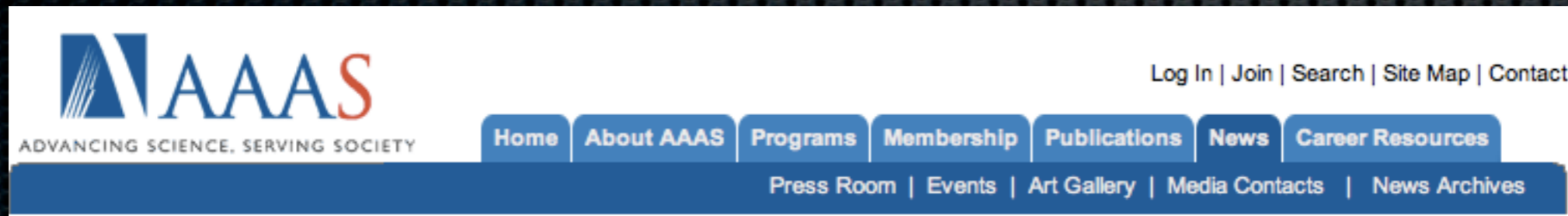


*Can there be a science of cities?  
May be yes*

# Toward **scientific theory** of cities:

HyeJin Youn  
Santa Fe Institute  
July 13 2012





- In detective novels, a "theory" is little more than an educated guess, often based on a few circumstantial facts. In science, the word "theory" means much more. A scientific theory is **a well-substantiated explanation of some aspect of the natural world, based on a body of facts that have been repeatedly confirmed through observation and experiment.**

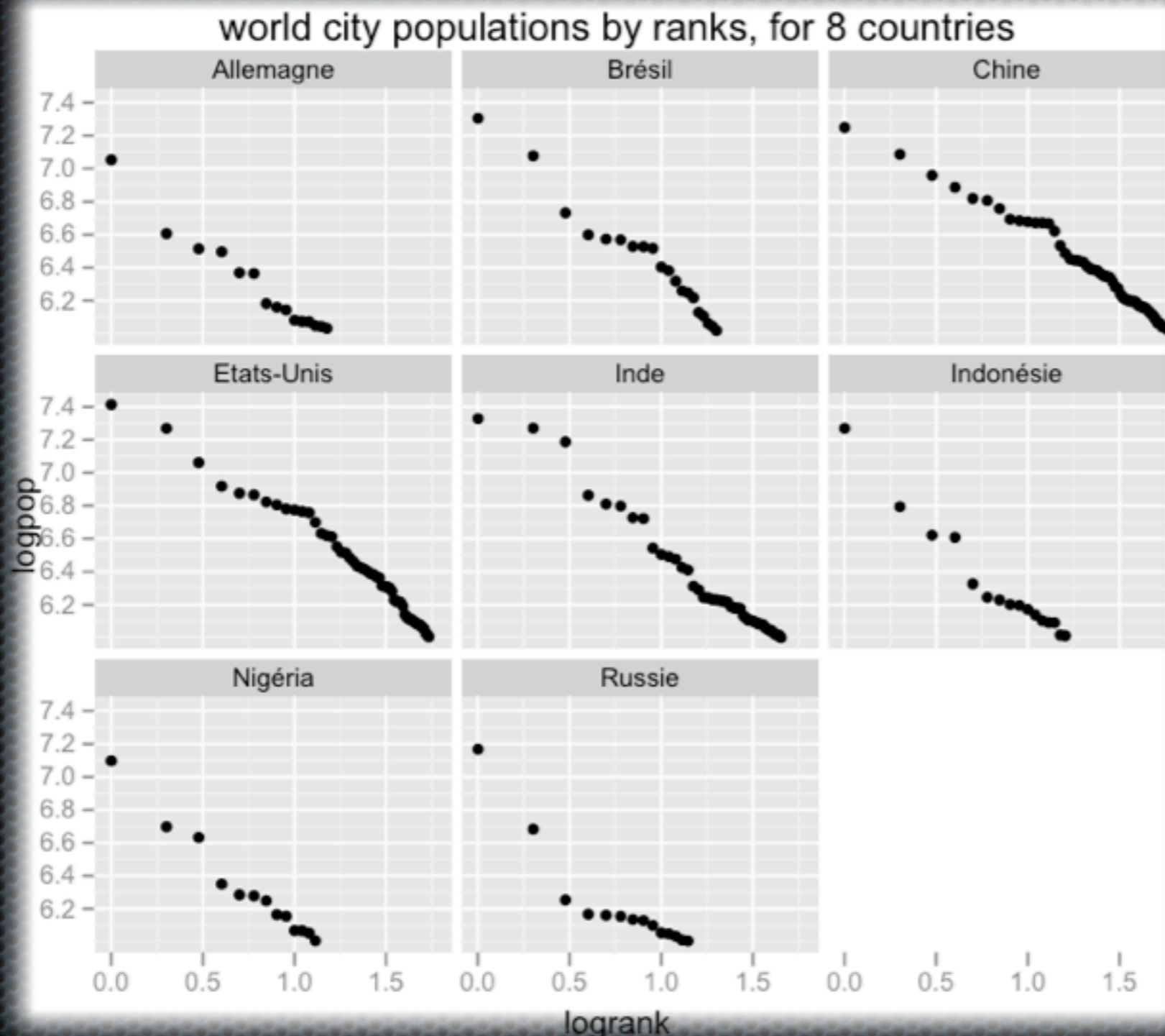
Quantifiable, comparable  
regular patterns across  
cities, based on which  
“Mathematical” theory can  
be constructed.

*(beyond just cherry pickings)*

**“What is a CITY?”**

**“What is a generic city”**

# Landmark: Zipf's law

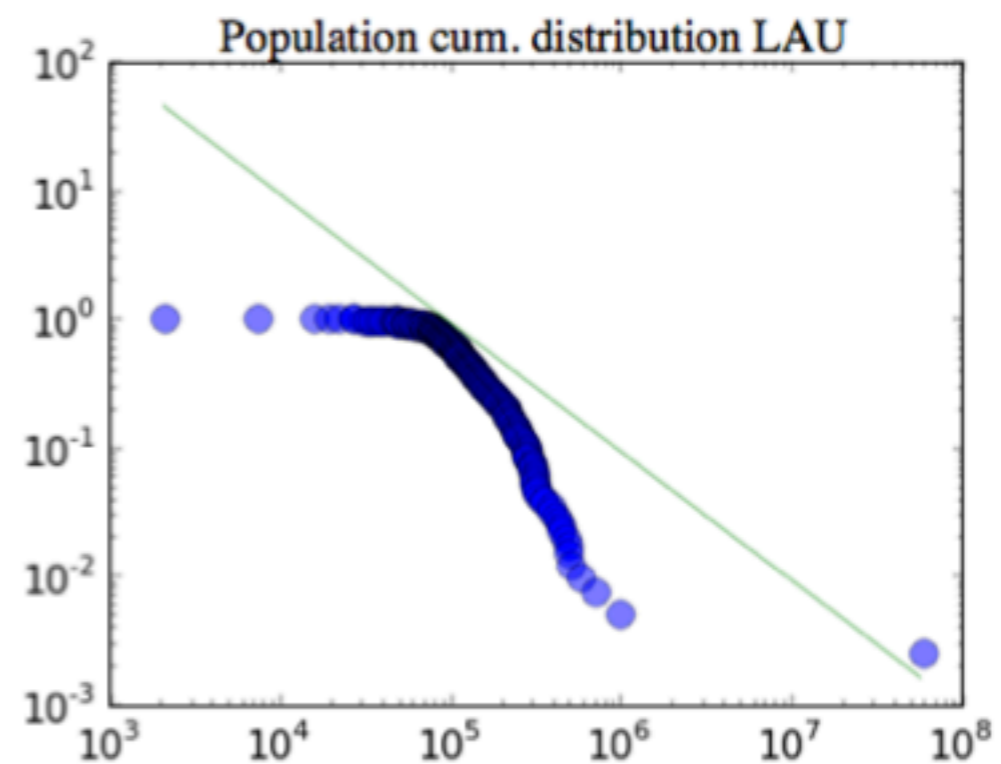
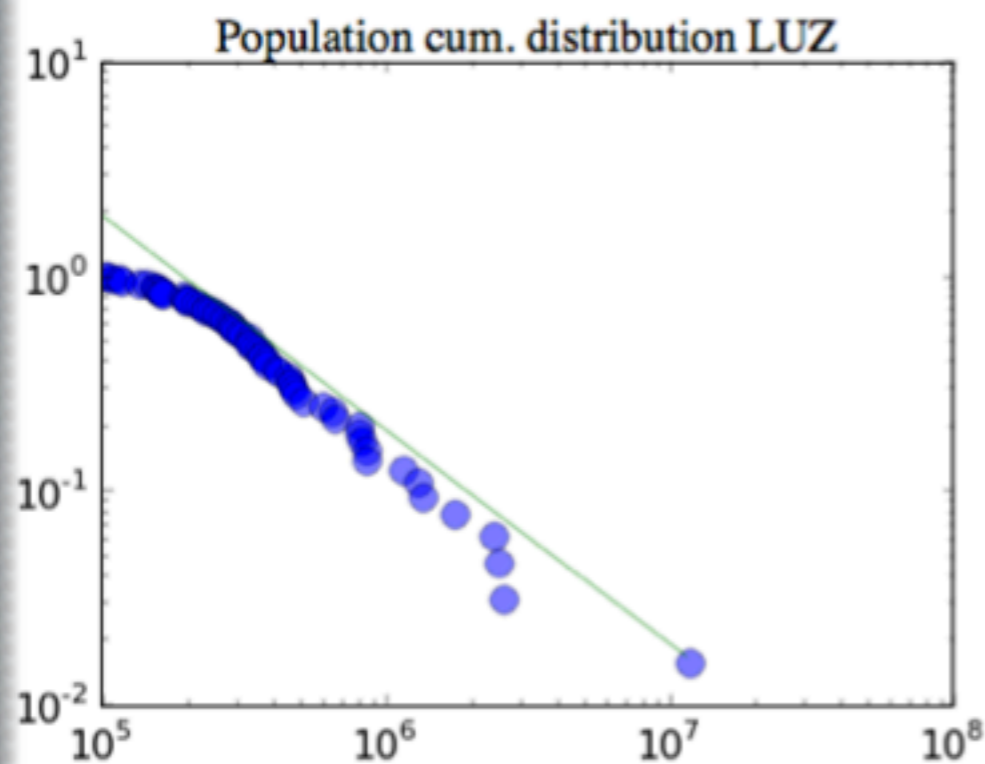


$$p(r) \sim 1/r$$

Models for  
Growth Dynamics

# Landmark: Zipf's law

*unit of analysis (UK)*



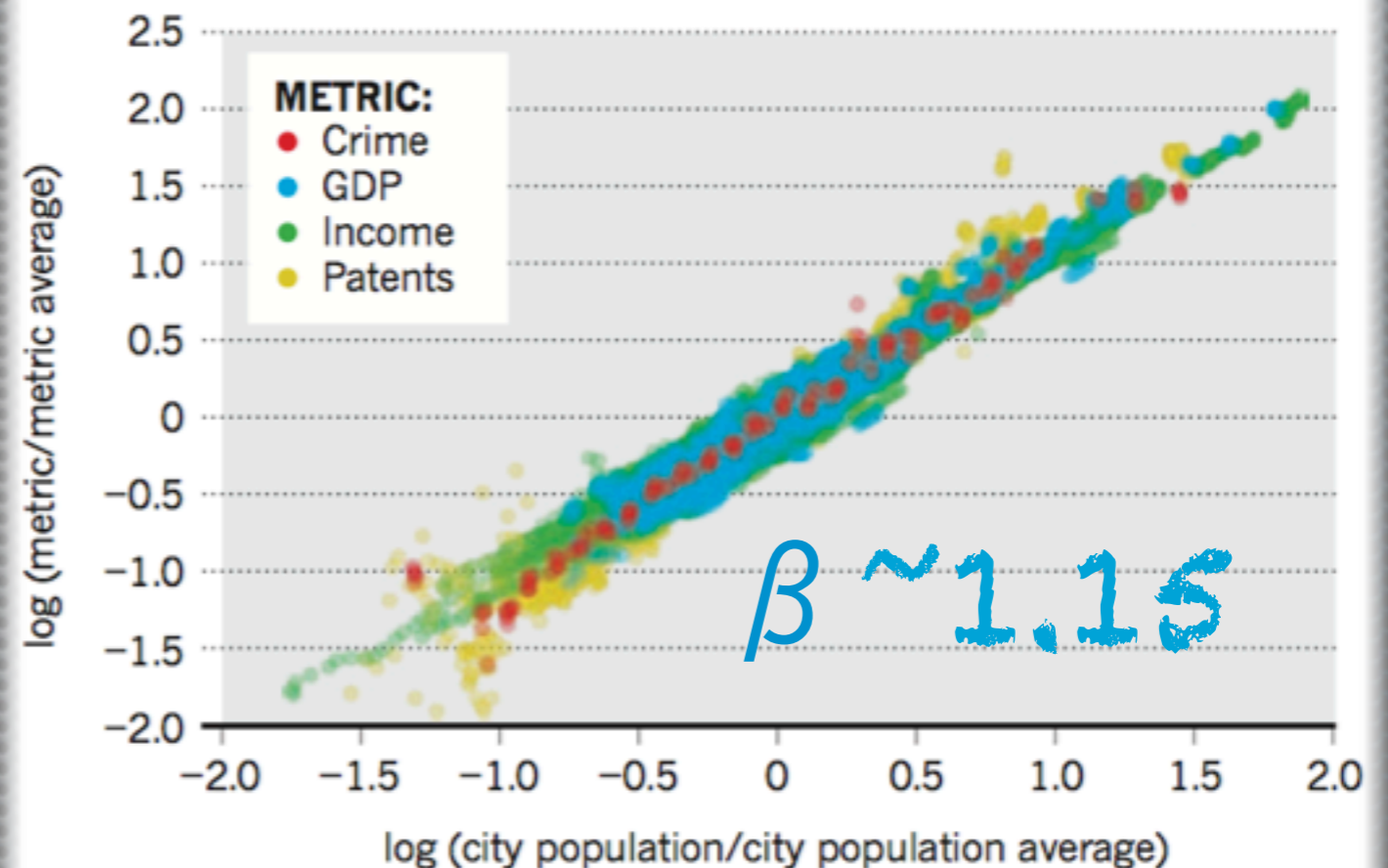
# Landmark: Urban Scaling

$$Y \sim N^\beta$$

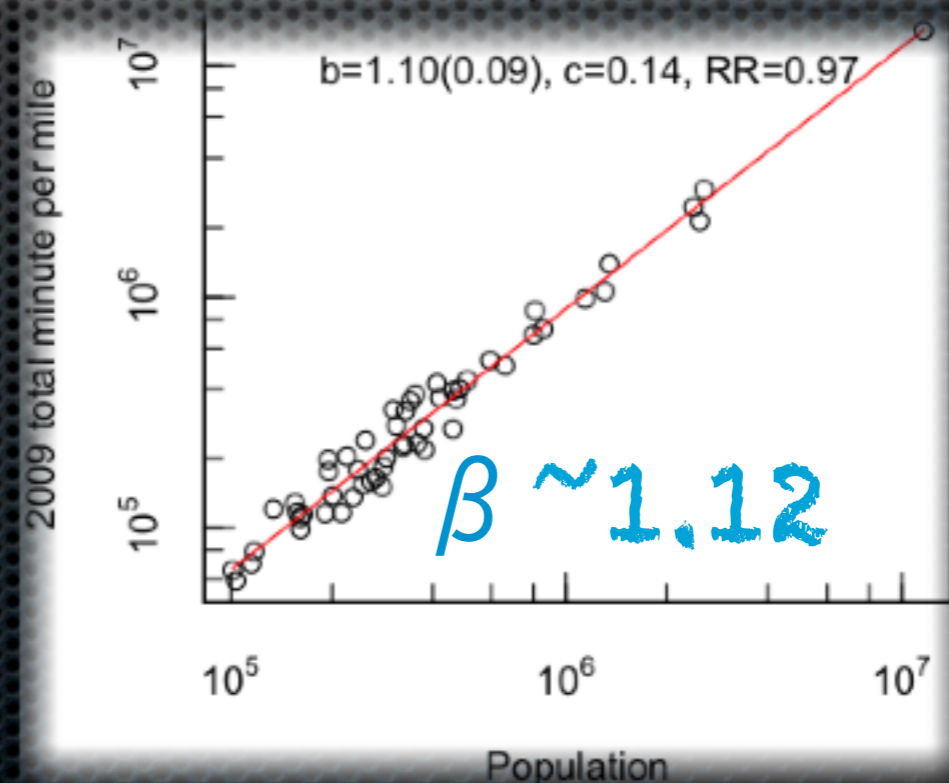
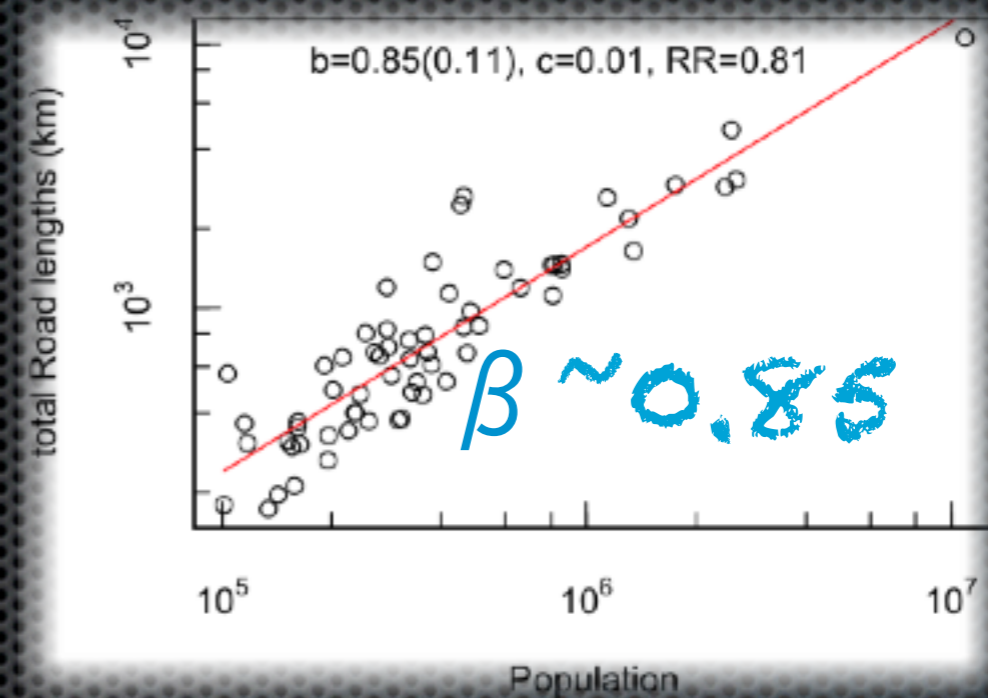
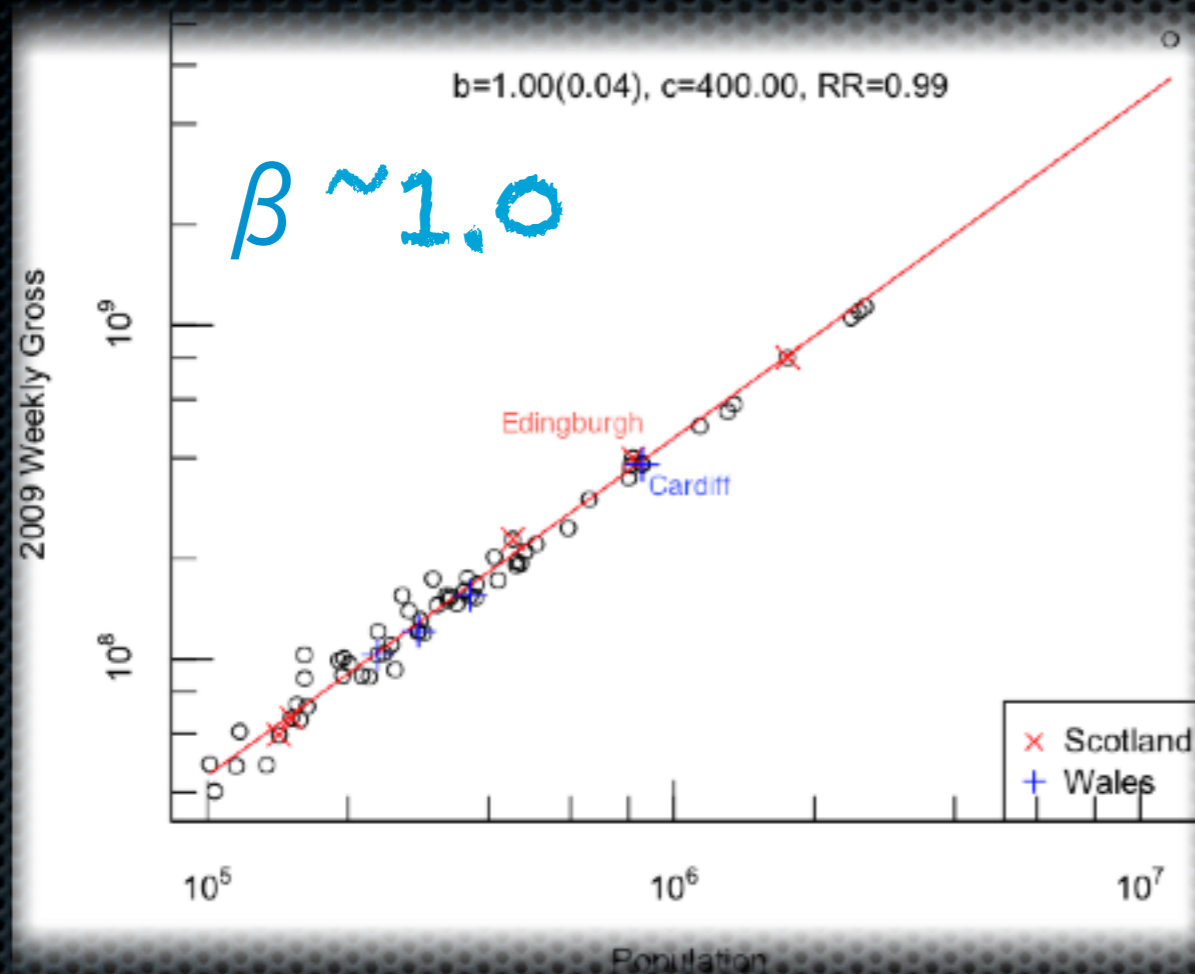
*Bettencourt & West  
Nature 467 (2010)*

## PREDICTABLE CITIES

Data from 360 US metropolitan areas show that metrics such as wages and crime scale in the same way with population size.



# Landmark: UK Scaling



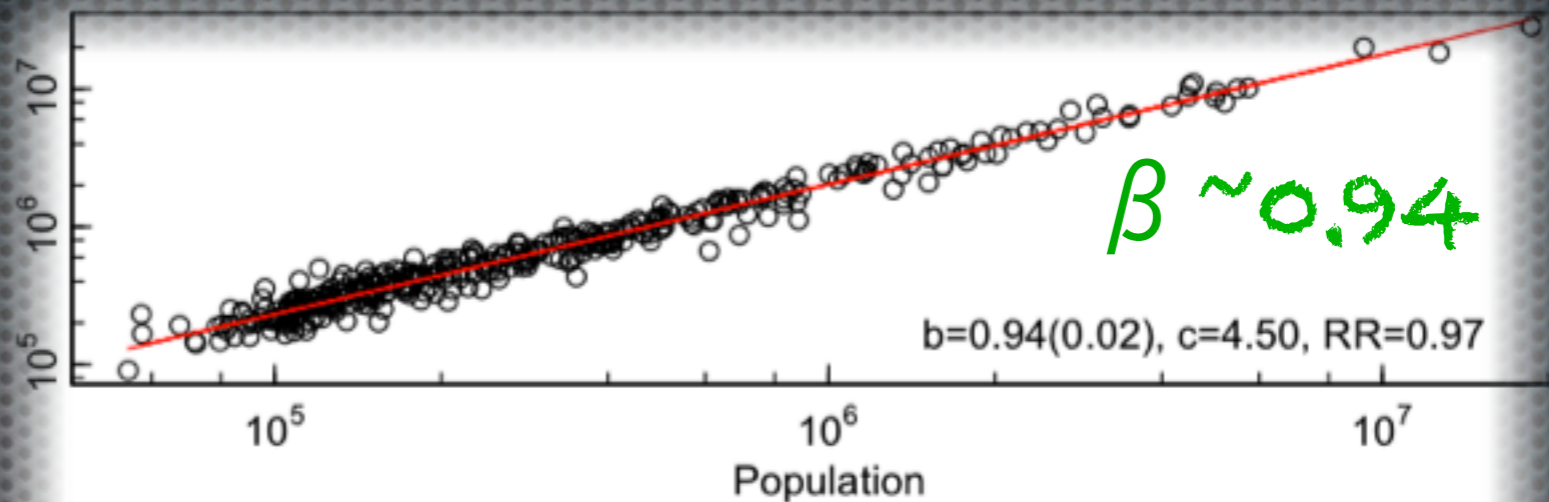
$$\begin{aligned}
 Nt &\sim N(N_v/L) \\
 &\sim N^2/N^{0.85} \\
 &\sim N^{1.15}
 \end{aligned}$$

# Bigger, Greener?

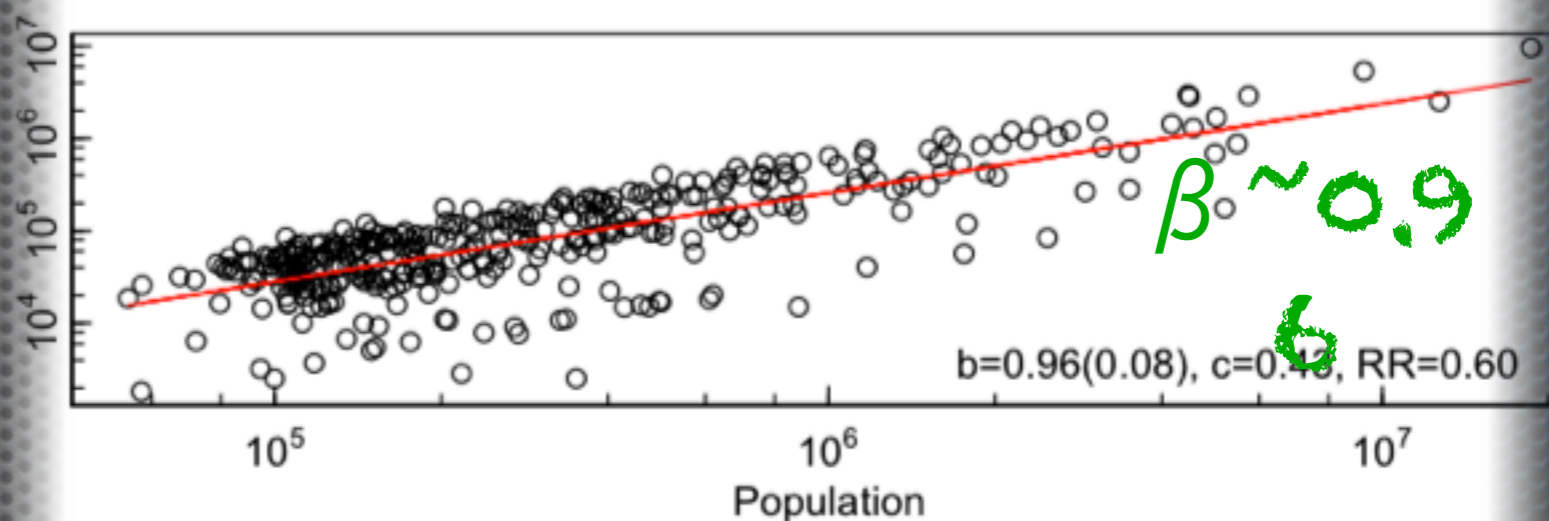
$$Y \sim N^\beta$$



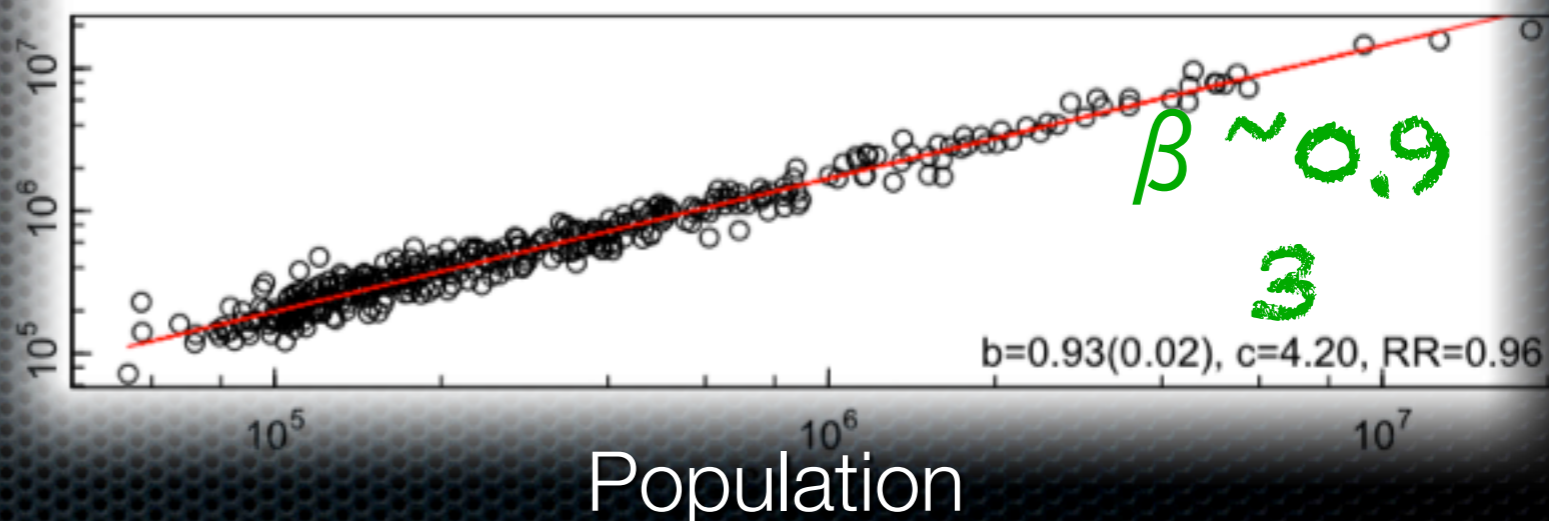
Total



Residential



Transportation



# Commuting Choice of Mode of Transportation

↙ Depreciation, Insurance, Parking

(fixed cost) + (marginal cost) × (distance travelled)

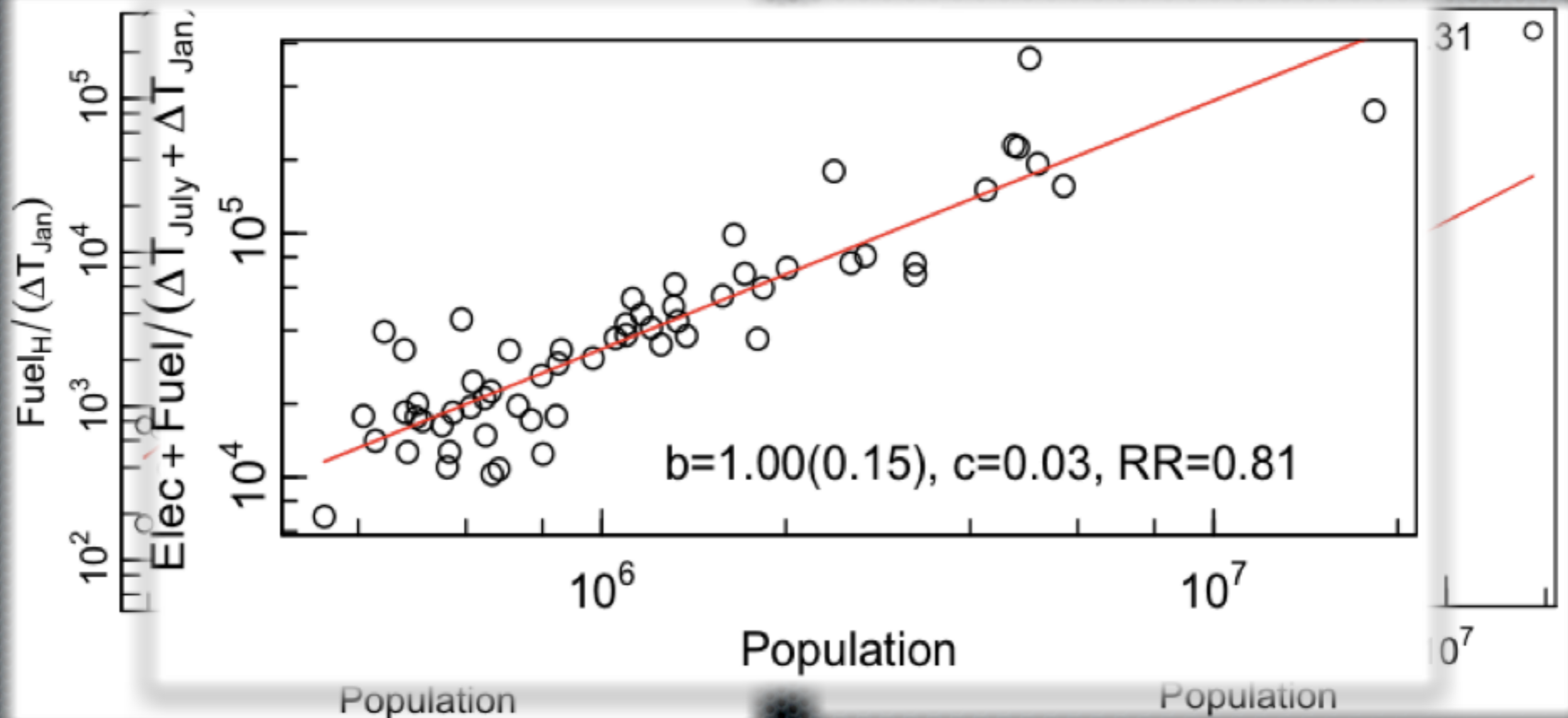
↘ Gas, maintenance, **TIME**

## Thermal Diffusion Model

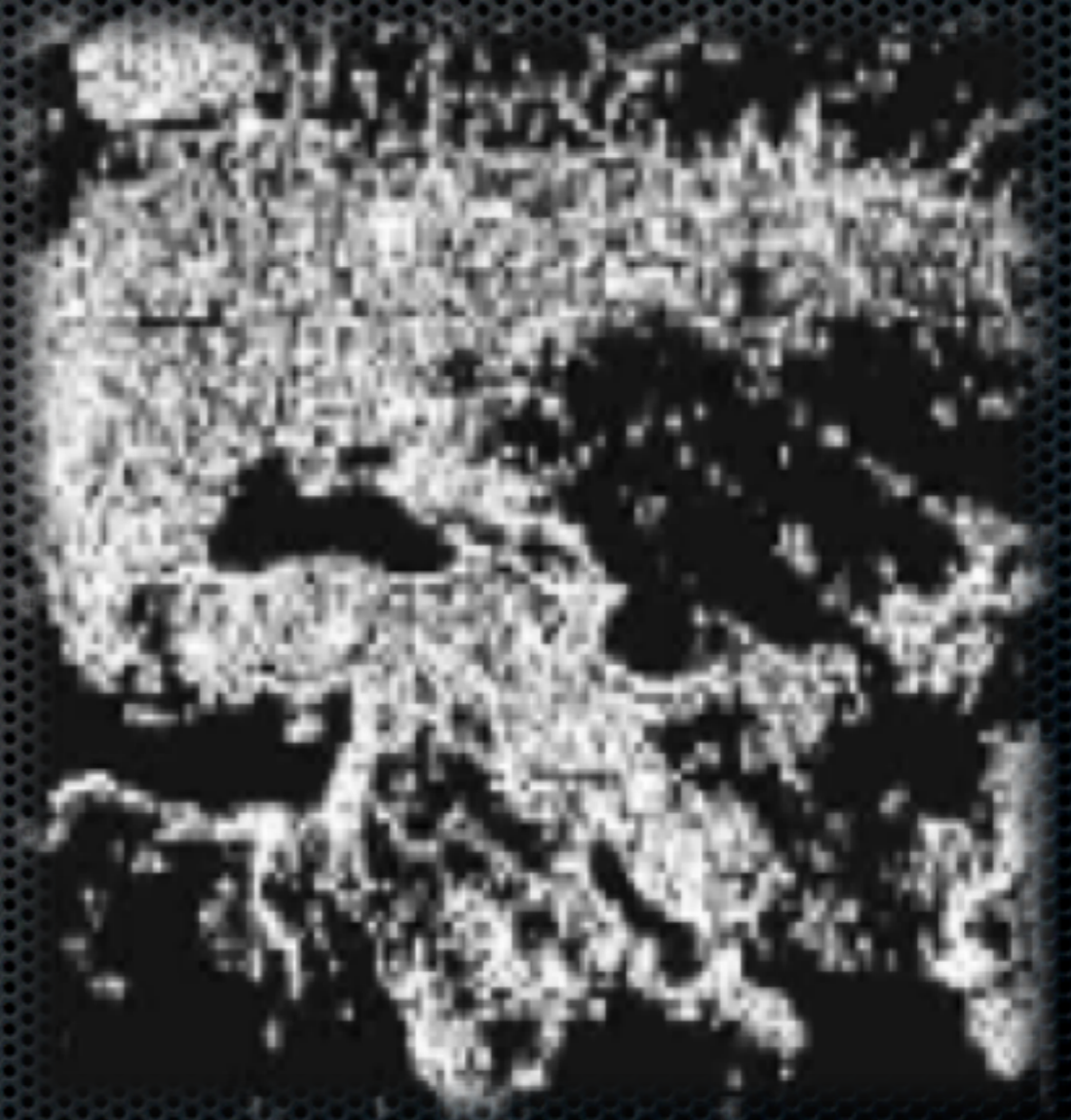
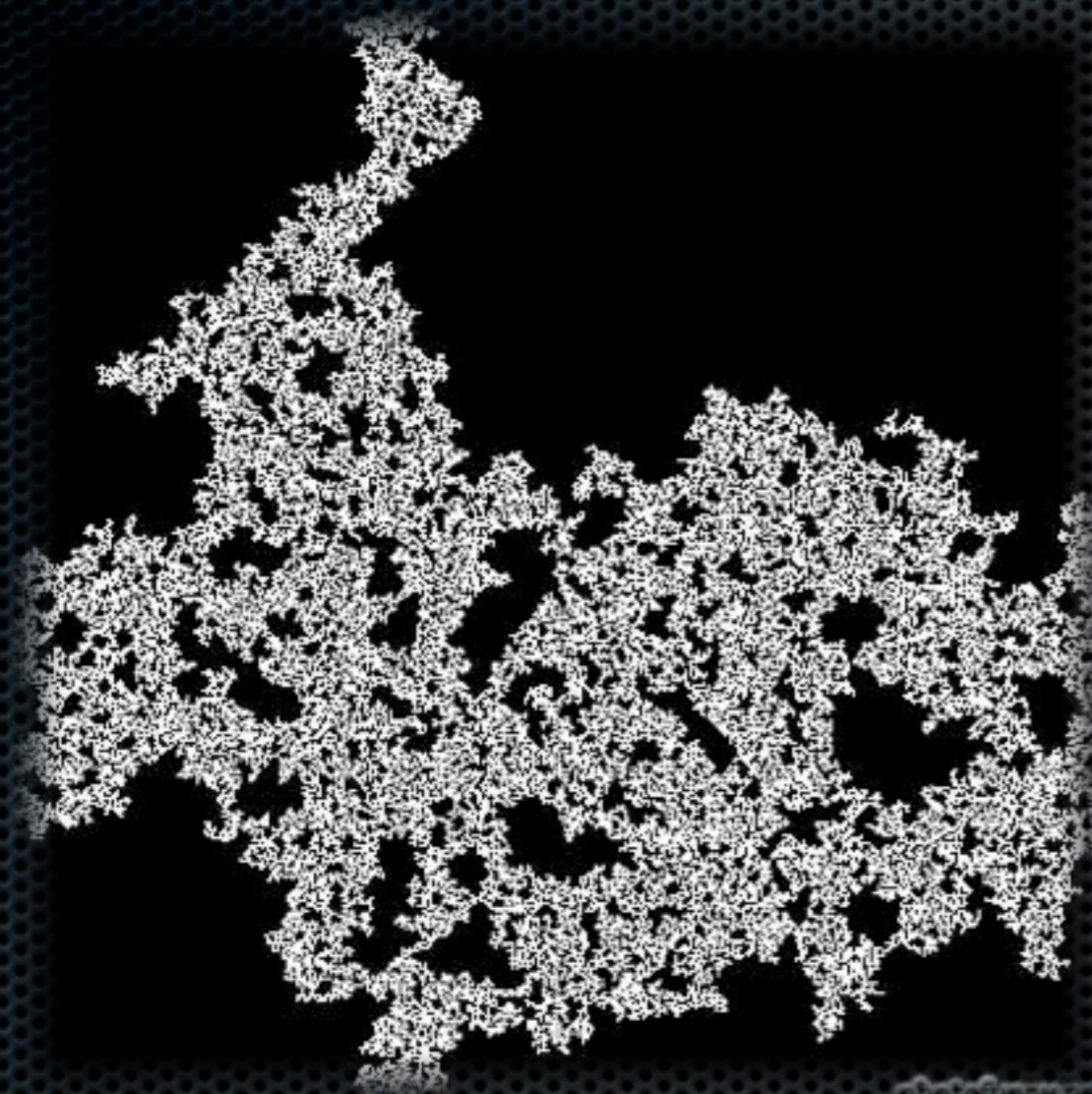
$$E_{HC} = \int dt \kappa' S \Delta T(t) \longrightarrow E_{HC} / \Delta T = \kappa' S$$

# Thermal Diffusion Model

$$E_{HC} = \int dt \kappa' S \Delta T(t) \longrightarrow E_{HC} / \Delta T = \kappa' S$$

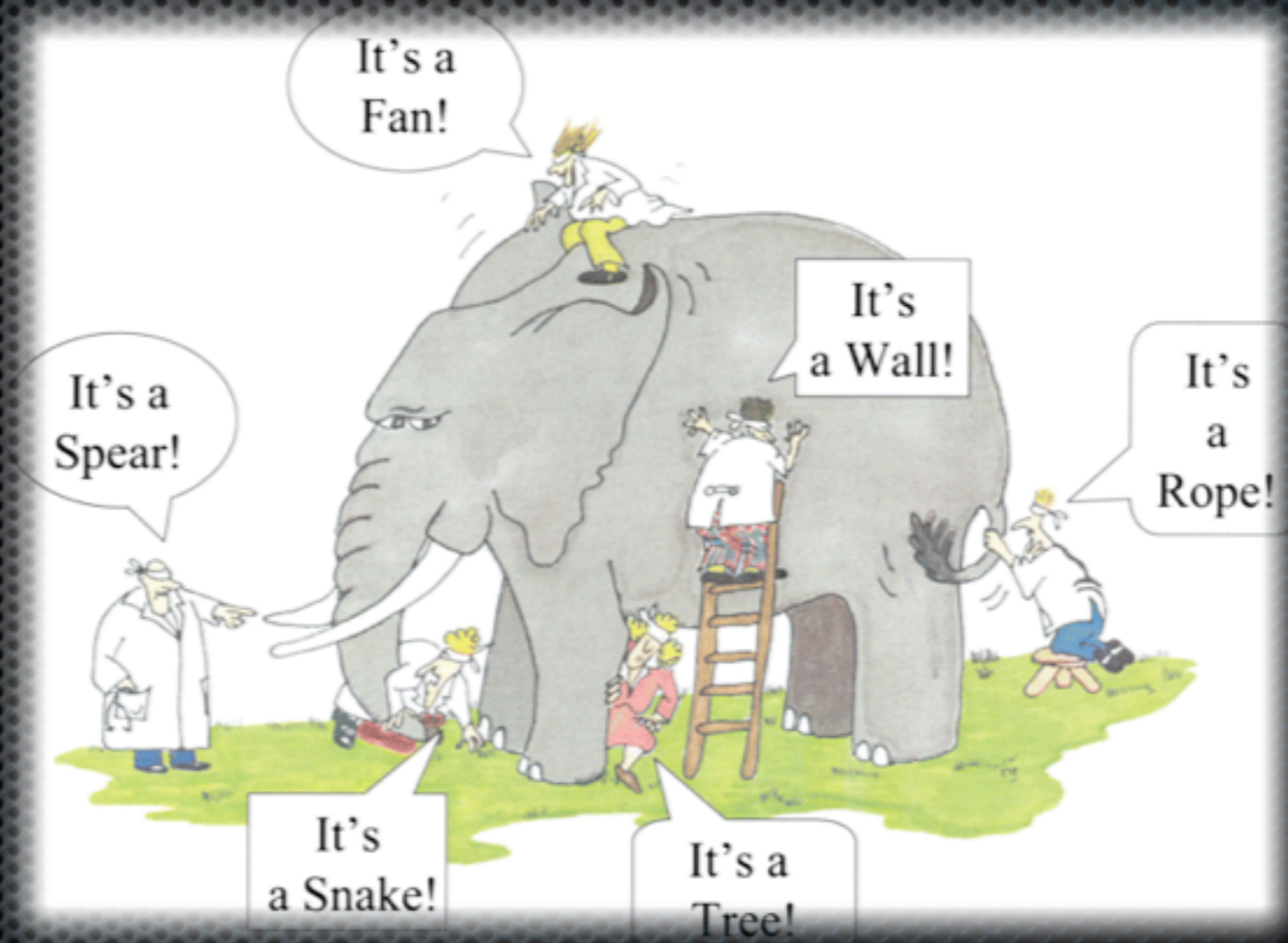


# Population Distribution



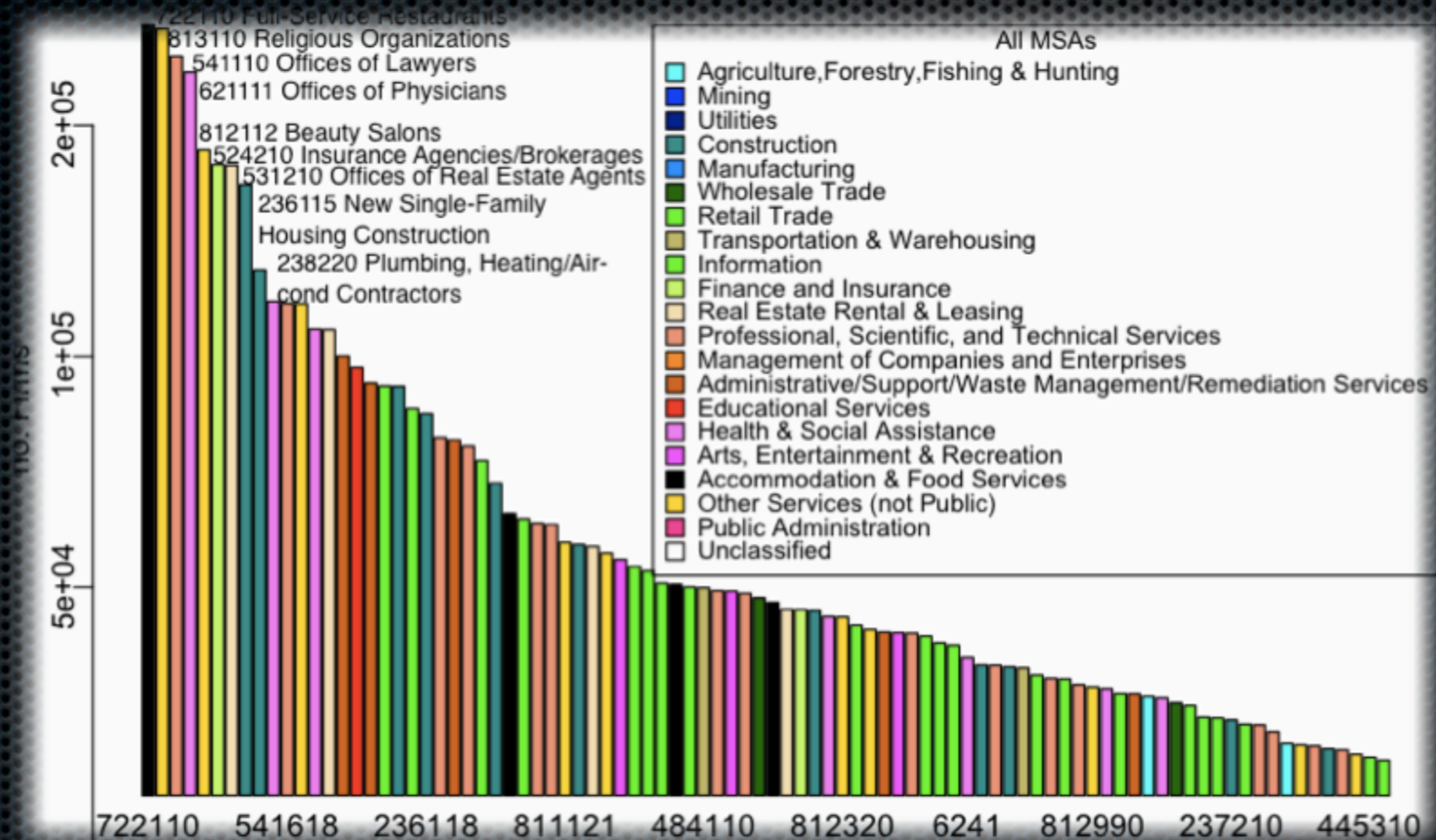
# Urban Economic Diversity

- Important urban feature
- Industrial Types (NAICS): Restaurants, Religious organizations, Lawyers, Physicians...
- Every city is special
  - Silicon Valley, Detroit, Phoenix, New York...



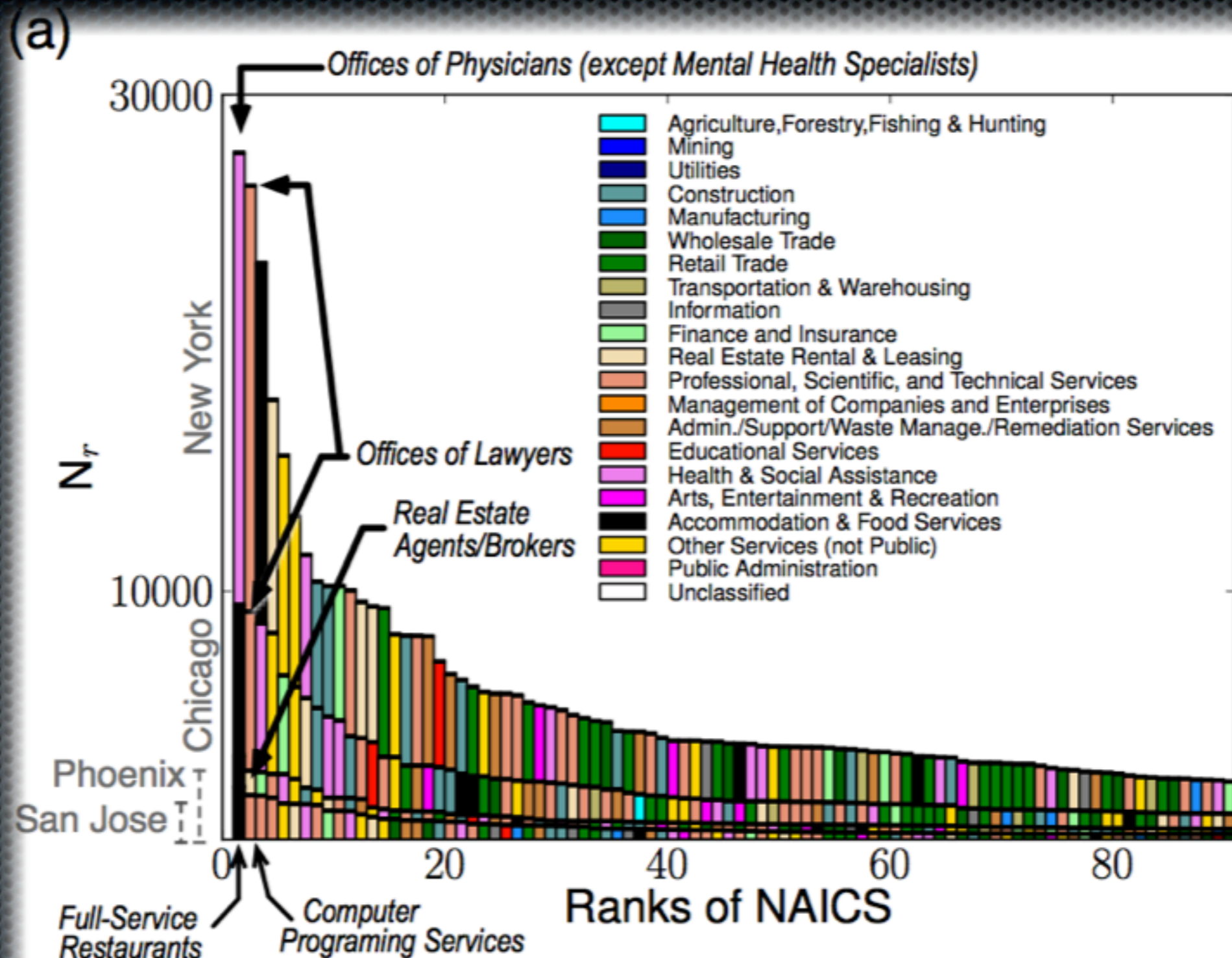
# “Whole Picture” of All MSAs

Number of Firms of given Industry



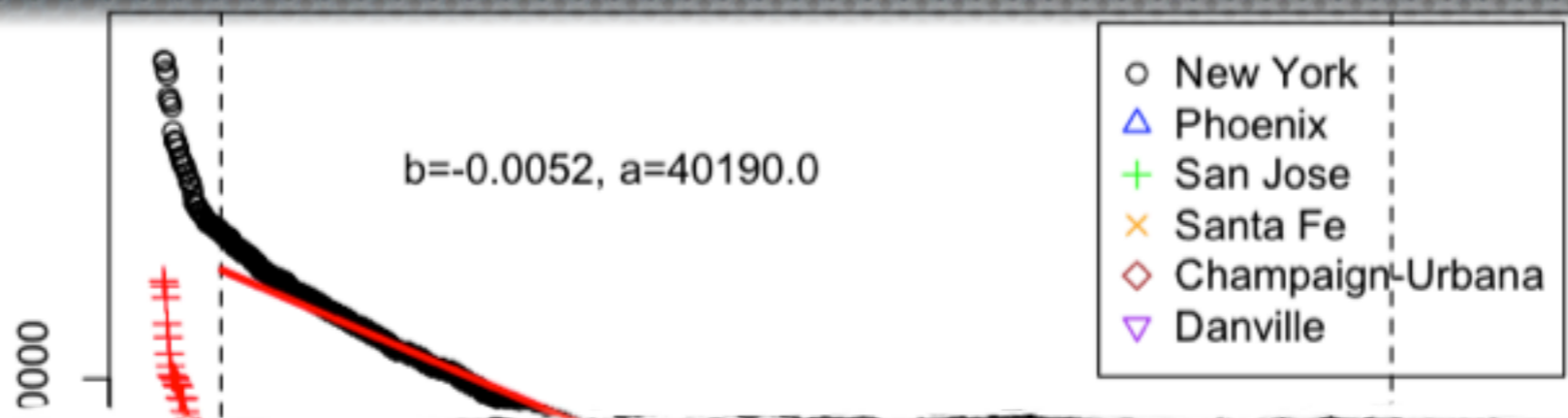
# Individual Cities

Number of Firms of given Industry



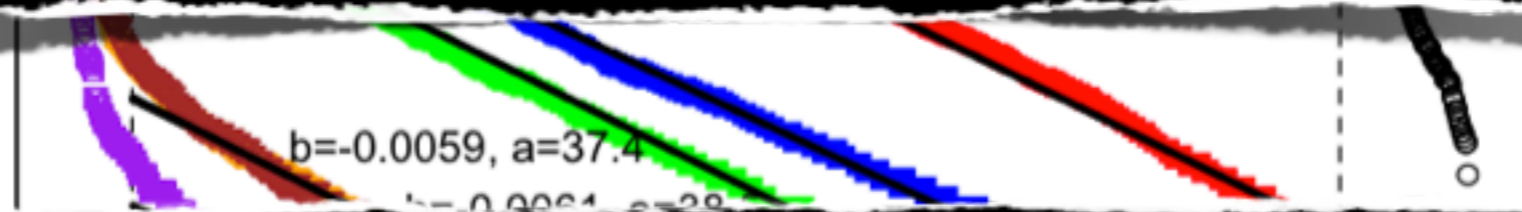
# Only Abundance Shape

Industry



Universal Shape?

of Fir



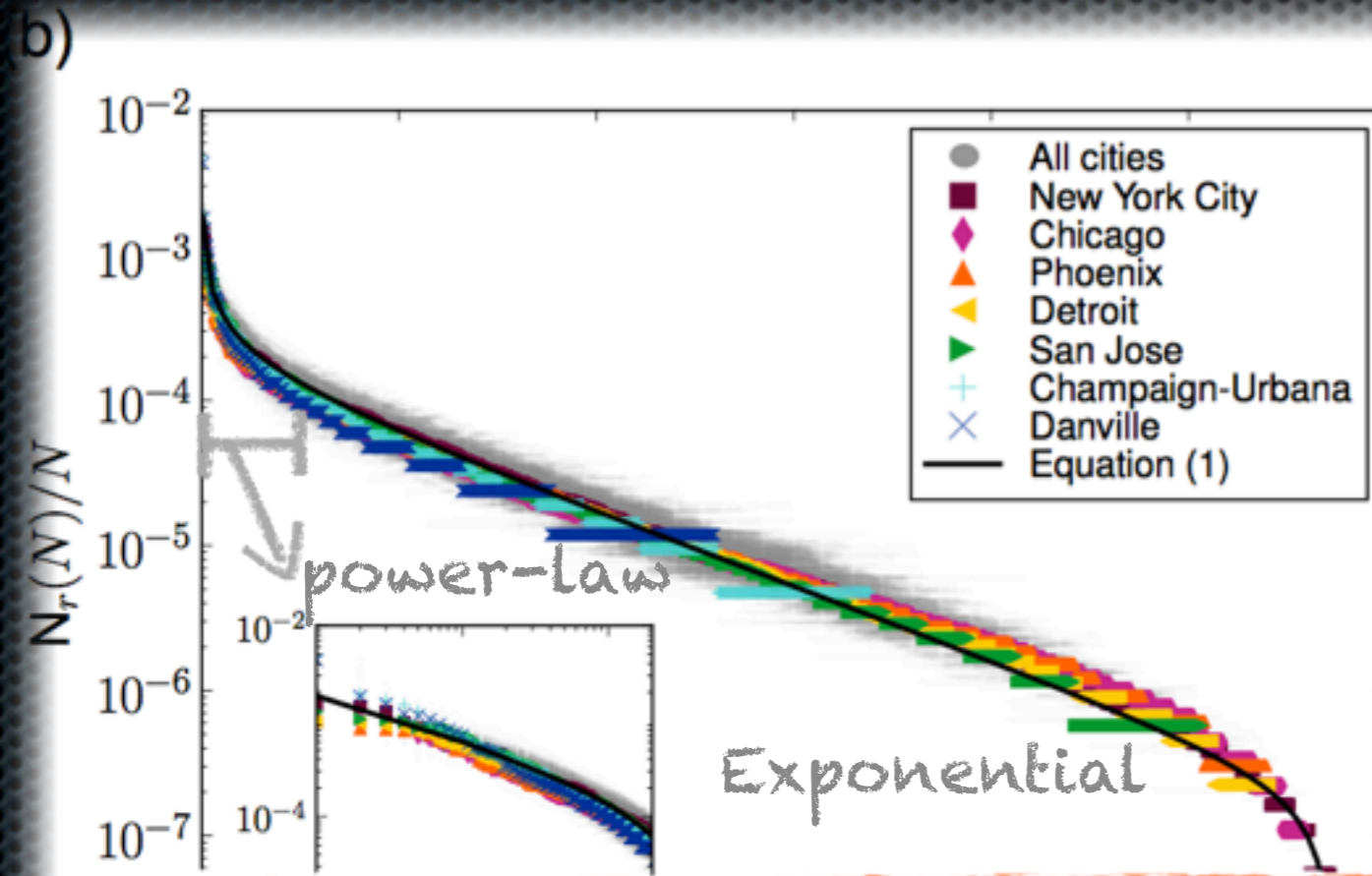
*Normalize by Population Size*

Num

0 200 400 600 800 1000 1200

Rank of NAICS by  $n_i$

# Universal Distribution



- Regardless of **Density** and **Wealth**
- **Common Niche structures** across all cities
- SAME underlying models for

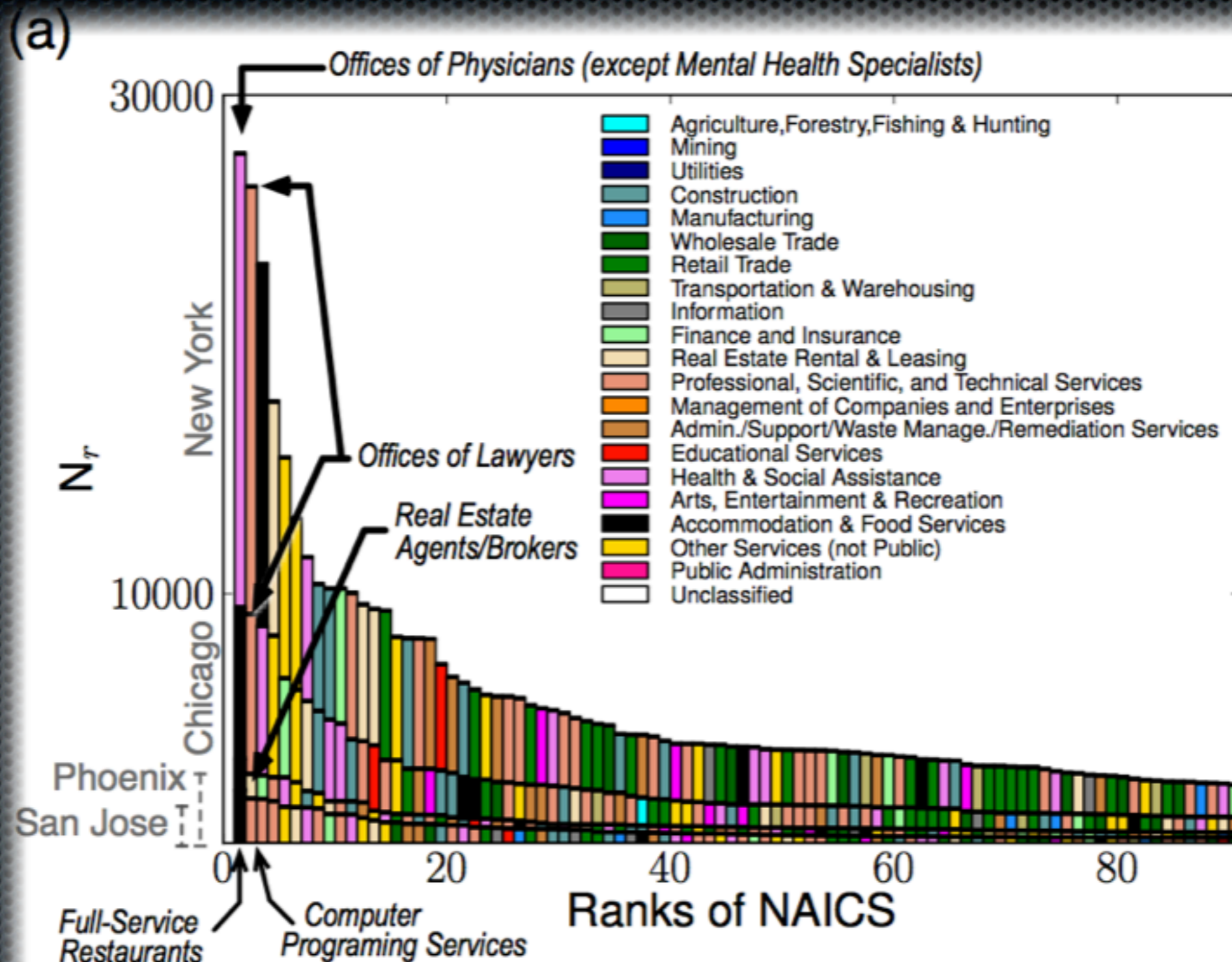
However Special you are,  
You cannot escape from this  
universal distribution!

$$p(r) \sim r^{-\gamma} e^{-r/r_0}$$

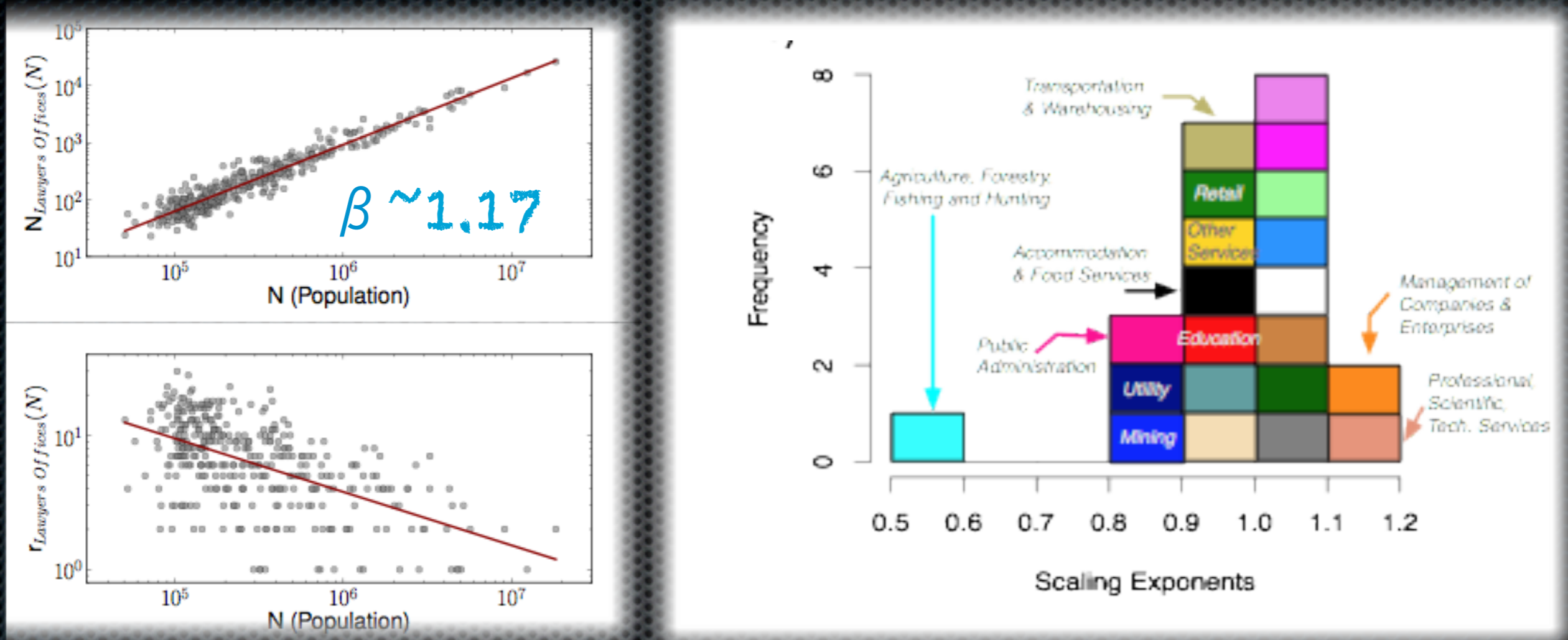
$$J(i, ivf) = \frac{1}{N_0} e^{-\gamma i} \left( 1 + A \frac{i - D_{\max}}{i - D_{\max}} + B \frac{(1+i)^\gamma}{(1+i)^\gamma} \right).$$

# Individual Cities

Number of Firms of given Industry

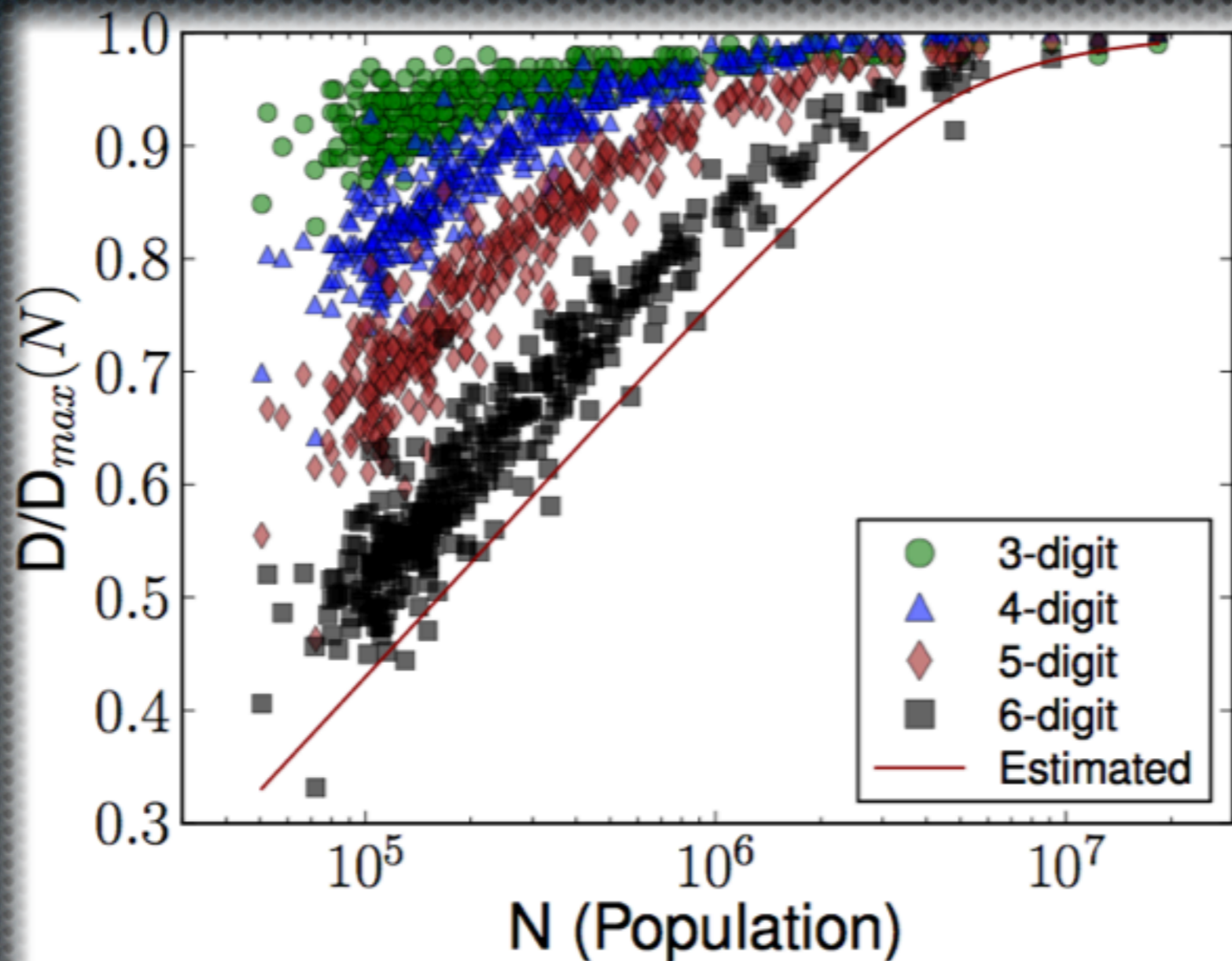


# Systematic Shift of Sectors



- rank  $i = \left\{ N^{(1-\alpha)/\gamma} \right.$  for small  $i < i_0 (1 - \alpha) \log (A)$
- Increases in Productivity, Consumer demand

# Total diversity of cities



- Genuine saturation, combination, not captured refinement

# Conclusion

- Cities are unique in many particular aspects of their economic constitution, no city can deviate substantially from a universal pattern.
- Inherently self-similar not only in terms of their aggregated quantities (GDP, wages, homicides) but also of their internal economic fabric.
- a step forward towards developing a quantitative theory of cities.
- Collaborators: Luis, Jose, Debbie, Geoffrey