

# Homophily, Contagion and Confounding: Pick Any Three

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## The basic observation

*People who are close to each other in social networks tend to be similar and vice versa*

## Why?

Dynamics *on* the network (influence, diffusion, contagion)

vs.

Dynamics *of* the network (homophily, assortativity) vs.

Non-network dynamics

## Did They Jump or Were They Pushed?

Difference between:

- 1 jumping off a bridge because your friend Joey did it (contagion)
- 2 being friends with Joey because you're both the kind of kid who'd jump off a bridge (homophily)
- 3 You and Joey both watch the wrong TV shows, and respond independently to them

Knowing which is which matters for understanding and for intervention

## Making homophily and contagion look like causation

A lot of social science, theoretical and applied, is about connecting long-term, hard-to-change social/economic status to more short-term, malleable cultural / political / consumer variables

- Political sociology
- Marketing and political strategy
- Historical materialism

The idea is: how you live has a deep influence on what you think, feel and choose

*Brecht: "Grub first, then ethics."*

*Gellner: "Social structure is who you can marry, culture is what you wear at the wedding."*

## What's the evidence?

- The stories sound good
- Casual empiricism
- Correlation/regression analyses; cultural choices are predictable from social positions

Probably even true a lot of the time

BUT usually ignores social networks and just looks at surveys

$X_i$



$Y_i$

$X_j$



$Y_j$

social

cultural

## Responsible Just-So Story-telling

These accounts are usually adaptationist/functionalist

At the very least they are causal accounts

We should really check them

Biology suggests: a **neutral model**

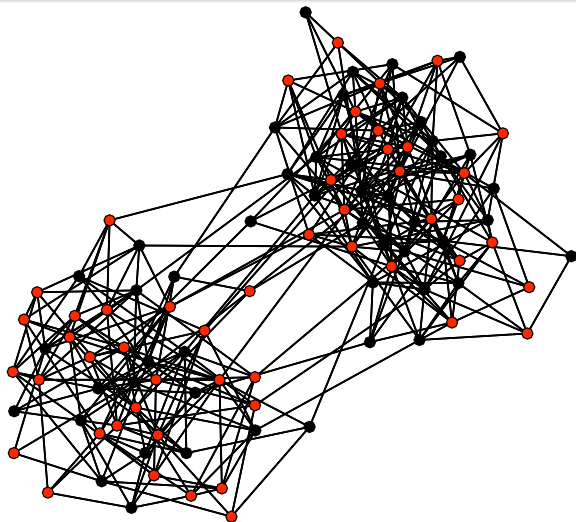
- Include all the evolutionary processes *except* adaptation
- Work out expected behavior of this model
- Data departing from neutral model  $\Rightarrow$  evidence of adaptation

## Caricature Neutral Model of Cultural Evolution

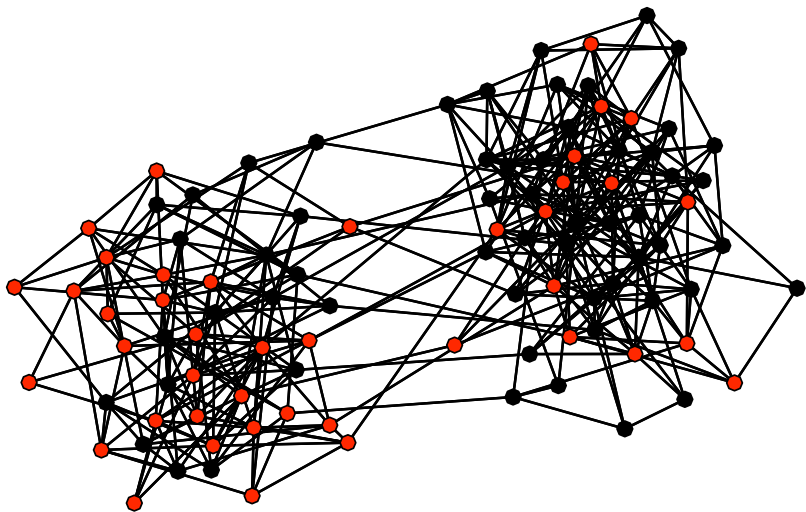
- $X_i$  = unchanging status variable for node  $i$  (“social”)
- Network is assortative on  $X$
- $Y_i(t)$  = rapidly changing choice variable for  $i$  (“cultural”)
  - 1 At each  $t$ , pick a random  $i$ , and a random neighbor  $j$
  - 2 Set  $Y_i(t) = Y_j(t - 1)$
  - 3 Go to (1)

(= “voter model” of statistical mechanics on a stochastic graph)



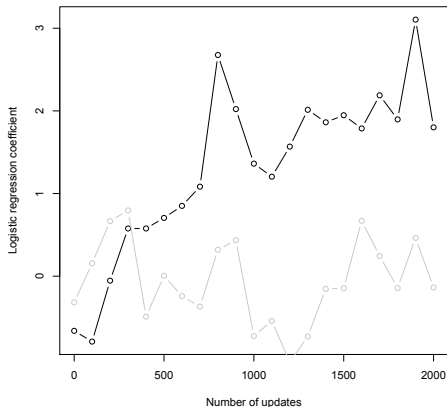


100 node network, homophily for status (2 groups), initial choices



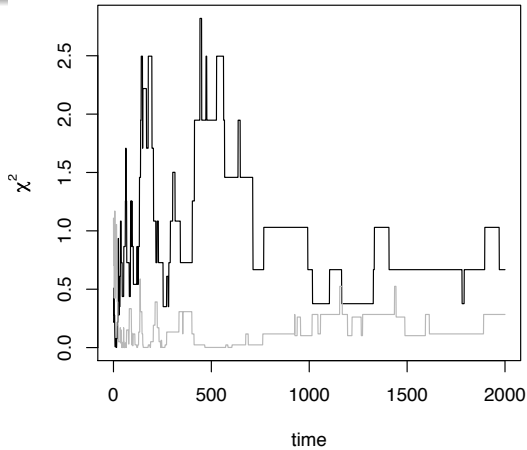
After 1000 updates



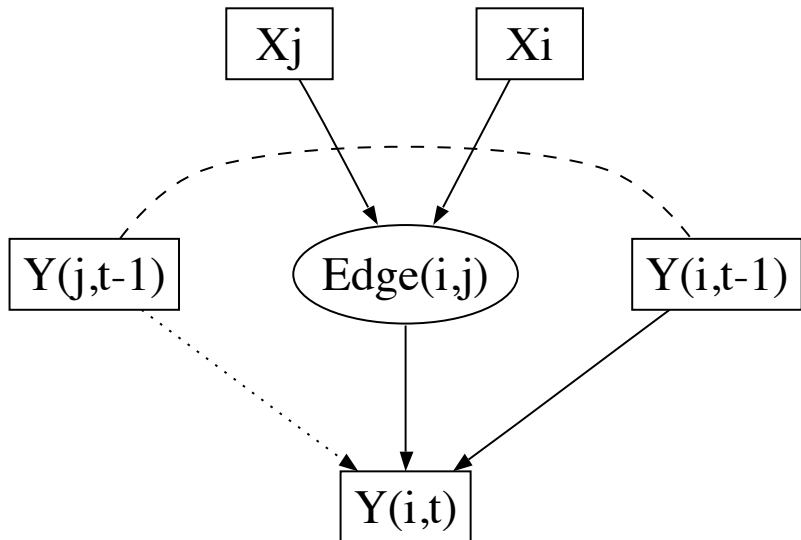


100 node network

Logistic regression of choice on status  
black = assortative  
grey = non-assortative



Same,  $\chi^2$  for status/choice contingency table



- Neutral diffusion + homophily looks like a real connection between social status and cultural choices
- Problem is *not* the ecological fallacy (red-state/blue-state fallacy), since we're not using aggregated data
- Problem is that choices are not independent conditional on statuses
- Deconfound by conditioning on previous  $Y_j$  of neighbors

## Can You Really Get Cooties From Touching Someone?

Finding: whether  $i$  does something at time  $t$  is well-predicted by whether  $i$ 's neighbors had already done it at  $t - 1$

- Diffusion of innovations
- Infectious diseases
- Not-obviously-infectious medical conditions (e.g., obesity)

...

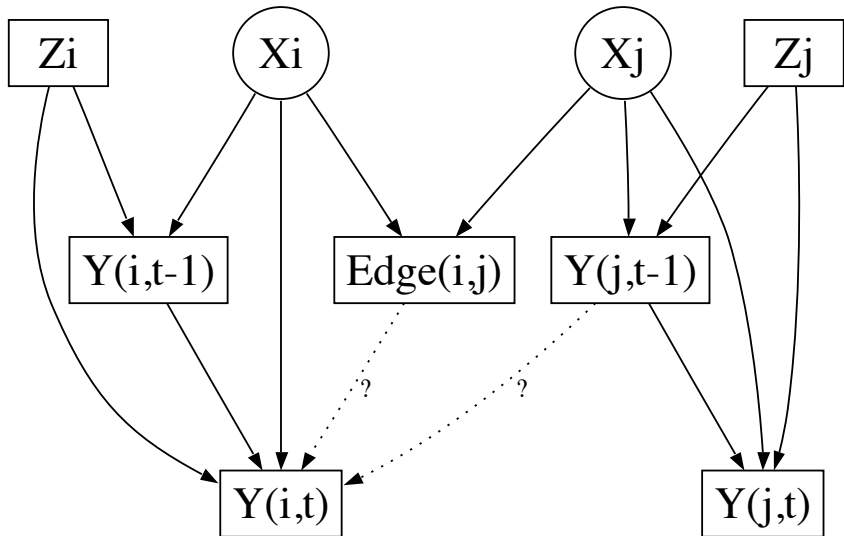
Again, often correct

Again, how hard is it to fake this without real contagion?

Suppose that:

- $X_i$  = persistent trait/traits of node  $i$ , *not directly observable*
- Homophily on  $X$
- $Z_i$  = other, non-assortative but observable traits
- $Y_i(t)$  = whether  $i$  has adopted at  $t$ ,  $\tau_i$  = time of adoption
- $X_i$  influences whether/when  $i$  adopts





*Item:*  $Y_i$  is a cue for  $X_i$

*Item:* Neighbor's  $X_j$  are cues for  $X_i$

$\therefore$  Neighbors'  $Y_j$  are cues for  $X_i$

$\therefore$   $Y_i$  depends statistically on previous  $Y_j$  of neighbors, whether there's a direct edge or not

$\therefore$  Latent homophily is confounded with contagion

—Conditioning on  $Y_i(t-1)$ ,  $Y_j(t-1)$  does not screen off homophily

except for homophily due to adoption status

—Need to condition on the homophilous trait  $X_j$

Or other covariates  $Z$  such that  $X_i \perp X_j | (Z_i, Z_j)$ , if they exist

## Conclusion

- Homophily + contagion looks like causality
- Homophily + causality looks like contagion
- Contagion looks like homophily (especially with causality)