

# Simple models of teens, diplomats, religious cults and more

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KTH, CSC, Computational Biology

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<http://www.csc.kth.se/~pholme/>

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and more

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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

simple mechanistic models of the micro- to macro-transition in networked social systems (toy models), of:

- group formation *w Andreas Grönlund*
- youth subcultures *w Andreas Grönlund*
- co-evolution of networks and opinions *w Mark Newman*
- agents maximizing centrality & minimizing degree *w Gourab Ghoshal*

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religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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PETTER  
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formation

youth  
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coevolution of  
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Simple  
models of  
teens,  
diplomats,  
religious cults  
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PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
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PETTER  
HOLME

group  
formation

youth  
subcultures

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networks and  
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- *macro phenomena*: subcultures & other distinct social groups in social networks
- *micro process*: search for personal identity
- *idea*: modify the “seceder model” [Dittrich *et al.*, Phys. Rev. Lett. **84** (2000), 3205–3208] to a network model

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subcultures

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networks and  
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# the seceder model

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PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
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- $N$  individuals with a real number  $s(i)$  representing the traits of  $i$
- Select three individuals  $i_1$ ,  $i_2$  and  $i_3$  randomly.
- Pick the one of these  $\hat{i}$  whose  $s$ -value is furthest from the average  $[s(i_1) + s(i_2) + s(i_3)]/3$ .
- Replace the  $s$ -value of a random agent  $j$  with  $s(\hat{i}) + \eta$ , where  $\eta$  is a random number from the normal distribution  $N(0, 1)$ .

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HOLME

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youth  
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group  
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PETTER  
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formation

youth  
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teens,  
diplomats,  
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PETTER  
HOLME

group  
formation

youth  
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coevolution of  
networks and  
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# time evolution

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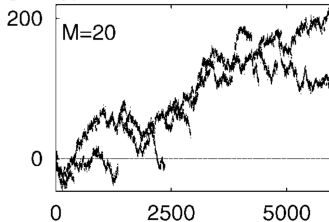
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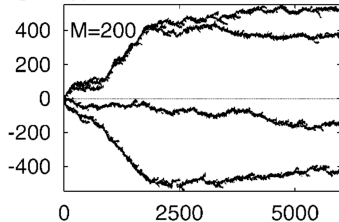
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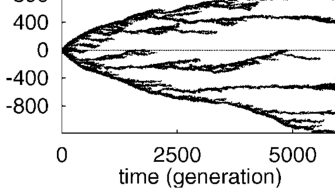
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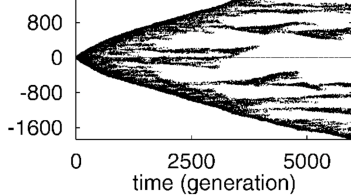
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M=2000



M=20000



# the networked seceder model

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
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- Select three random (but distinct) vertices  $i_1$ ,  $i_2$  and  $i_3$ .
- Pick the one of these with highest eccentricity  $\hat{i}$  (or, if the graph is disconnected, the member of the smallest group with highest eccentricity).
- Pick another random vertex  $j$  in  $V \setminus \{\hat{i}\}$ . Rewire as many of  $j$ 's edges as possible to  $\hat{i}$ .
- Go through all  $j$ 's edges once more and, with a probability  $p$ , rewire these to random others.

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teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

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networks and  
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teens,  
diplomats,  
religious cults  
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PETTER  
HOLME

group  
formation

youth  
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coevolution of  
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teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

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teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

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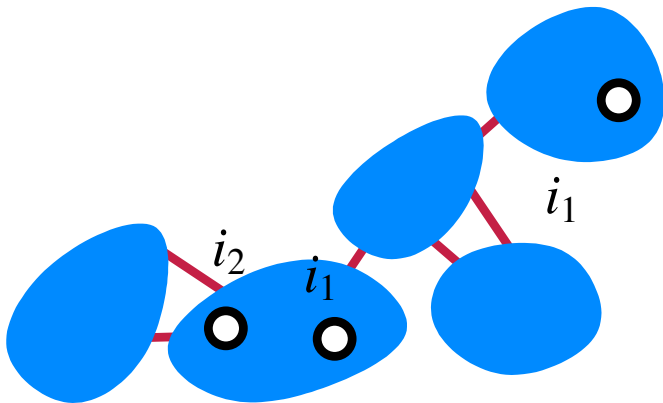
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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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diplomats,  
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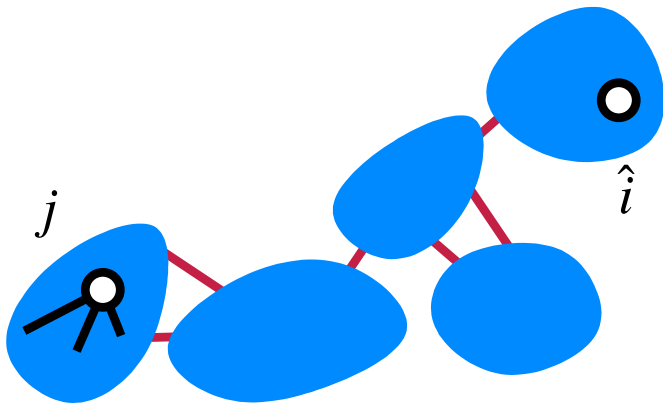
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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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diplomats,  
religious cults  
and more

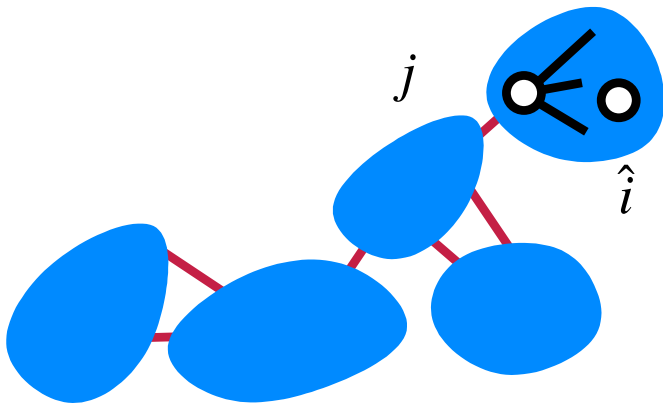
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group  
formation

youth  
subcultures

coevolution of  
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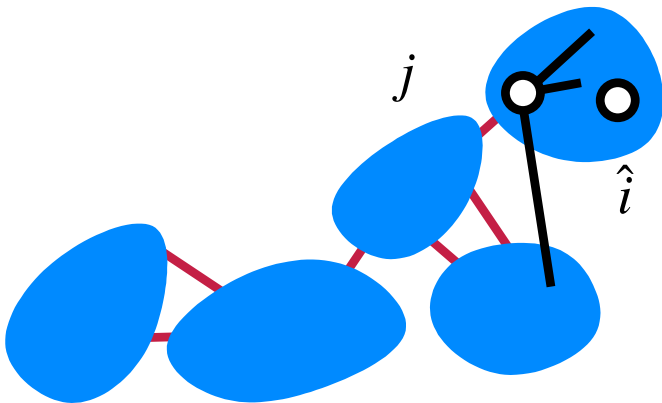
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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



# output: example network

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religious cults  
and more

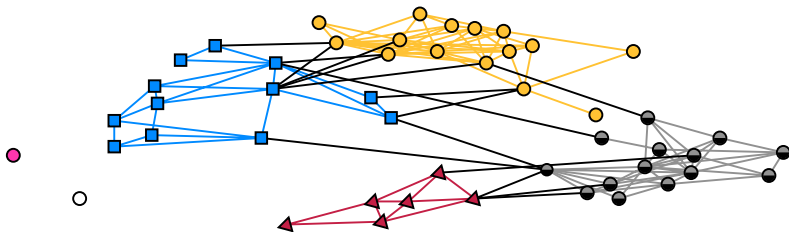
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formation

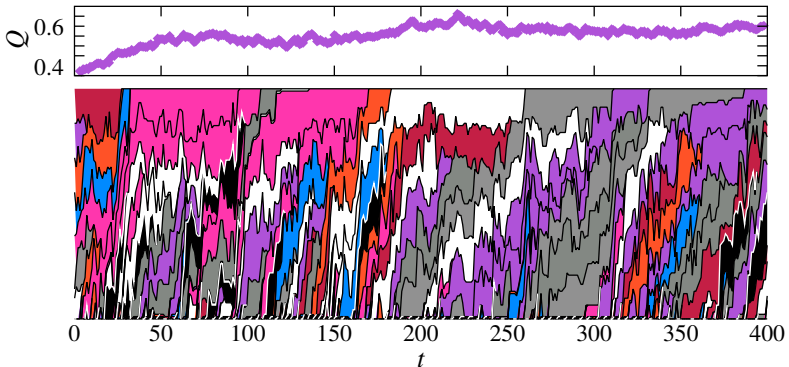
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subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



# output: time evolution



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diplomats,  
religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

# output: parameter dependence

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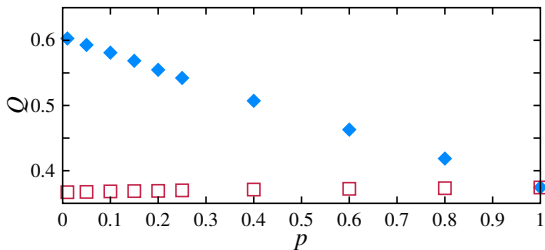
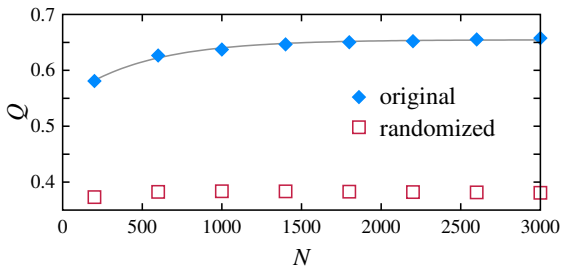
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youth subcultures

coevolution of networks and opinions

the diplomat's dilemma



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teens,  
diplomats,  
religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
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the diplomat's  
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- group formation (the desired qualitative behavior) occurs
- turned an agent-based model of group formation into a network-evolution model
- the original model was simplified, by omitting the explicit trait variable



Simple  
models of  
teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
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# the idea

- to start with documented principles and derive a model for the dynamics of youth subcultures
- turn these observations into a mechanistic model

Simple  
models of  
teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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models of  
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religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

Simple  
models of  
teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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PETTER  
HOLME

group  
formation

youth  
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HOLME

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diplomats,  
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PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

- an adolescent belongs to one subculture at a time
- threshold behavior: if the fraction of friends that have adopted a certain subculture is big enough then an adolescent will adopt that subculture too
- the attractiveness of a subculture decreases with its age
- there is a certain resistance to changing subcultures
- the dynamics of the underlying social network is negligible

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models of  
teens,  
diplomats,  
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PETTER  
HOLME

group  
formation

youth  
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group  
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teens,  
diplomats,  
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PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
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## attractiveness

$$s_c(t, i) = \frac{k}{k_i} n_i(c) \frac{t(c) - t(c_i)}{t - t(c_i)}$$

- where  $t(c)$  is the age of  $c$
- $k = 2M/N$  is the average degree
- $k_i$  is the degree of  $i$
- $n_i(c)$ , the number of neighbors of  $i$  with the identity  $c$

# model definition: iterations

- For every vertex  $i$  (chosen sequentially) calculate the score  $s_c(t, i)$  of all subcultures  $c$ .
- Go through the vertex set sequentially once again. If the score is higher than a threshold  $T$  for some identity  $c$ , then  $i$  change its identity to  $c$ . If more than one subculture has a score above the threshold then the individual adopts the subculture with the highest score.
- With a probability  $R$  a new identity is assigned to a vertex. (On average,  $NR$  fads are introduced per time step.)

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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

# model definition: iterations

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formation

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subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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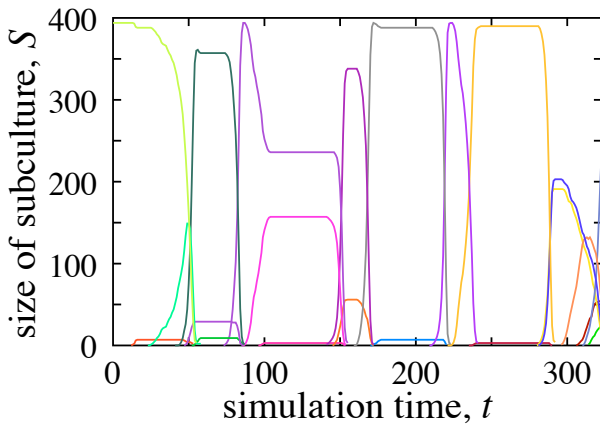
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subcultures

coevolution of  
networks and  
opinions

the diplomat's  
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# output: time evolution



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## output: parameter dependence

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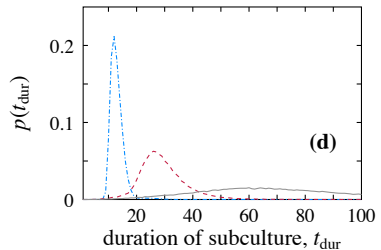
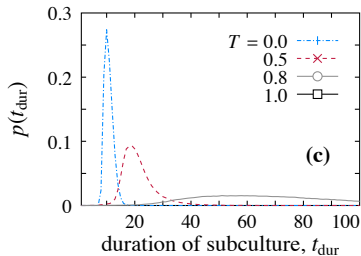
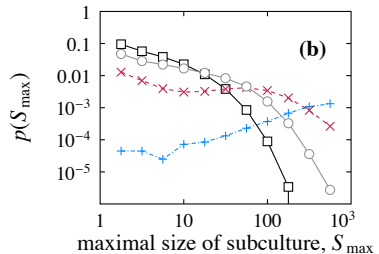
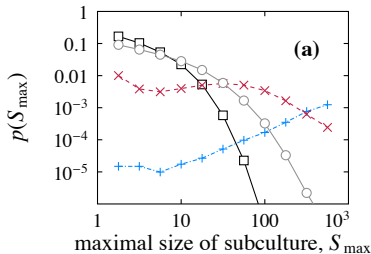
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subcultures

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religious cults  
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formation

youth  
subcultures

coevolution of  
networks and  
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- broad distributions of sizes and durations of subcultures (in agreement with some qualitative statements)

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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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diplomats,  
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and more

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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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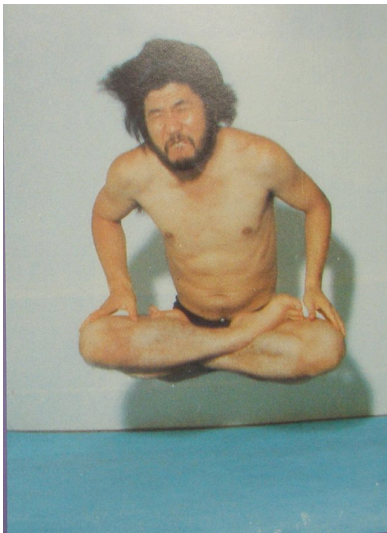
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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma





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teens,  
diplomats,  
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youth  
subcultures

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the diplomat's  
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P. Holme & M. E. J. Newman, Phys. Rev. E **74**, 056108 (2006).

- Opinions spread over social networks.
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- We try to combine these points into a simple model of simultaneous opinion spreading and network evolution.

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group  
formation

youth  
subcultures

coevolution of  
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formation

youth  
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coevolution of  
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the diplomat's  
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youth  
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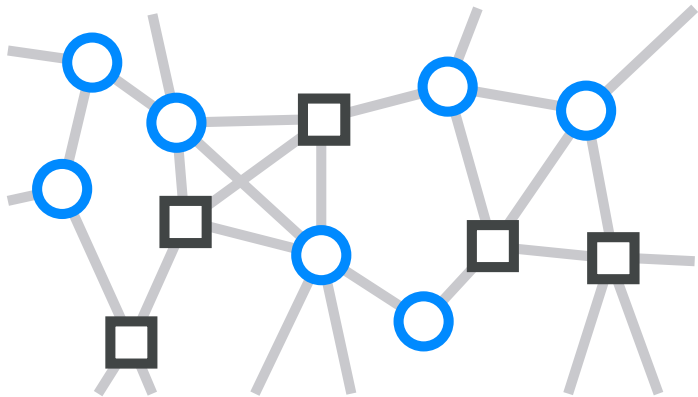
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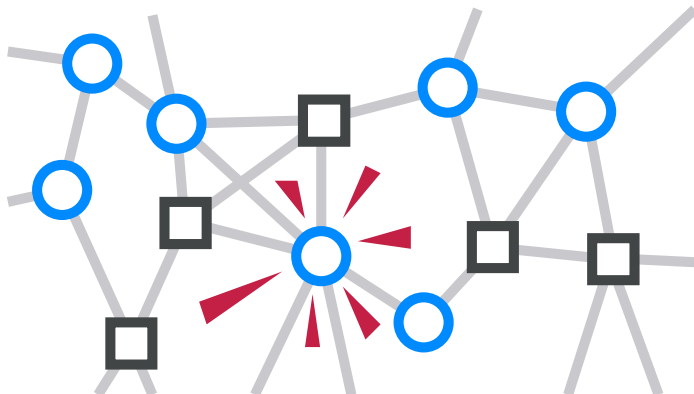
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# the voter model



Clifford & Sudbury, *Biometrika* **60**, 581 (1973).  
Holley & Liggett, *Ann. Probab.* **3**, 643 (1975).

# the voter model



choose one vertex randomly

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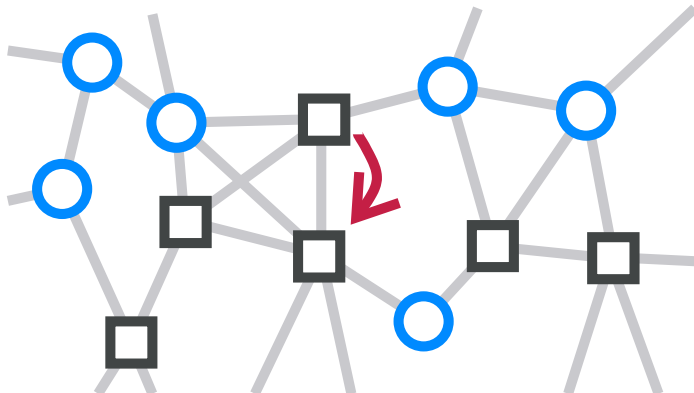
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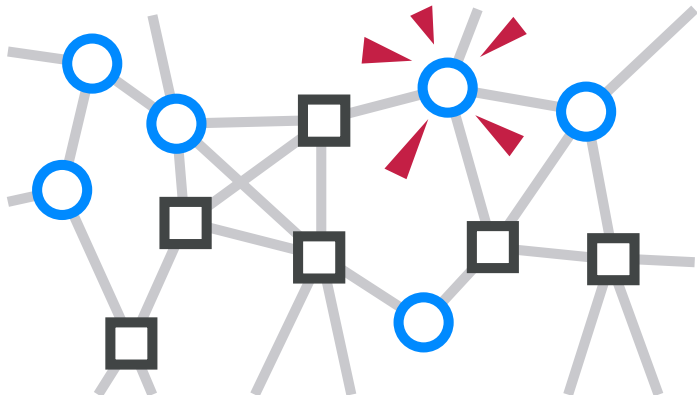
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# the voter model



copy the opinion of a random neighbor

# the voter model



and so on . . .

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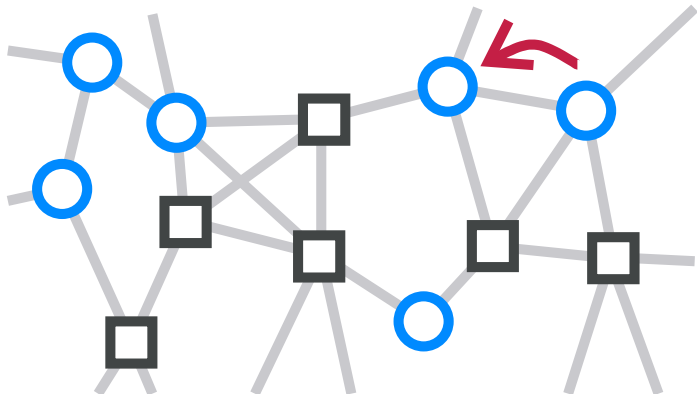
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opinions

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dilemma

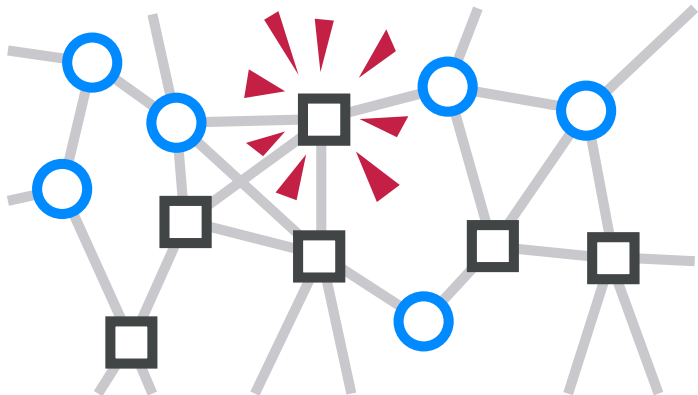


# the voter model



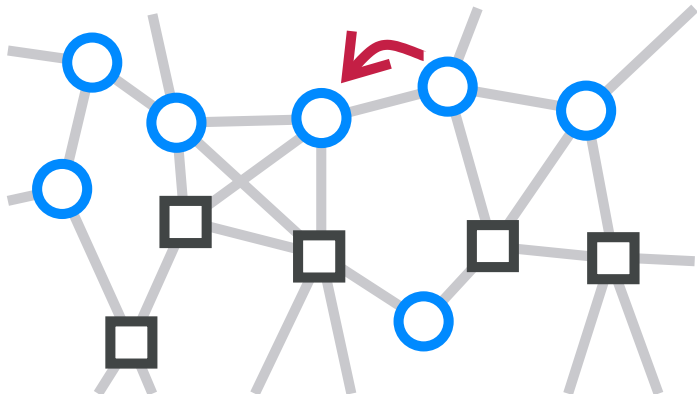
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# the voter model



and so on . . .

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

# acquaintance dynamics: precepts

- People of similar interests are likely to get acquainted.
- The number of edges is constant.

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models of  
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diplomats,  
religious cults  
and more

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HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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models of  
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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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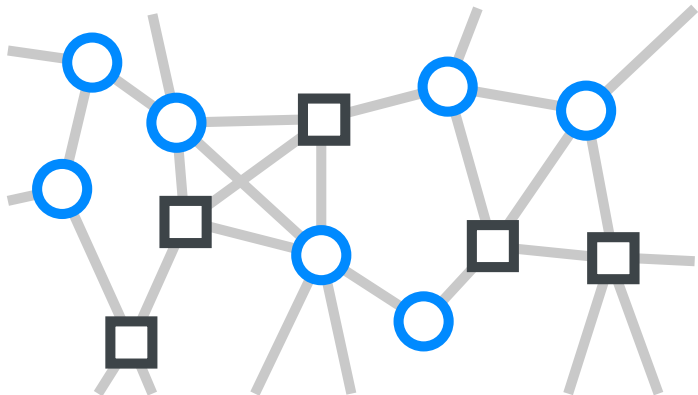
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youth  
subcultures

coevolution of  
networks and  
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the diplomat's  
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group  
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youth  
subcultures

coevolution of  
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opinions

the diplomat's  
dilemma

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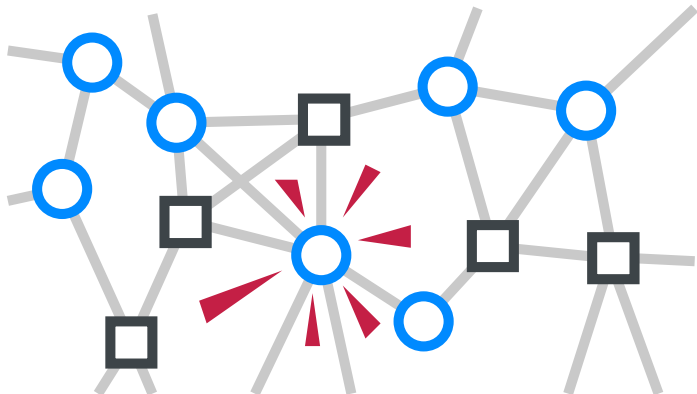
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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



choose one vertex randomly



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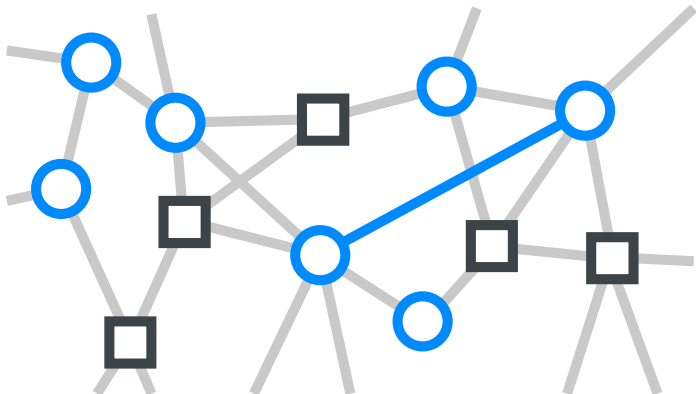
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coevolution of  
networks and  
opinions

the diplomat's  
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rewire an edge to a vertex w same opinion

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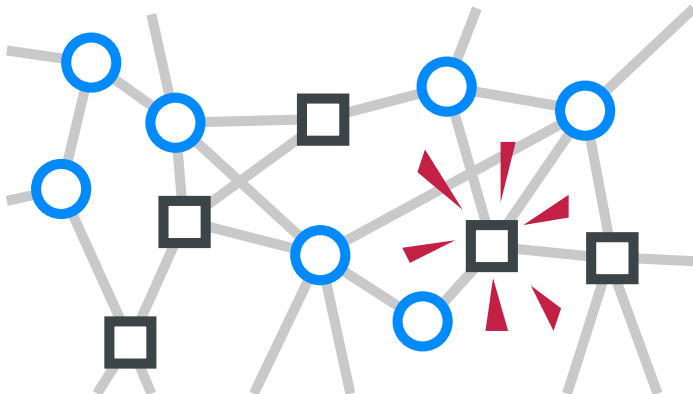
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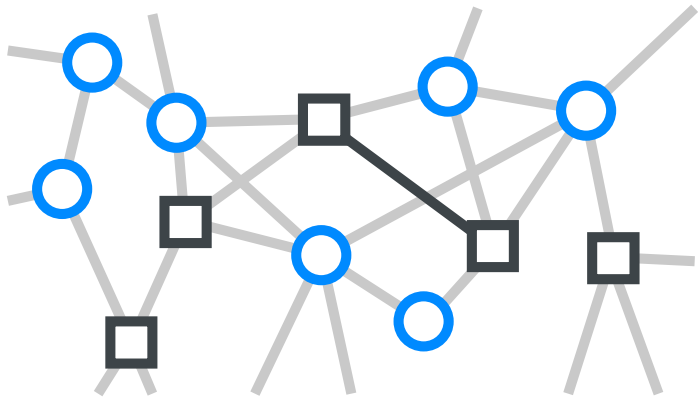
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coevolution of  
networks and  
opinions

the diplomat's  
dilemma



and so on . . .



and so on . . .

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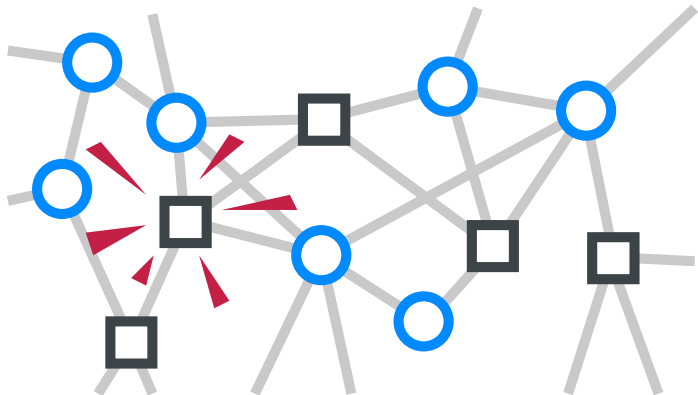
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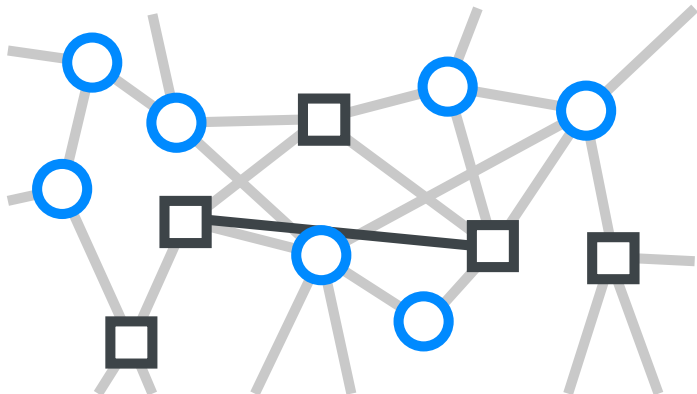
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subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



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and so on . . .

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- 2 Pick a vertex  $i$  at random.
- 3 With a probability  $\phi$  make an acquaintance formation step from  $i$ .
- 4 . . . otherwise make a voter model step from  $i$ .
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diplomats,  
religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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teens,  
diplomats,  
religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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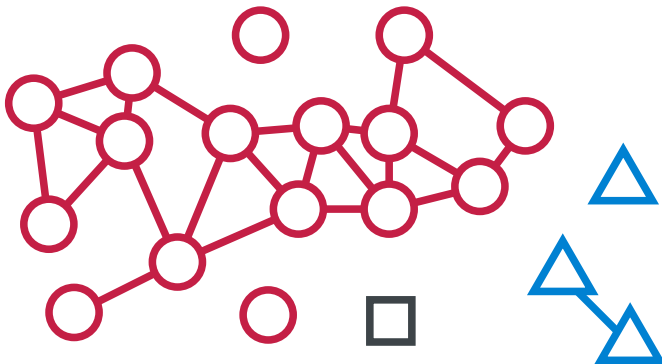
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subcultures

coevolution of  
networks and  
opinions

the diplomat's  
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low  $\phi$ —one dominant cluster

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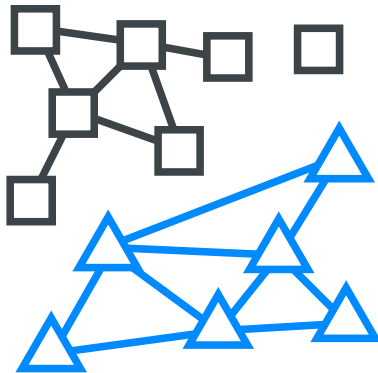
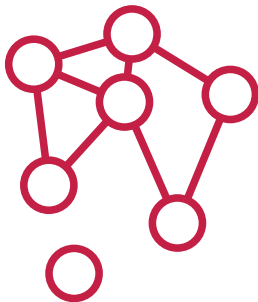
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the diplomat's dilemma



high  $\phi$ —clusters of similar sizes

# quantities we measure

- The relative largest size  $S$  of a cluster (of vertices with the same opinion).
- The average time  $\tau$  to reach consensus.

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religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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religious cults  
and more

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group  
formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



## cluster size distribution

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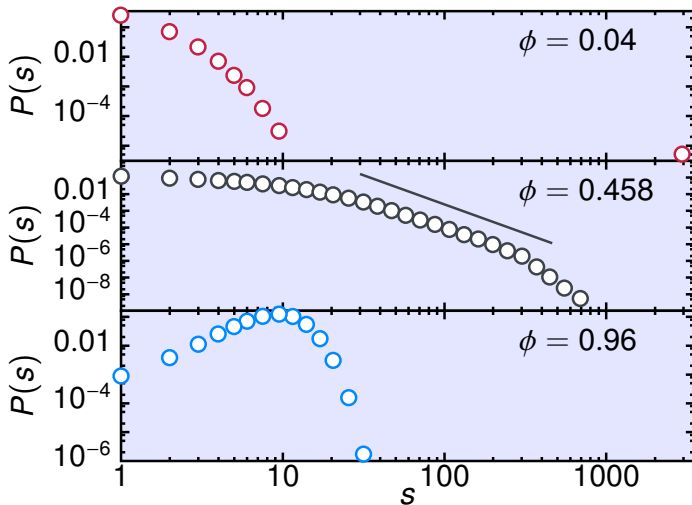
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subcultures

## coevolution of networks and opinions

## the diplomat's dilemma



# finding the phase transition

Assume a critical scaling form:

**scaling form**

$$S = N^{-a} F\left(N^b(\phi - \phi_c)\right)$$

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HOLME

group  
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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma

# finding the phase transition

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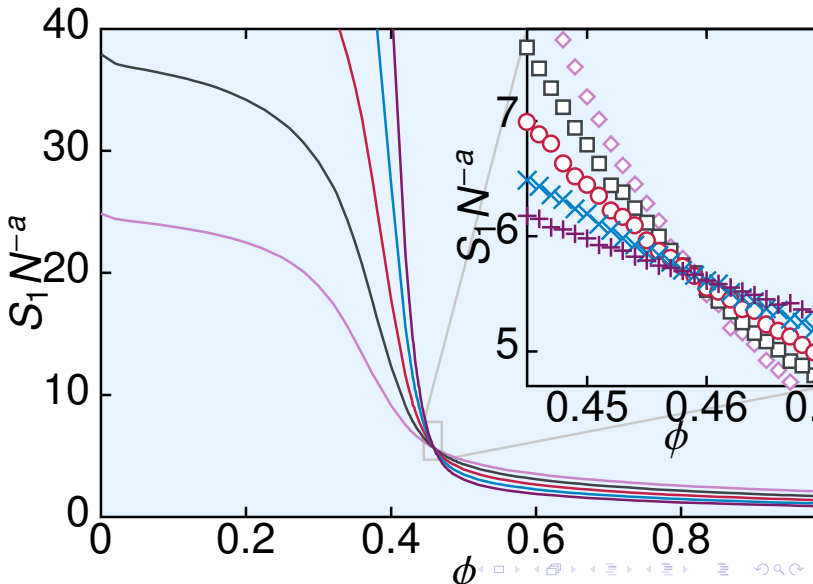
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the diplomat's dilemma



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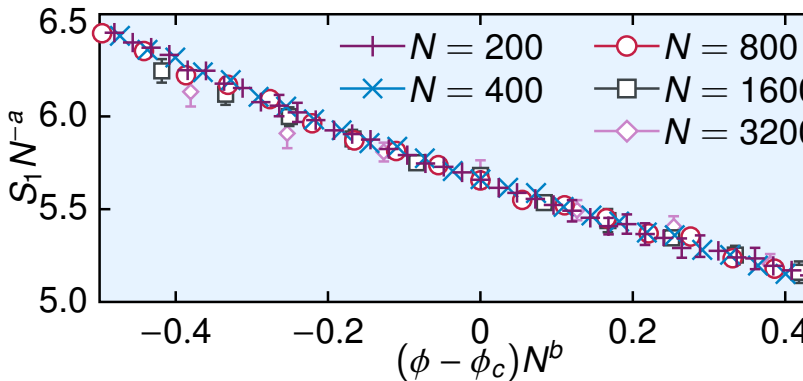
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coevolution of networks and opinions

the diplomat's dilemma



$a = 0.61 \pm 0.05$ ,  $\phi_c = 0.458 \pm 0.008$ ,  $b = 0.7 \pm 0.1$   
random graph percolation:  $a = b = 1/3$

# finding the phase transition

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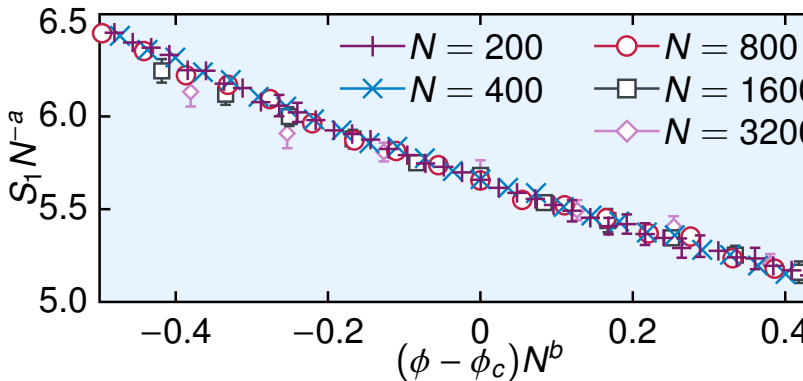
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youth subcultures

coevolution of networks and opinions

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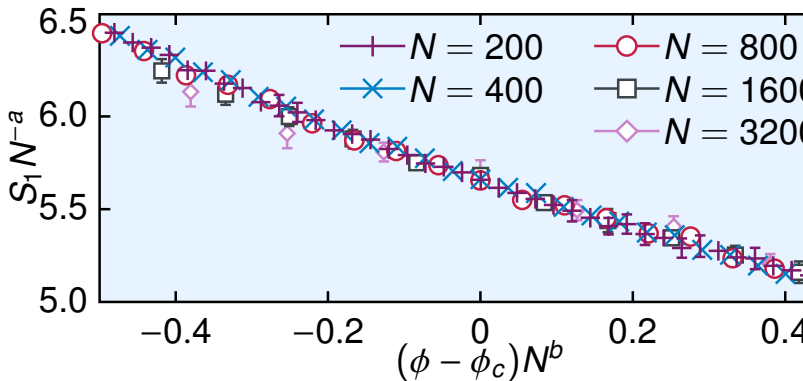
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youth subcultures

coevolution of networks and opinions

the diplomat's dilemma



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# dynamic critical behavior

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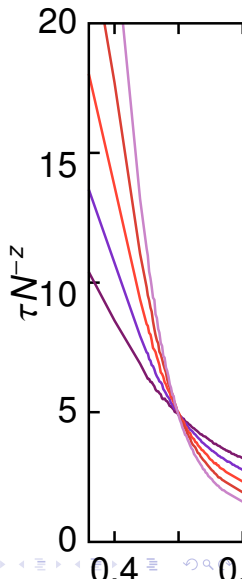
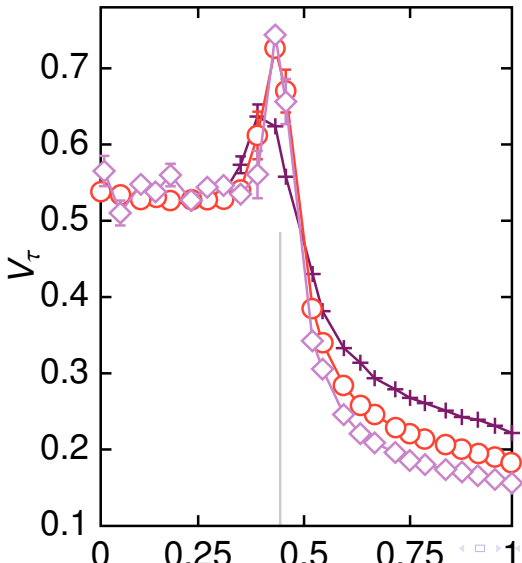
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formation

youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma



- We have proposed a simple, non-equilibrium model for the coevolution of networks and opinions.
- The model undergoes a second order phase transition between: One state of clusters of similar sizes. One state with one dominant cluster.
- The universality class is not the same as random graph percolation.
- In society, a tiny change in the social dynamics may cause a large change in the diversity of opinions.



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models of  
teens,  
diplomats,  
religious cults  
and more

PETTER  
HOLME

group  
formation

youth  
subcultures

coevolution of  
networks and  
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the diplomat's  
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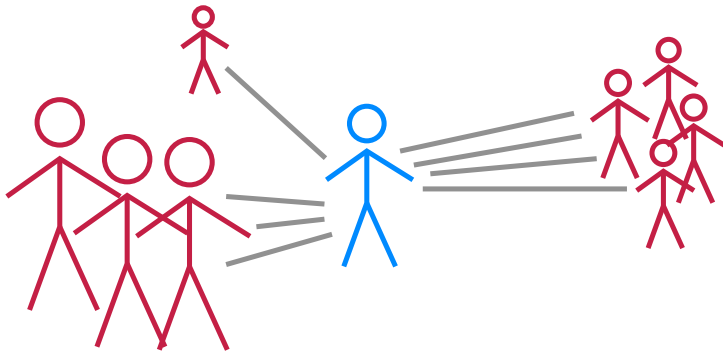
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Holme & Ghoshal, Phys. Rev. Lett. **96**, 098701 (2006).

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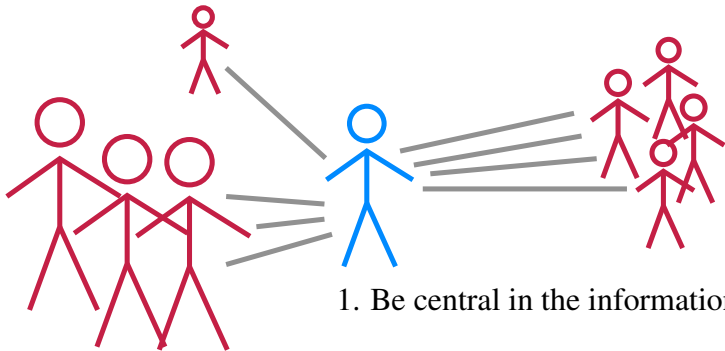
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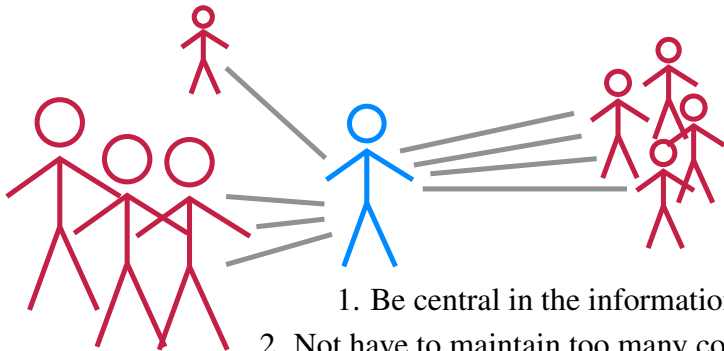
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In diplomacy, lobbying or other political or corporate networking, it is important to:



1. Be central in the information flow.
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# the object system

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youth  
subcultures

coevolution of  
networks and  
opinions

the diplomat's  
dilemma





# score function

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diplomats,  
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formation

youth  
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- Central is good—*closeness centrality*

$$C(i) = (N - 1) / \sum_{j \neq i} d(i, j)$$

- If the network is disconnected, being a part of a large component is good.
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**definition of closeness**: If we sum the reciprocals (instead of  
inverting the sum), we get the score function:

## Definition

$$s(i) = \begin{cases} (1/k_i) \sum_{H_i} 1/d(i,j) & \text{if } k_i > 0 \\ 0 & \text{if } k_i = 0 \end{cases} \quad (1)$$

$H_i$  is the component  $i$  belongs to, except  $i$

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# time evolution

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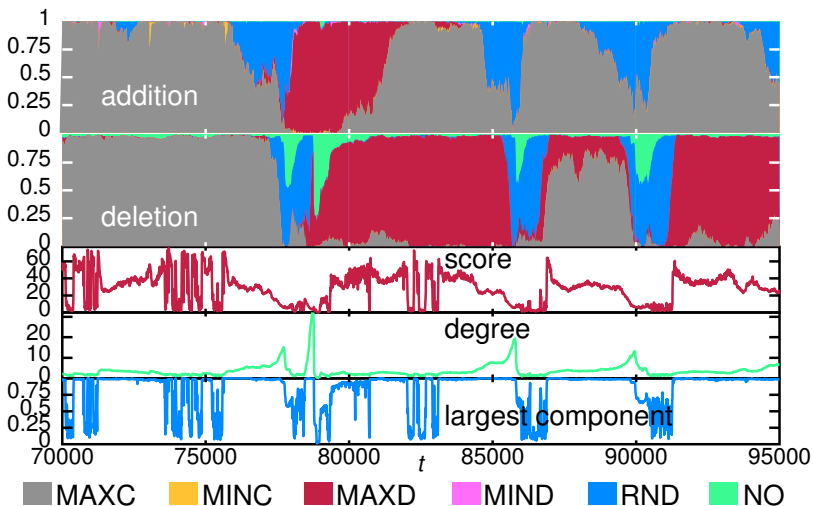
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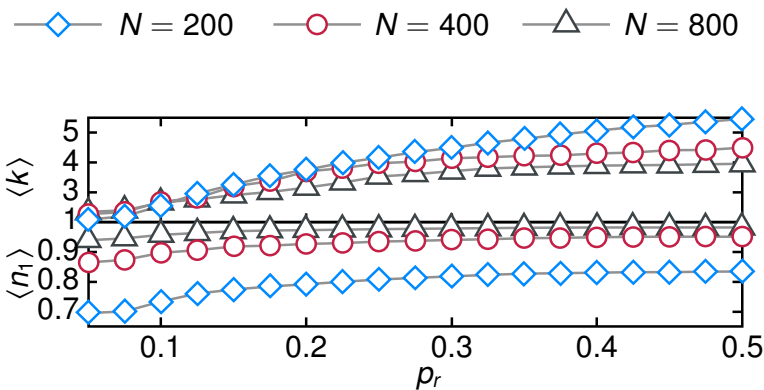
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# effect of random moves: degree & cluster size



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coevolution of networks and opinions

the diplomat's dilemma

# conclusions

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subcultures

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- Complex time evolution with spikes, quasi-equilibria and trends.
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- The NO/NO strategy is not stable—Red Queen.
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