time)  $T_d$

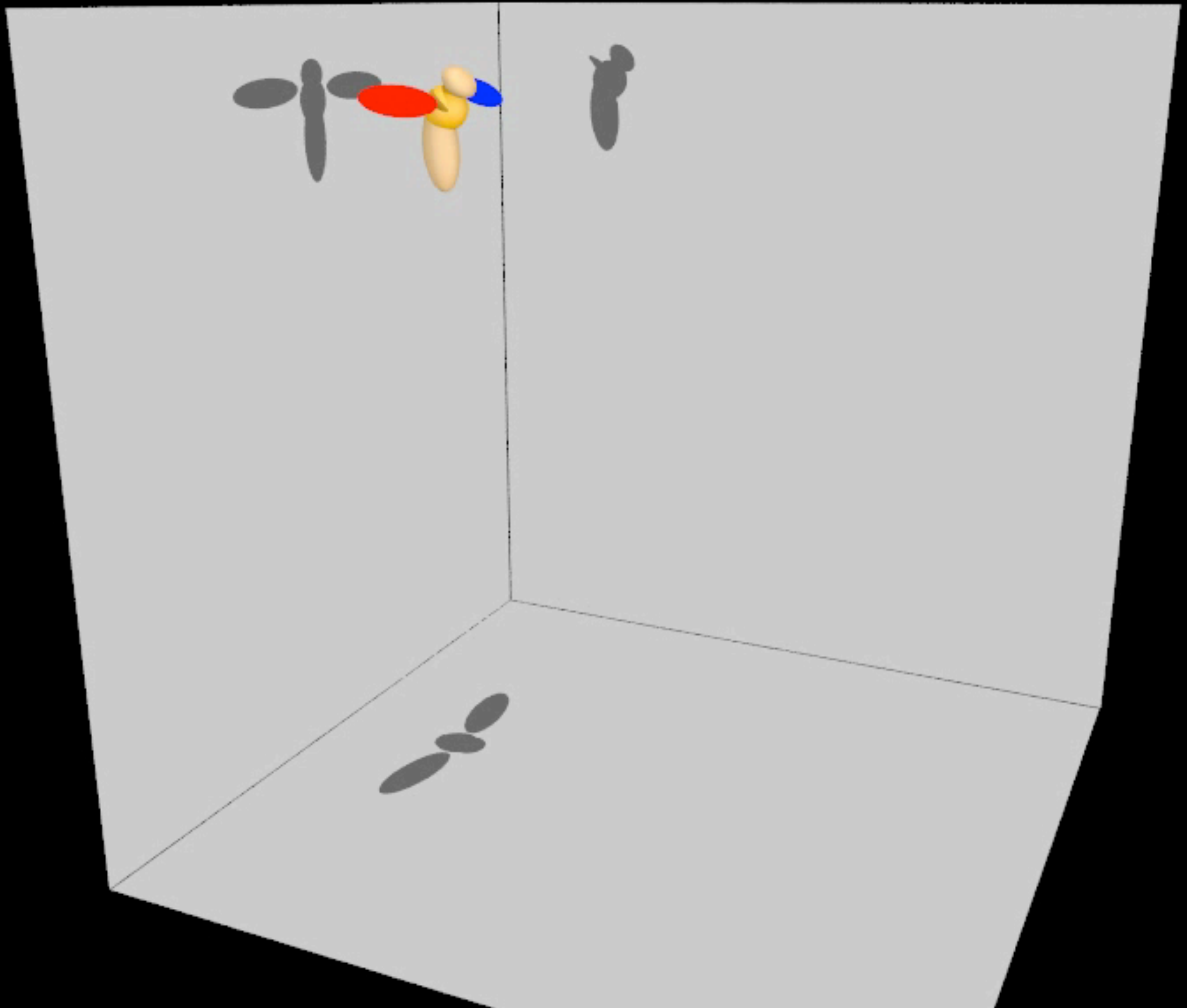
II. discrete sampling rate  $\tau_n - \tau_{n-1} = T_s$

III. a linear controller

interested in the effect of  $T_d$  and  $T_s$

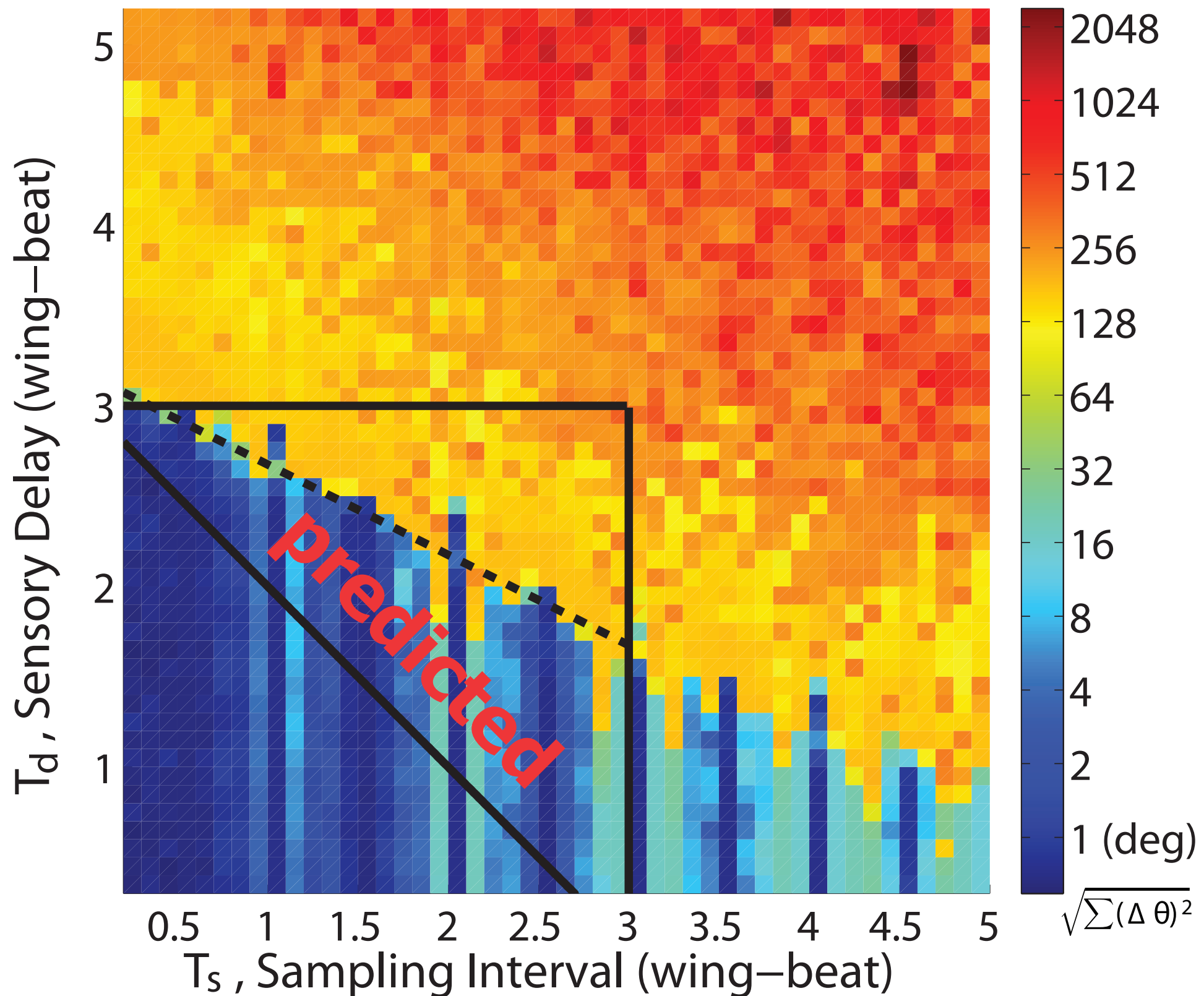






# Predicting Sensing Rate

beat-to-beat sensing to stabilize flight



Chang & Wang, submitted

# Conjecture

Fruit flies sense their state **every wing-beat** in order to stabilize themselves

# Quantitative Study of Organismal Behavior

from flight dynamics to neural dynamics

